

1.

| Stage | P (kPa) | T(C) | v (m ³ /kg) | u (kJ/kg) | h (kJ/kg) | x |
|-------|---------|------|------------------------|-----------|-----------|--------|
| 1 | 101.42 | 100 | 0.2851 | 773.85 | 802.76 | 0.17 |
| 2 | 101.42 | 100 | 0.4332 | 958.8 | 1002.76 | 0.2586 |
| 3 | 1000 | 100 | 0.001043 | 419.06 | 419.17 | - |
| 4 | 1000 | 600 | 0.40111 | 3297.5 | 3698.6 | - |
| 5 | 10 | 600 | 40.296 | 3303.3 | 3703.3 | - |

| Process | Q (kJ) | W (kJ) |
|---------|---------|--------|
| 1 to 2 | 1000 | 75.25 |
| 2 to 3 | -2917.9 | -219.2 |
| 3 to 4 | 16397 | 2004.8 |
| 4 to 5 | 9315 | 9286 |

2.

| | T [C] | P [kPa] | v [m ³ /kg] | u [kJ/kg] | h [kJ/kg] | x [-] | State |
|---|-------|---------|------------------------|-----------|-----------|--------|-------------------|
| 1 | 80 | 1000 | 0.001029 | 334.97 | 335.02 | - | Compressed liquid |
| 2 | 160 | 618.28 | 0.1490 | 1589.9 | 1682 | 0.4834 | Saturated mixture |
| 3 | 350 | 800 | 0.35442 | 2878.6 | 3162 | - | Superheated vapor |
| 4 | 500 | 5 | 71.36 | 3132.9 | 3489.7 | - | Superheated vapor |
| 5 | 500 | 10 | 35.68 | 3133 | 3489.7 | - | Superheated vapor |
| 6 | 190 | 1255.2 | 0.1051 | 2000 | 2132.6 | 0.67 | Saturated mixture |

ME40 Spring 2017 MID #1

①

$$T_1 = 100^\circ\text{C}$$

$$x = 0.17 \rightarrow \text{mixture}$$

$$\Rightarrow P_1 = 101.42 \text{ kPa}$$

$$v_1 = v_f + x v_{fg} = 0.001043 + 0.17(1.6720 - 0.001043) = 0.2851 \text{ (m}^3/\text{kg)}$$

$$u_1 = u_f + x u_{fg} = 773.85 \text{ kJ/kg}$$

$$h_1 = 802.76 \text{ kJ/kg}$$

$$1 \rightarrow 2 : Q_{12} = \Delta U_{12} + W_{12} = \Delta H_{12}$$

$$\frac{1000 \text{ kJ}}{5 \text{ kg}} = h_2 - h_1$$

$$h_2 = 802.76 + 200 = 1002.76 \text{ (kJ/kg)}$$

$$P_2 = P_1 = 101.42 \text{ kPa}$$

$$\Rightarrow x_2 = \frac{h_2 - h_f}{h_{fg}} = \frac{1002.76 - 419.17}{2256.4} = 0.2586$$

$$v_2 = 0.4332 \text{ m}^3/\text{kg}$$

$$u_2 = 958.8 \text{ kJ/kg}$$

$$1 \rightarrow 2 : Q_{12} = 1000 \text{ kJ}$$

$$W_{12} = Q_{12} - \Delta U_{12} = Q_{12} - m(u_2 - u_1) = 75.25 \text{ kJ}$$

$$T_3 = 100^\circ\text{C}$$

$$P_3 = 1 \text{ MPa}$$

$$\Rightarrow v_3 \approx v_f @ 100^\circ\text{C} = 0.001043 \text{ m}^3/\text{kg}$$

$$u_3 \approx 419.06 \text{ kJ/kg}$$

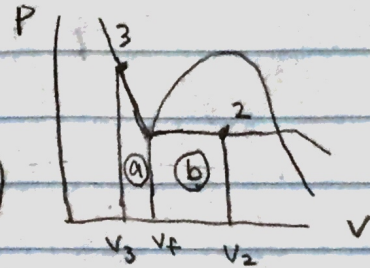
$$h_3 \approx 419.17 \text{ kJ/kg}$$

$$2 \rightarrow 3 : W_{23} = \int_2^3 P dV$$

$$= (a) + (b)$$

$$\left(\begin{array}{l} \text{since } v_3 \approx v_f \\ (a) \rightarrow 0 \end{array} \right)$$

$$\approx (b)$$



$$W_{23} = m P_2 (v_f - v_2) = -219.2 \text{ kJ}$$

$$Q_{23} = \Delta U_{23} + W_{23} = -2917.9 \text{ kJ}$$

$$\left. \begin{array}{l} T_4 = 600^\circ\text{C} \\ P_4 = 1 \text{ MPa} \end{array} \right\} \rightarrow \text{superheated vapor}$$

