

Midterm 1

General Notes:

- You are allowed to bring in one sheet of notes
- All loading combinations should follow ASD
- For a member to be acceptable, its demand/capacity ratio must be equal to or less than 1.00 and it must meet any stated deflection criteria
- Do not reduce any live loads unless asked to
- Box, cloud, or highlight final answers
- When making assumptions, clearly state what they are

		Maximum
Problem 1	10	10
Problem 2	10	10
Problem 3	15	15
Problem 4	15	15
Total	<u>50</u>	50

Good luck!

V. Good!

Problem 1 (10 pts)

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Match the definitions to the appropriate terms:

Def. #	Definition	Term	Def. #
1. ✓	Lumber from 2"-4" (nominal) thick by min. 2" wide	Cal	12
2. ✓	Structure and orientation of wood fibers in a member	Stanford	11
3. ✓	Horizontal distributed framing member; typically loaded in bending	Mud Sill	9
4. ✓	Vertical distributed framing member; typically loaded both axially and in bending	Grain	2
5. ✓	Solid-sawn member larger than 5x5	Header	10
6. ✓	Horizontal, flat member framing the top and bottom of wall panels	King Stud	7
7. ✓	Full-height stud adjacent to opening	Nominal Size	8
8. ✓	Designated member size; actual (dressed) dimensions are smaller	Dimensional Lumber	1
9. ✓	Sill connected to foundation; typically pressure-treated for decay	Timber	5
10. ✓	Beam framed over opening	Plate	6
11. ✓	Over-rated, elitist engineering school. (community college)	Joist	3
12. ✓	The best engineering program with the brightest students.	Stud	4

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Problem 2 (10 pts)

Find F_b , F_v and E' for the following members:

- a) 2x4, Doug Fir-Larch #2; D+L+0.6W
- b) 2x10 Doug Fir-Larch #1; D+L; Joists spaced at 16" o.c. & sheathed for load sharing
- c) 6x12 Alaska Cedar Select Structural; D+Lr; Wet service (MC > 19%);

a). Dimension Lumber.

DFL #2 from Table 4A:

$$F_b = 900 \text{ psi}, F_v = 180 \text{ psi}, E = 1.6 \times 10^6 \text{ psi}$$

$$C_D = 1.6, C_F = 1.5 \text{ all other factors per 1.0}$$

$$F_b' = (F_b)(1.6)(1.5) = \boxed{2160 \text{ psi}}$$

$$F_v' = (F_v)(1.6) = \boxed{288 \text{ psi}}$$

$$E' = E = \boxed{1.6 \times 10^6 \text{ psi}}$$

b). Dimension Lumber.

DFL #1 from table 4A:

$$F_b = 1000 \text{ psi}, F_v = 180 \text{ psi}, E = 1.7 \times 10^6 \text{ psi}$$

$$C_D = 1.0, C_r = 1.15, C_F = 1.1 \text{ all other factors are zero}$$

$$F_b' = (F_b)(1.0)(1.15)(1.1) = \boxed{1265 \text{ psi}}$$

$$F_v' = (F_v)(1.0) = \boxed{180 \text{ psi}}$$

$$E' = E = \boxed{1.7 \times 10^6 \text{ psi}}$$

c) Timber, $(d-b) \geq 2" \rightarrow$ beams and stringer

Alaska Cedar Select Structural from table 4D:

$$F_b = 1400 \text{ psi}, F_v = 155 \text{ psi}, E = 1.2 \times 10^6 \text{ psi}$$

$$C_D = 1.25, C_M = 1.0 \text{ for } F_b, F_v, E, C_F = 1.0 \text{ since } d \leq 12.0$$

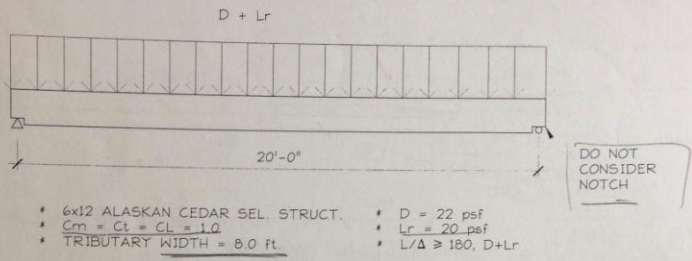
$$F_b' = (1400 \text{ psi})(1.25)(1.0)(1.0) = \boxed{1750 \text{ psi}}$$

$$F_v' = (155 \text{ psi})(1.25)(1.0) = \boxed{194 \text{ psi}}$$

$$E' = (1.2 \times 10^6 \text{ psi})(1.0) = \boxed{1.2 \times 10^6 \text{ psi}}$$

