

Intro to Solid Mechanics
CIVENG W30/MECENG W85
Summer 2020

Final Exam

Time: 3 hours

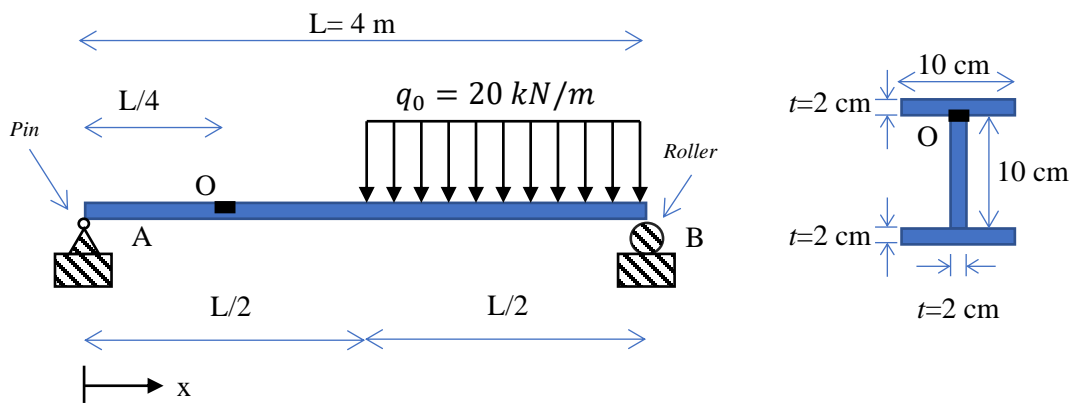
Question	Grade
1	/20
2	/20
3	/25
4	/20
5	/20
Total	/105

Name: _____

ID: _____

Please fill out and submit this page. If not submitted, there will be a **5 points** penalty.

- 1- A beam is under a distributed load as illustrated in the image.
- Find the location and magnitude of the equivalent force of the distributed force and the reaction forces and moments at the supports. (5 points)
 - Calculate the **shear forces** and **internal moment** of the beam as a function of x and plots their diagram. (10 points)
 - Determine the location and value of maximum shear force and internal moment. (5 points)
 - Considering the cross-section illustrated below, what is the shear stress at point O? (5 points)

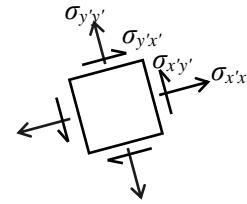
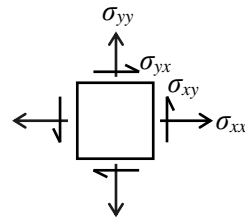
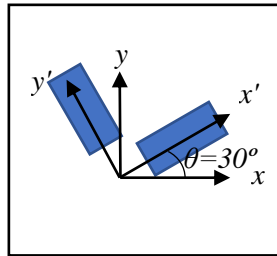


2- The state of stress for a thin plate is given as:

$$\sigma = \begin{bmatrix} 100 & 45 \\ 45 & 90 \end{bmatrix} \text{MPa}$$

in a plane with the normal vector along x . We have attached two strain gauges as shown on this plate.

