

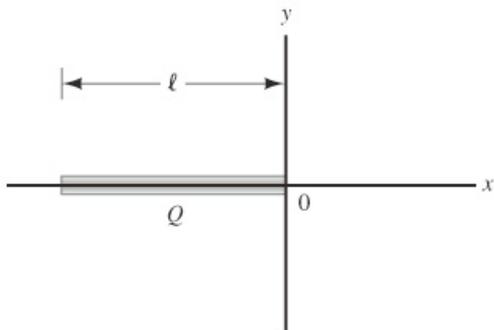
University of California, Berkeley  
Physics 7B, Fall 2008 (*Xiaosheng Huang*)

**Midterm 2**  
Monday, 11/3/2007  
6:30-8:30 PM

Name: \_\_\_\_\_ D/L Section: \_\_\_\_\_



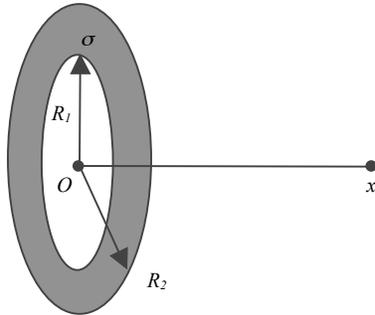
1) (20 pts.) A thin rod of length  $l$  carries a total charge  $Q$  distributed uniformly along its length. Determine the electric field along the axis of the rod starting at one end. That is, find  $\mathbf{E}(x)$  for  $x \geq 0$  in the figure below, both its direction and magnitude.



Answer:



2) (20 pts.) A flat ring of inner radius  $R_1$  and outer radius  $R_2$  (see the figure below) carries a uniform surface charge density  $\sigma$ .



a) Find the electric potential along the axis (the  $x$  axis), assuming the electric potential at infinity is zero.

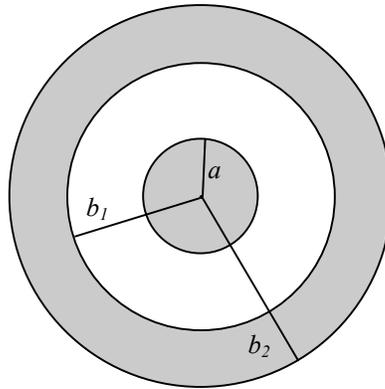
Answer:

b) Find the magnitude and the direction of the electric field along the axis by using the relationship between the electric potential and the electric field.

Answer:



3) (25 pts.) A capacitor consists of two concentric spherically-shaped conductors. The smaller one has radius  $a$ , and the larger one has inner radius  $b_1$  and outer radius  $b_2$ .



If we put  $-q_1$  on the smaller conductor and  $+q_2$  on the larger one, assuming  $q_2 > q_1 > 0$ , find the electric field (magnitude and direction) for  
a)  $r < a$ ;

Answer:

b)  $a < r < b_1$ ;

Answer:

c)  $b_1 < r < b_2$ ;

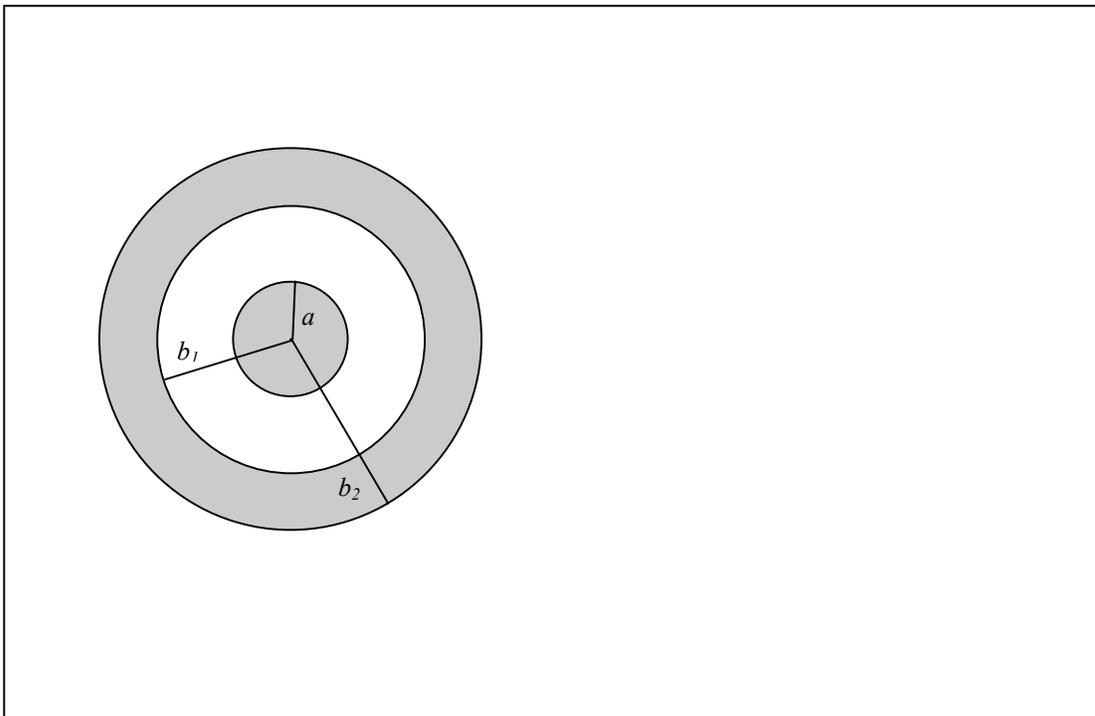
Answer:

d)  $r > b_2$ ;

Answer:

e) use the picture below and words, if necessary, to describe how the charge is distributed on the two conductors.

Answer:



f) If  $q_1 = q_2$  (but the two conductors still carry opposite charge), find the electric potential difference between the two conductors.

Answer:

g) Find the capacitance of this capacitor.

Answer:



4) (15 pts.) Two resistors when connected in series to a battery with voltage  $V_0$  use one-fourth the power that is used when they are connected in parallel. If one resistor has resistance  $R_1$ , what is the resistance of the other?

Answer:



5) (20 pts) A conductor is charged after it is brought into contact with a metal plate, which initially had charge  $Q$ . The conductor now has charge  $q$ .

Suppose the electric potential of the metal plate after the contact is  $V$  relative to infinity. (That is, take the electric potential to be zero at infinity.)

a) What is the electric potential of the conductor after the contact?

Answer:

b) Find the charge on the metal plate after the contact.

Answer:

c) Find the capacitance of the conductor,  $C_c$ .

Answer:

d) Find the capacitance of the metal plate,  $C_p$ .

Answer:

e) Find the ratio  $C_p/C_c$  in terms of  $Q$  and  $q$ .

Answer:

After the metal plate is recharged to the same initial charge  $Q$ , the conductor is brought into contact with the metal plate a second time. Suppose the metal plate loses an amount of charge  $x$ .

f) Find the charge on the conductor.

Answer:

g) Find  $x$  in terms of  $Q$  and  $q$ .

Answer:

We can add more charge to the conductor by repeatedly contacting it with the metal plate, which after each contact is recharged to the same amount of charge  $Q$ , until the charge on the conductor reaches a maximum.

h) What is the ultimate charge on the conductor?

Answer: