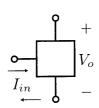
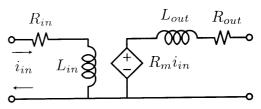
Midterm Exam (closed book) Tuesday, October 19, 2004

Guidelines: Closed book. You may use a calculator. Do not unstaple the exam. *Warning*: Illustrations not to scale.

1. A new device has been invented with the following I-V characteristic:

$$V_o = -K_v \frac{1}{1 + \left(\frac{I_{in}}{I_p}\right)}$$





This relation holds for $I_{in} > 0$ and for any passive termination. The device parameters are as follows: $I_p = 750 \,\mu\text{A}$, $K_v = .6 \,\text{V}$. A small-signal model including layout parasitics is shown above.

(a) (6 points) Calculate an expression for the maximum gain of the amplifier at 10 GHz. Note:

$$G_{Tu,max} = \frac{|z_{21}|^2}{4\Re(z_{11})\Re(z_{22})}$$

By inspection
$$2\pi = Rin + j\omega Lin$$
 $2m = Rout + j \omega Lin$
 $2m = Rout + j \omega Lin$

$$2n = Rout$$

$$2n = Rin + j\omega Lin$$

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$$2n = Rin + j\omega Lin$$

$$2n = R$$

(b) (10 points) Design a matching network to acheive an input match with $R_S = 50 \Omega$. Assume that $R_{in} = 5 \Omega$ and $L_{in} = 3 \text{ nH}$. Draw the complete input network to the amplifier and specify the bandwidth of the match. Note that $f_0 = 10 \text{ GHz}$.

$$Q = \sqrt{\frac{50}{5}} - 1 = 3$$

$$X_5 = 3 \times 5 = 15$$

$$X_7 = (1 + 0^2) \cdot 5$$

$$X_7 = (1 + 2^2) \cdot 3 = (16675) \quad (= 954.7 \text{ FF})$$

$$C = 78.4f \quad (5evius combination)$$

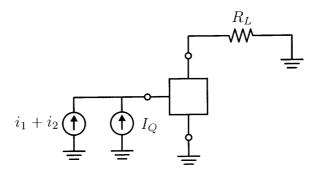
$$L_7 = 265.3 \text{ ptf}$$

$$Cres = 84.66f$$

$$78.4f$$

$$265.3 \text{ pt}$$

$$B = \frac{40}{2} = \frac{106}{3} = 3.336 \text{ Hz}$$



(c) (10 points) For the circuit shown above, calculate the IM_3 at low frequency for two current input signals at 100 MHz and 101 MHz of magnitude 100 μ A. The circuit is biased as shown with $I_Q=2\,\mathrm{mA}$.

$$V_{0} = -k_{V} \frac{1}{(+\frac{i_{M}+I_{A}}{I_{P}})}$$

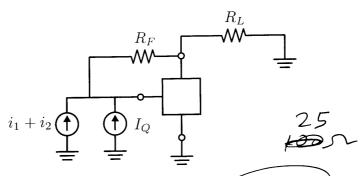
$$= -k_{U} \frac{1}{(+\frac{I_{A}}{I_{P}})(1+\frac{i_{M}}{I_{X}})} \frac{I_{X} = \frac{1}{I_{P}+I_{A}}}{I_{X} = \frac{1}{I_{P}+I_{A}}}$$

$$V_{0} = -k_{U} \frac{1}{(+\frac{I_{A}}{I_{P}})(1+\frac{i_{M}}{I_{X}})} \frac{I_{X} = \frac{1}{I_{Y}+I_{A}}}{I_{X} = \frac{1}{I_{Y}}}$$

$$V_{0} = -k_{U} \frac{1}{(+\frac{I_{A}}{I_{P}})(1+\frac{I_{A}}{I_{X}})}{I_{X} = \frac{1}{I_{X}}} \frac{I_{X} = \frac{1}{I_{X}}}{I_{X}} + \cdots$$

$$I_{X} = \frac{1}{I_{X}} \frac{1}{I_{X}} \frac{I_{X}}{I_{X}} + \cdots$$

$$I_{X} = \frac{3}{4} \frac{1}{(I_{X})} \frac{I_{X}}{I_{X}} = \frac{3}{4} \frac{1}{I_{X}} \frac{I_{X}}{I_{X}} = \frac{3}{4} \frac{1}{1} \frac{I_{X}}{I_{X}} = \frac{3}{4$$



(d) (10 points) Assume a shunt feedback resistor of value $R_F = 1 \text{ k}\Omega$ is added to the circuit. Calculate HD_2 under this condition. Assume $R_F \gg R_{in}$.

Circuit. Calculate
$$HD_2$$
 under this condition. Assume $HF \gg I_{th}$.

$$i_F = \frac{V_0}{RF} \qquad f = \frac{I}{RF}$$

$$T = q_1 f = \frac{Rm}{RF}$$

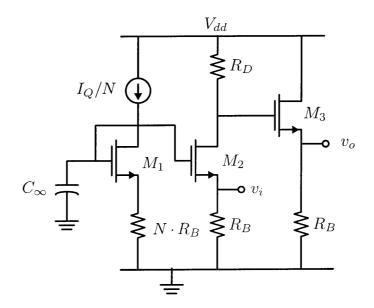
$$R_m = \frac{KV}{I + \frac{I}{2}} \qquad I_X = \left(\frac{\partial \cdot 6}{(1 + \frac{2m}{\partial \cdot 75})}\right) \qquad \frac{1}{2.75} m$$

$$= 5q.5 = 2.38$$

$$T = \frac{5q.5}{25} = 2.38$$

$$\begin{aligned}
|HD_2 &= \int_{2}^{2} \frac{q_2}{q_1^2} \frac{1}{1+T} & \delta_{om} \\
&= \int_{2}^{2} \frac{1}{q_1^2} \frac{1}{1+T} & \delta_{om} \\
&= \int_{2}^{2} \frac{1}{\sqrt{1+T}} \frac{1}{\sqrt{1+T}} & \delta_{om} \\
&= \int_{2}^{2} \frac{1}{\sqrt{1+T}} & \delta_{om}$$

 $\frac{1}{2} \left(\frac{1}{1 + \frac{Ia}{4p}} \right) \left(\frac{1}{1 + T} \right)$ Som = -21 dBc



- 2. The amplifier shown above is designed in a triple-well process (body and source are shorted). Assume that the resistor $R_B \gg \frac{1}{g_m}$ and $R_D \ll r_o$.
 - (a) (10 points) Calculate the bandwidth of the above amplifier. Assume the amplifier is designed for an input and output match.

DRAIN OF M2

$$C_{tot} = C_{db2} + C_{\mu 1} + \frac{C_{353}}{1+9_{m3}n_3} + C_{\mu 2}$$

$$R_{tot} = R_D$$

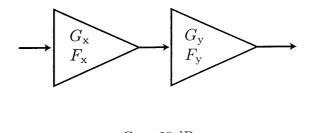
$$T = R_D C_{tot}$$

$$f = L_{2trt}$$

(b) (10 points) Calculate $G_{T,max}$ for this amplifier. Explain your assumptions.

(c) (16 points) Calculate the noise figure for the amplifier. Assume the amplifier is driven by a source with resistance R_S and loaded by a matched load $R_L = R_S$. Assume the amplifier is designed for an input and output match. Ignore gate noise.

3. You would like to design an amplifier with a power gain of 50 dB from two amplifiers, each with the following characteristics:



$$G_1 = 30 \, dB$$

 $NF_1 = 1.7 \, dB = 1.479$

$$G_2 = 20 \, dB$$

 $NF_2 = 1.3 \, dB$ = 1.349

(a) (8 points) Find the optimal ordering of the amplifiers in cascade to acheive the lowest possible noise figure.

$$F_{12} = F_{1} + \frac{F_{2}-1}{G_{1}} = 1.479$$

$$F_{21} = 1.349 + \frac{0.479}{100} = 1.354$$

$$ORDER 2-1 () SETTER$$

$$M_{1} = \frac{G_{1}F_{1}-1}{G_{1}-1} = 1.479$$

$$M_{2} = 1.353$$

(b) (10 points) Find the lowest possible signal power (minimum detectable signal) to maintain an $SNR_o > 10$ dB. Assume the input noise is from a source resistance $R_S = 50 \Omega$ and the communication bandwidth is 1 MHz.

$$SNR_0 = \frac{SNR_i}{F} > 10$$

 $SNR_i > 10 \cdot F = (3.54)$
 $P_i > 13.54 \cdot P_{noise} = 13.54 \cdot kT \cdot B$
 $= (3.54 \cdot 4 \times 10^{-21} \text{ W} \cdot 10^6 = 5.42 \times 10^{-14} \text{ W}$
 $= -103 \text{ dBm}$

(c) (10 points) Assume that the system is designed to work with a signal as large as $-10 \,\mathrm{dBm}$. What's the requires IIP_3 for the entire system to maintain a signal-to-distortion $SDR > 10 \,\mathrm{dB}$.

SDR 710

$$\frac{Pi}{Pd}$$
 70 \Rightarrow $Pd = \frac{Pi}{10} = \frac{0.1 \text{mW}}{10} = 0.0 \text{lmW}$
 IM_3 DEGRADES BY $2d3/(aB)$ (NPTT

 $INPOT$ INCREASES BY $5d3 \Rightarrow IM_3 = 0d3$
 $IIP_3 = -10dBm + 5d3m = -5dBm$