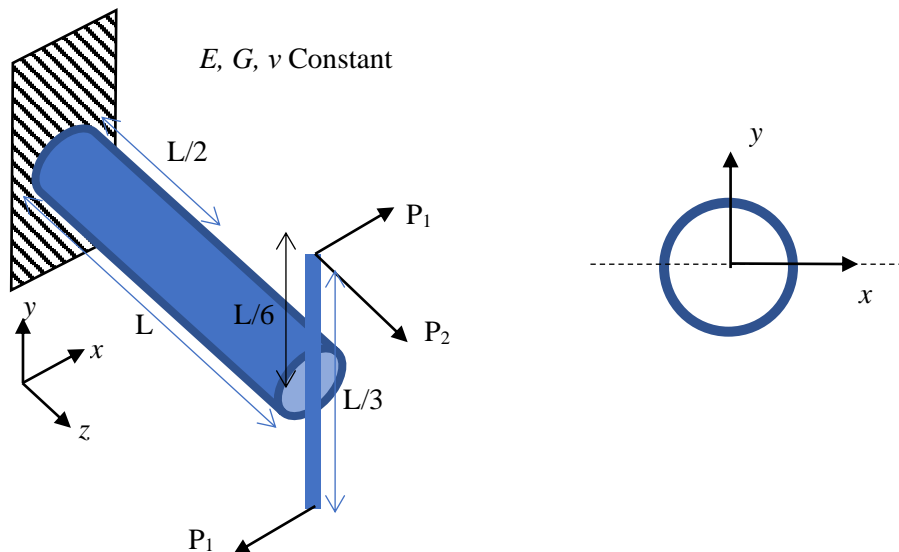
- Using **Mohr Circle** calculate the **strain** values that these two strain gauges would show. ($E = 100 \text{ GPa}$, $\nu = 0.1$). Also, calculate the shear strain in this direction. (10 points)
- Calculate the angle of the primary axes of stress and the corresponding stress values. (5 points)
- Assuming $\sigma_Y = 150 \text{ MPa}$, does this plate break? Use Von-mises criteria to explain your answer. (5 points)



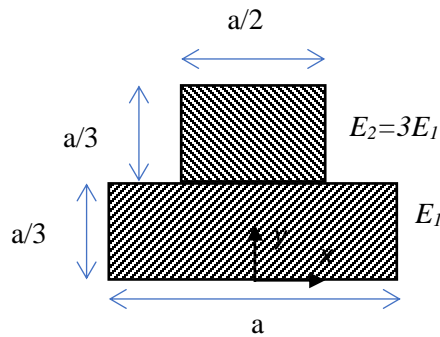
- 3- We have attached a handle to a hollow cylindrical bar with a radius of R and thickness of t ($t \ll R$). Three forces are applied to the handle as shown in the picture, resulting in **torsion, bending, and axial force** on the cylinder.
- Assuming $P_1 = 0$ and $P_2 = 200$ kN, is there any location in the cross-section of the cylinder without any normal stress along z ? If yes, at what value(s) of the y coordinate the normal stress along z would be zero? (5 points)
 - Assuming $P_1 = 100$ kN, $P_2 = 200$ kN, what is the maximum value for the shear stress in this cylinder, and at what location of the cross-section does it happen? (10 points)
 - Use the **eigenvalue method** to calculate the primary stress values at this location. (5 points)
 - Assuming $\tau_Y = 30$ MPa, does this cylinder break under this set of forces? Use Tresca's criteria to explain your answer. (5 points)

$$L = 10 \text{ m}, R = 0.5 \text{ m}, t = 0.01 \text{ m}, I_{xx} = \pi t R^3.$$

Assume the handle is rigid and the attachment between the handle and the cylinder is perfect. The cylinder is fixed to the wall.



- 4- A beam is under a bending moment of $M = 100 \text{ N.m}$. The cross-section of this beam is shown in the image. The upper section and the lower section of the beam are from different materials.
- Find the neutral axis of bending. (5 points)
 - Find the effective bending stiffness. (5 points)
 - Calculate and plot the diagram of the normal strain and stress due to bending. (10 points)



$$a = 0.06 \text{ m}$$

$$E_1 = 100 \text{ GPa}$$

- 5- Consider the truss system shown in the image.
- Calculate the support forces at A and B (5 points).
 - Calculate the axial force in beams 1, 2, and 3. If buckling would occur in either beam 1 or beam 2, determine the maximum force P that we can apply before the structure collapses. Assume all the beams have pin-pin boundary conditions, and $E_1 = E_2$, $I_1 = I_2$. (10 points)
 - If we could choose the second moment of area of beam 1 as a factor of the second moment of area of beam 2 ($I_1 = \alpha I_2$), for what value of α , beam 1 and beam 2 would buckle with the same amount of force P . (5 points)

