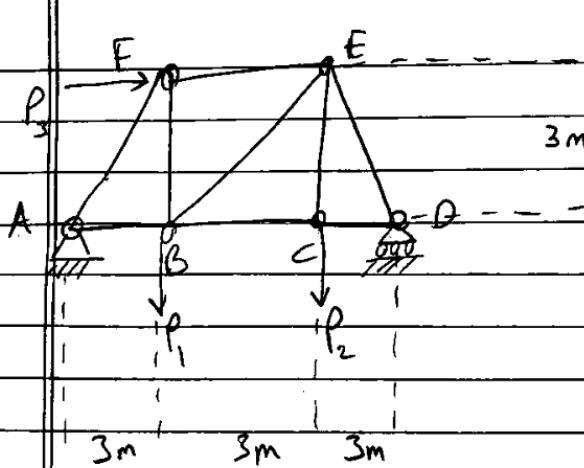


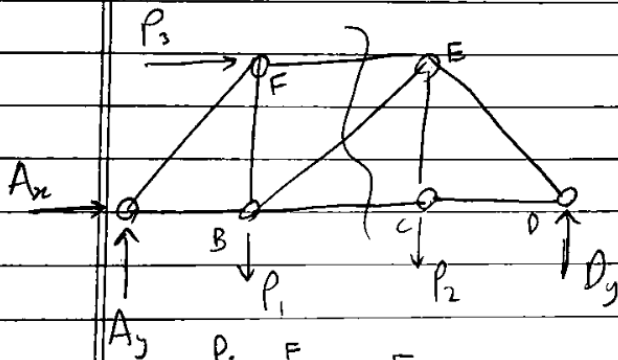
Problem 1



$$P_1 = 6 \text{ kN}$$

$$P_2 = 9 \text{ kN}$$

$$P_3 = 12 \text{ kN}$$

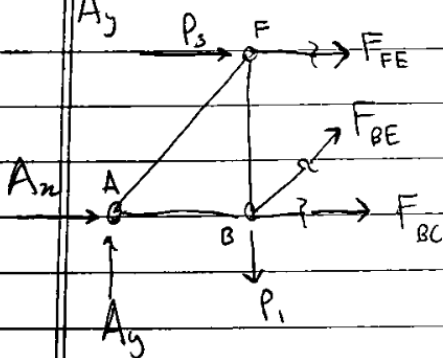


$$\sum M_D = 0$$

$$\hookrightarrow 9A_y + 3P_3 = 6P_1 + 3P_2$$

$$A_y = 3 \text{ kN}$$

$$\sum F_x = 0 \rightarrow A_x = -12 \text{ kN}$$



$$\sum M_B = 0$$

$$\hookrightarrow 3A_y + 3P_3 + 3F_{FE} = 0$$

$$F_{FE} = -3 - 12 = -15 \text{ kN}$$

$$F_{FE} = 15 \text{ kN (C)}$$

$$\sum F_y = 0 \rightarrow A_y - P_1 + \frac{\sqrt{2}}{2} F_{BE} = 0$$

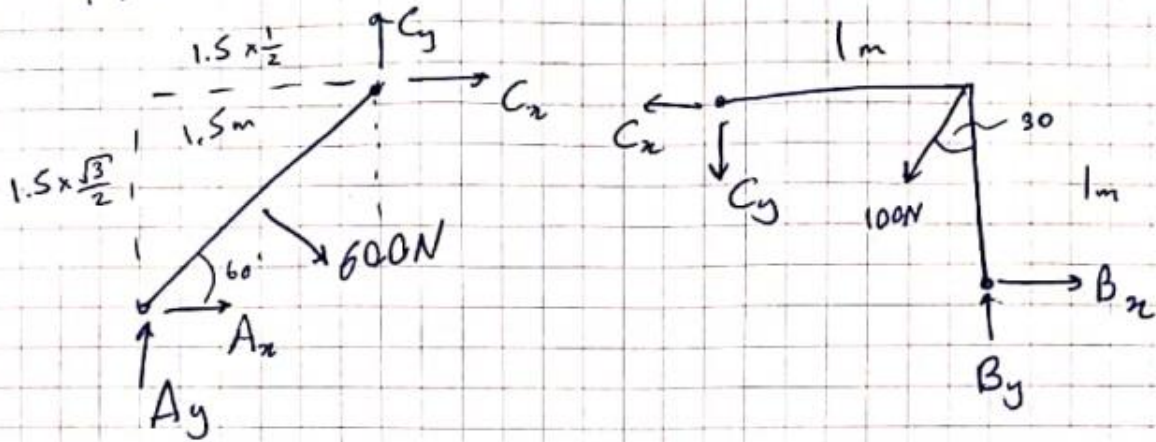
$$F_{BE} = 3\sqrt{2} \text{ (T)}$$

$$\sum F_x = 0 \rightarrow P_3 + F_{FE} + A_x + F_{BC} + \frac{\sqrt{2}}{2} F_{BE} = 0$$

$$F_{BC} = 12 \text{ kN (T)}$$

Problem 2

Find forces on pin C.



$$\begin{aligned} \sum M_A = 0 &\rightarrow 600 \times 0.75 + C_x \times \frac{1.5\sqrt{3}}{2} - C_y \times 1.5 = 0 \\ &\Rightarrow 600 \times \frac{3}{4} + C_x \frac{3\sqrt{3}}{4} - C_y \frac{3}{4} = 0 \end{aligned}$$

$$\Rightarrow \sqrt{3} C_x - C_y = -600 \quad \text{--- (1)}$$

$$\sum M_B = 0 \rightarrow C_x + C_y + 100 \sin 30 = 0$$

$$C_x + C_y = -50 \quad \text{--- (2)}$$

from (1) & (2) \Rightarrow

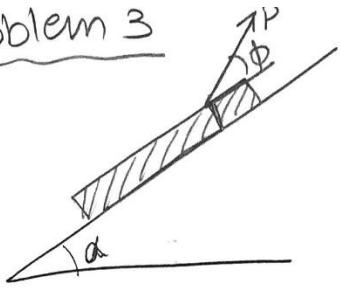
$$\sqrt{3} C_x - (-50 - C_x) = -600$$