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Problem 3 (15 pts)



Based on the diagram above, find the following:

- Find the demand-capacity ratio for bending, $D/C = f_b/F'_b$
- Using the full beam depth, find the demand-capacity ratio for shear, $D/C = f_v/F'_v$
- Find the $(D + L_r)$ deflection ratio, L/Δ
- Is the beam adequate? What controls the design?

a). F'_b was determined in problem 2 c) as 1730 psi.

$$A_t = 8' \times 20' = 160 \text{ ft}^2 < 200 \text{ ft}^2 \Rightarrow R_1 = 0$$

$$F = 0 \Rightarrow R_2 = 0$$

$L_r = 20$ psf. (no reduction).

$$\text{Load case: } D+L_r = 22 \text{ psf} + 20 \text{ psf} = 42 \text{ psf (w-total)}$$

$$\text{linear w: } (42 \text{ psf}) (8 \text{ ft}) = 336 \text{ plf}$$

$$M_{\text{max}} = \frac{wl^2}{8} = \frac{(336 \text{ plf})(20')^2}{8} = 16800 \text{ lb-ft}$$

$$S_{xx} = 121.2 \text{ m}^3 \text{ from table 1B}$$

$$f_b = \frac{M}{S} = \frac{(16800 \text{ lb-ft})(12 \text{ in/ft})}{121.2 \text{ m}^3} = 1664 \text{ psi}$$

$$\frac{D}{C} = \frac{1664 \text{ psi}}{1730 \text{ psi}} = 0.95 \rightarrow \text{OK}$$

\Rightarrow part b), c), d)

b) F_i was determined in part c) of problem 2 to be 194 psi

$$V_{max} = \frac{wL}{2} = \frac{(336 \text{ plf})(20')}{2} = 3360 \text{ lb}$$

$$f_v = \frac{3}{2} \frac{V}{A}, \text{ where } A = 63.25 \text{ in}^2 \text{ from table 1B}$$

$$f_v = \frac{3}{2} \frac{3360 \text{ lb}}{63.25 \text{ in}^2} = 79.7 \text{ psi}$$

notches are not considered, thus:

$$\frac{P}{C} = \frac{f_v}{F_i} = \frac{79.7 \text{ psi}}{194 \text{ psi}} = 0.41 \rightarrow \text{ok}$$

$$c) \Delta_{allow} = \frac{L}{180} = \frac{(20')(12)}{180} = 1.33''$$

$$\Delta_{DHLr} = \frac{5wL^4}{384EI}, \quad E' = 1.2 \times 10^6 \text{ psi} \text{ (as in part c) of problem 2}$$

$$\Delta_{DHLr} = \frac{(5)(336 \text{ plf})(1' \text{ ft}/12 \text{ inches})(20' \times 12)^4}{(384)(1.2 \times 10^6 \text{ psi})(697.1 \text{ in}^4)}$$

$$= 1.45''$$

$$\frac{L}{\Delta_{DHLr}} = \frac{(20')(12)}{1.45''} = 166 < 180 \text{ Not good!}$$

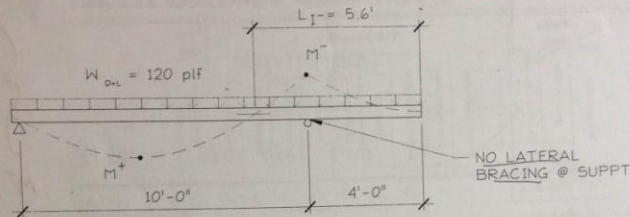
$$\frac{D}{C} = \frac{180}{166} = 1.09$$

d) According to the results from part a) - c), the beam is inadequate as it fails to achieve allowable deflection. The controlling criterion is the one with the highest P/C ratio, which is the deflection (due to DHLr)

Good

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Problem 4 (15 pts)