$$\Rightarrow v_4 = 0.40111 \text{ m}^3/\text{kg}$$

$$u_4 = 3297.5 \text{ kJ/kg}$$

$$h_4 = 3698.6 \text{ kJ/kg}$$

$$3 \rightarrow 4 : Q_{34} = \Delta H_{34} = m (h_4 - h_3) = 16397 \text{ kJ}$$

$$W_{34} = Q_{34} - \Delta U_{34} = 2004.8 \text{ kJ}$$

$$\left. \begin{array}{l} T_5 = 600^\circ\text{C} \\ P_5 = 10 \text{ kPa} \end{array} \right\} \rightarrow \text{Superheated vapor}$$

$$\Rightarrow v_5 = 40.296 \text{ m}^3/\text{kg}$$

$$u_5 = 3303.3 \text{ kJ/kg}$$

$$h_5 = 3703.3 \text{ kJ/kg}$$

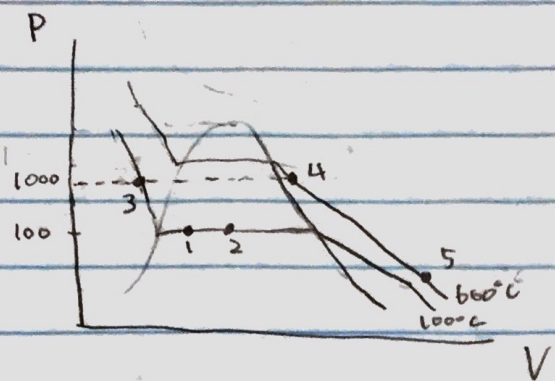
$$4 \rightarrow 5 : \text{approximately ideal gas}$$

$$W_{45} = \int_4^5 P dV = mRT \ln \left(\frac{v_5}{v_4} \right)$$

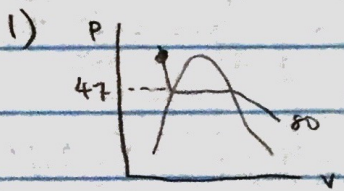
$$= (5)(0.4615)(873) \ln \left(\frac{40.296}{0.40111} \right)$$

$$= 9286 \text{ (kJ)}$$

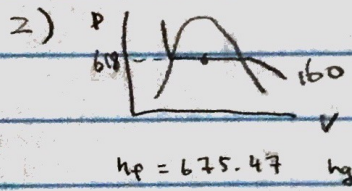
$$Q_{45} = \Delta U_{45} + W_{45} = m(u_5 - u_4) + W_{45} = 9315 \text{ (kJ)}$$



2)

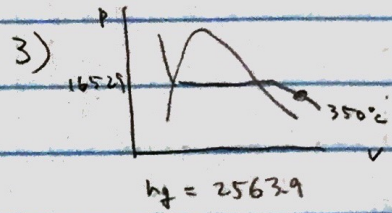


$v = 0.001029 \text{ m}^3/\text{kg}$
 $u = 334.97 \text{ kJ/kg}$
 $h = 335.02 \text{ kJ/kg}$
 comp. liq.



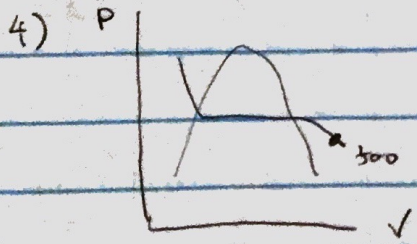
$h_f = 675.47$ $h_g = 2757.5$

$x = \frac{h - h_f}{h_{fg}} = 0.4834$
 $u = u_f + x u_{fg} = 1589.9 \text{ kJ/kg}$
 $P = 618.28 \text{ kPa}$ $v = 0.1490 \text{ m}^3/\text{kg}$
 Sat. mix



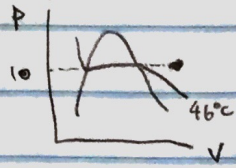
$h_f = 2563.9$

s. h. vap
 $P = 0.8 \text{ MPa}$
 $v = 0.35442 \text{ m}^3/\text{kg}$
 $u = 2878.6 \text{ kJ/kg}$



s. h. vap \rightarrow ideal gas $u, h = f(T)$
 $[PV]_{10 \text{ kPa}, 300^\circ\text{C}} = [PV]_{5 \text{ kPa}, 300^\circ\text{C}} \Rightarrow v = 71.36 \text{ m}^3/\text{kg}$
 $u = 3132.9 \text{ kJ/kg}$
 $h = 3481.7 \text{ kJ/kg}$

5)



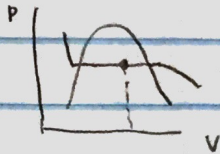
s: h. vap

$$T = 500^\circ\text{C}$$

$$h = 3489.7 \text{ kJ/kg}$$

$$v = 37.68 \text{ m}^3/\text{kg}$$

6)



sat. mix

$$u = u_f + x u_{fg}$$

$$2000 = u_f + 0.67 u_{fg}$$

$$u_{fg} = \frac{2000 - u_f}{0.67}$$

Trial & error

$$T = 190^\circ\text{C}$$

$$P = 1255.2 \text{ kPa}$$

$$v = 0.001141 + 0.67 (0.15636 - 0.001141)$$

$$= 0.1051 \text{ m}^3/\text{kg}$$

$$h = 2132.6 \text{ kJ/kg}$$