$$C_x (\sqrt{3} + 1) = -650$$

$$C_x = -\frac{650}{\sqrt{3} + 1}$$

$$C_y = -50 + \frac{650}{\sqrt{3} + 1}$$

Problem 3

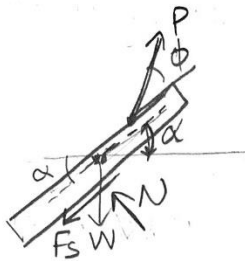


Pipe of weight W

• show that for slipping $P = \frac{W \sin(\alpha + \theta)}{\cos(\phi - \theta)}$

where $\theta = \tan^{-1} \mu_s$ (μ_s is static friction coefficient).

FBD



Along the inclined plane right before the pipe starts moving we have $\sum F = 0$ and $F_s = \mu_s N$, therefore

$$P \cos \phi - F_s - W \sin \alpha = 0$$

$$\text{or } \boxed{P \cos \phi - \mu_s N - W \sin \alpha = 0} \quad \text{⊕}$$

Also, we have $\sum F = 0$ perpendicular to the inclined plane, hence

$$P \sin \phi + N - W \cos \alpha = 0 \Rightarrow \boxed{N = W \cos \alpha - P \sin \phi} \quad \text{⊕⊕}$$

From ⊕ and ⊕⊕ we get:---

$$P \cos \phi - \mu_s W \cos \alpha + \mu_s P \sin \phi - W \sin \alpha = 0$$

$$P (\cos \phi + \mu_s \sin \phi) = \mu_s W \cos \alpha + W \sin \alpha \quad \mu_s = \tan \theta$$

$$P \left(\cos \phi + \frac{\sin \theta}{\cos \theta} \sin \phi \right) = \frac{\sin \theta}{\cos \theta} W \cos \alpha + W \sin \alpha$$

$$P (\cos \phi \cos \theta + \sin \theta \sin \phi) = W (\cos \alpha \sin \theta + \cos \theta \sin \alpha)$$

$$\Rightarrow \boxed{P = \frac{W \sin(\alpha + \theta)}{\cos(\phi - \theta)}}$$