- * 2x10 DF-L #1 → actual dimension → 1.5" x 9.25" per table 1B
- * $C_d = C_m = C_t = 1.0$
- * $C_r = 1.15$

Based on the diagram above, find the following:

- What is the effective cantilever length l_e ?
- What is the slenderness ratio R_b for the cantilever?
- Given $C_c = 0.94$, what is F'_b for the cantilever? $F_{DE} = \frac{1.2(620000)}{1.579} = 2050$
- Find the demand-capacity ratio for cantilever bending, $D/C = f_b/F'_b$ $C_c = 0.94$ ✓
- Sketch the load pattern giving the highest value of M' for the back span.

a) $l_u = 5.6'$ for the cantilever

$$\frac{l_e}{d} = \frac{(5.6')(12)}{9.25} = 7.26 \geq 7$$

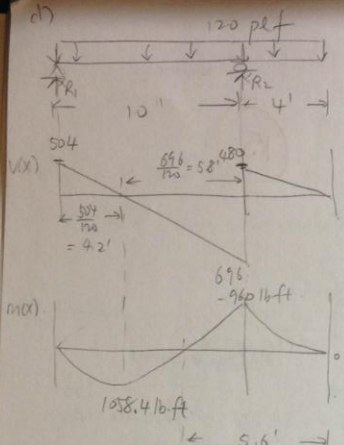
The cantilever is loaded uniformly across its span, thus

$$l_e = 0.9l_u + 3d = (0.9)(5.6') + (3)(9.25'')/12 = \boxed{7.3525'}$$

b) $R_b = \sqrt{\frac{l_e d}{b^2}} = \sqrt{\frac{(7.3525')(12)(9.25'')}{(1.5'')^2}} = \boxed{19.05} \leq 50 \text{ ok}$

⇒ parts d, e)

c) DF-L #1 from table 4A $F_b = 1000 \text{ psi}$
 $C_F = 1.1$, $C_r = 1.15$, $C_L = 0.94$ all other factors = 1.0
 $F'_b = (1000 \text{ psi})(1.1)(1.15)(0.94) = \boxed{1189 \text{ psi}}$



Reactions:

$$\sum F_y = 0$$

$$R_1 + R_2 = (120 \text{ plf})(14')$$

$$R_1 + R_2 = 1680 \text{ lb.}$$

$$\sum M_i = 0$$

$$\frac{Wl^2}{2} = (R_2)(10)$$

$$\frac{(120 \text{ plf})(14')^2}{2} = R_2(10)$$

$$R_2 = 1176 \text{ lb.}$$

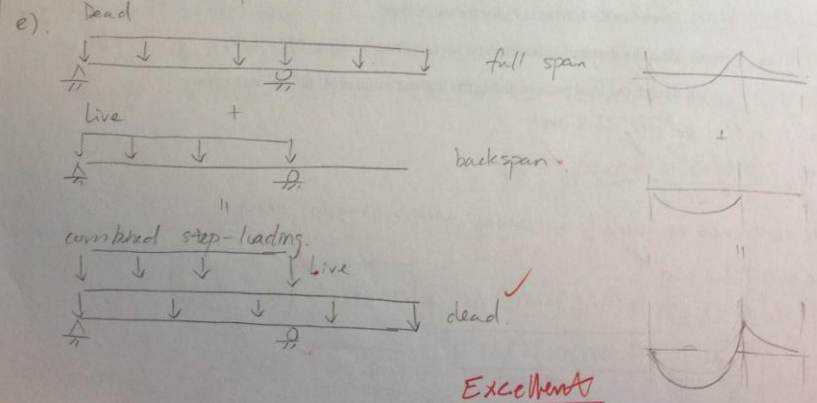
$$R_1 = 1680 - 1176 = 504 \text{ lb.}$$

Max REQ'D = only M asked for...

for cantilever we use $M_{max} = M^- = 960 \text{ lb. ft.}$, $S_x = 21.39 \text{ in}^3$ from table B.

$$f_b = \frac{(960 \text{ lb. ft})(12)}{21.39 \text{ in}^3} = 539 \text{ psi}$$

$$\frac{D}{c} = \frac{f_b}{F_b'} = \frac{539 \text{ psi}}{1189 \text{ psi}} = 0.45 \rightarrow \text{ok}$$



Excellent