

1. (40 pts.) Air at 300 kPa, 100°C is in a piston/cylinder arrangement with a volume of 0.1 m³. It is now compressed in a polytropic process with exponent, $n = 1.2$, to a final temperature of 200°C. You may assume constant properties for air in your calculations.

- a. (5) Calculate the mass of air. $R_{\text{air}} = 0.2870 \text{ kJ/kg K}$.
- b. (5) Calculate the work (and direction) done by the air in the process. The polytropic work equation is $W = \frac{mR}{1-n} (T_2 - T_1)$.
- c. (10) Calculate the heat transfer and direction for the process. (C_p and C_v air are 1.005 and .718 KJ/kg K respectively).
- d. (10) Derive the work equation in (b) above, don't just write down the equation.
- e. (10) Plot (using three points?) the process on a Pv and Tv diagram. Include the equation corresponding to the line you plotted and draw lines of constant temperature and constant pressure on the Pv and Tv diagrams respectively.

Air 100 °C,
300 kPa
Vol 0.1m³

2. (60 pts.) A combined gas-steam power cycle uses a simple gas turbine for the topping cycle and simple Rankine cycle for the bottoming cycle. Atmospheric air enters the gas compressor at 101 kPa and 20 °C, and the maximum gas cycle temperature is 1100 °C. The compressor pressure ratio is 8; the compressor isentropic efficiency is 85 percent; and the gas turbine isentropic efficiency is 90 percent. The gas stream enters and leaves the heat exchanger at points 8 and 9 respectively. Steam flows through the heat exchanger with a pressure of 6000 kPa ($T_{\text{sat}} = 275.6 \text{ °C}$), and leaves at 320 °C. The steam-cycle condenser operates at 20 kPa ($T_{\text{sat}} = 60.1 \text{ °C}$), and the isentropic efficiency of the steam turbine is 90 percent. Use constant specific heats for air at room temperature.

- a. (5) Draw a schematic of the system (a diagram of labeled components with lines connecting them and numbers placed according to the Ts diagram of the process below).
- b. (5) Draw actual processes (non-ideal) 3-4 and 5-6, and the ideal isentropic process 7-8 on the T-s diagram below. Label heat in, heat out, work in and work out on every process where they occur.
- c. (5) Why does process 4 - 1 occur at 20kPa. Does this present any difficulties?
- d. (45) Using symbols only, e.g. T_5 or h_2 , etc. write equations to describe how you would find each of items (i) - (ix) below. If you would consult tables, provide variables used to find the value, e.g. $T_x = T_{\text{sat}} @ y\text{-pressure}$. If quality (x) or work (w) are required, show the steps required to find them. You should have a basis for every independent variable in your equation that you've used to find the dependent variables below, e.g. "given in problem statement as...", or "calculated using...".

- i. T_{6s} and T_{6a}
- ii. T_{8s} and T_{8a}
- iii. T_9
- iv. h_1 and v_1
- v. $W_{\text{pump in}}$
- vi. h_2 isentropic
- vii. h_4 isentropic
- viii. $W_{\text{net, gas cycle}}$
- ix. $W_{\text{net, steam cycle}}$

