CS 61A Structure and Interpretation of Computer Programs Fall 2014 MIDTERM 2

INSTRUCTIONS

- You have 2 hours to complete the exam.
- The exam is closed book, closed notes, closed computer, closed calculator, except one hand-written $8.5" \times 11"$ crib sheet of your own creation and the 2 official 61A midterm study guides attached to the back of this exam.
- Mark your answers ON THE EXAM ITSELF. If you are not sure of your answer you may wish to provide a *brief* explanation.

Last name	
First name	
SID	
Login	
TA & section time	
Name of the person to your left	
Name of the person to your right	
All the work on this exam is my own. (please sign)	

For staff use only							
Q. 1	Q. 2	Q. 3	Q. 4	Q. 5	Total		
/12	/14	/8	/8	/8	/50		

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1. (12 points) Class Hierarchy

For each row below, write the output displayed by the interactive Python interpreter when the expression is evaluated. Expressions are evaluated in order, and **expressions may affect later expressions**.

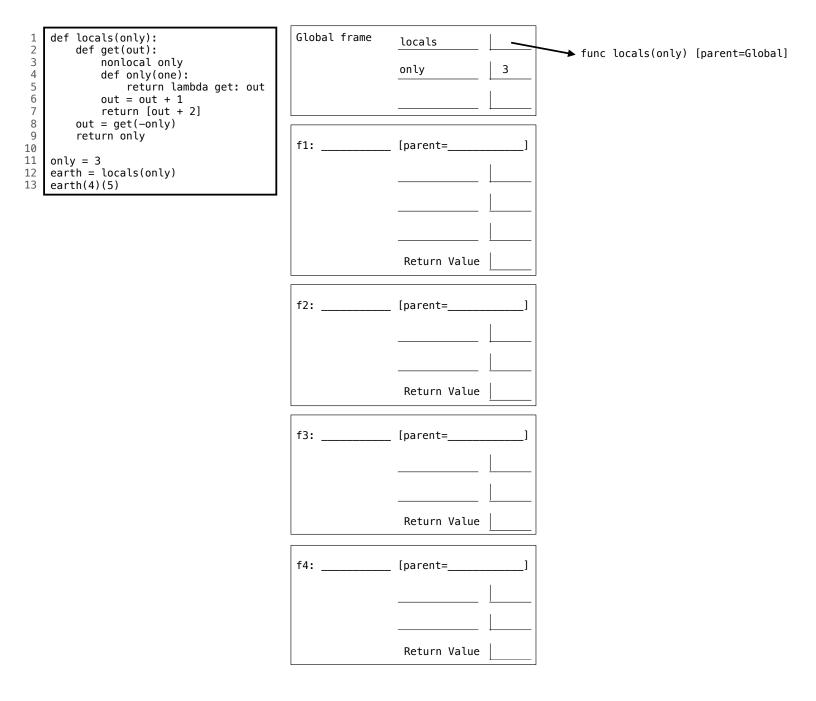
Whenever the interpreter would report an error, write ERROR. You *should* include any lines displayed before an error. *Reminder*: The interactive interpreter displays the **repr** string of the value of a successfully evaluated expression, unless it is **None**. Assume that you have started Python 3 and executed the following:

```
class Worker:
    greeting = 'Sir'
    def __init__(self):
        self.elf = Worker
    def work(self):
        return self.greeting + ', I work'
    def __repr__(self):
        return Bourgeoisie.greeting
class Bourgeoisie(Worker):
    greeting = 'Peon'
    def work(self):
        print(Worker.work(self))
        return 'My job is to gather wealth'
class Proletariat(Worker):
    greeting = 'Comrade'
    def work(self, other):
        other.greeting = self.greeting + ' ' + other.greeting
        other.work() # for revolution
        return other
jack = Worker()
john = Bourgeoisie()
jack.greeting = 'Maam'
```

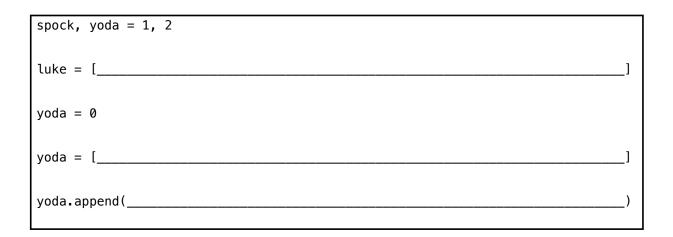
Expression	Interactive Output	Expression	Interactive Output
5*5	25		
1/0	Error		
Worker().work()		john.work()[10:]	
		Proletariat().work(john)	
jack			
		john.elf.work(john)	
jack.work()			

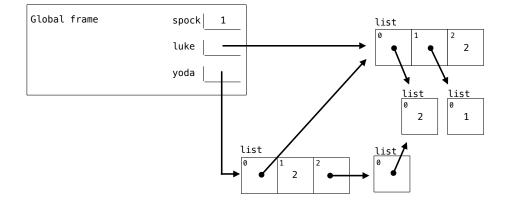
2. (14 points) Space

- (a) (8 pt) Fill in the environment diagram that results from executing the code below until the entire program is finished, an error occurs, or all frames are filled. You may not need to use all of the spaces or frames. A complete answer will:
 - Add all missing names and parent annotations to all local frames.
 - Add all missing values created during execution.
 - Show the return value for each local frame.



(b) (6 pt) Fill in the blanks with the shortest possible expressions that complete the code in a way that results in the environment diagram shown. You can use only brackets, commas, colons, and the names luke, spock, and yoda. You *cannot* use integer literals, such as 0, in your answer! You also cannot call any built-in functions or invoke any methods by name.





3. (8 points) This One Goes to Eleven

(a) (4 pt) Fill in the blanks of the implementation of sixty_ones below, a function that takes a Link instance representing a sequence of integers and returns the number of times that 6 and 1 appear consecutively.

```
def sixty_ones(s):
      """Return the number of times that 1 directly follows 6 in linked list s.
     >>> once = Link(4, Link(6, Link(1, Link(6, Link(0, Link(1)))))
     >>> twice = Link(1, Link(6, Link(1, once)))
     >>> thrice = Link(6, twice)
     >>> apply_to_all(sixty_ones, [Link.empty, once, twice, thrice])
     [0, 1, 2, 3]
      .....
     if _____:
         return 0
     elif _____:
         return 1 + _____:
     else:
         return _____
(b) (4 pt) Fill in the blanks of the implementation of no_eleven below, a function that returns a list of all
  distinct length-n lists of ones and sixes in which 1 and 1 do not appear consecutively.
  def no_eleven(n):
      """Return a list of lists of 1's and 6's that do not contain 1 after 1.
     >>> no_eleven(2)
```

- 4. (8 points) Tree Time
- (a) (4 pt) A GrootTree g is a binary tree that has an attribute parent. Its parent is the GrootTree in which g is a branch. If a GrootTree instance is not a branch of any other GrootTree instance, then its parent is BinaryTree.empty.

BinaryTree.empty should not have a parent attribute. Assume that every GrootTree instance is a branch of at most one other GrootTree instance and not a branch of any other kind of tree.

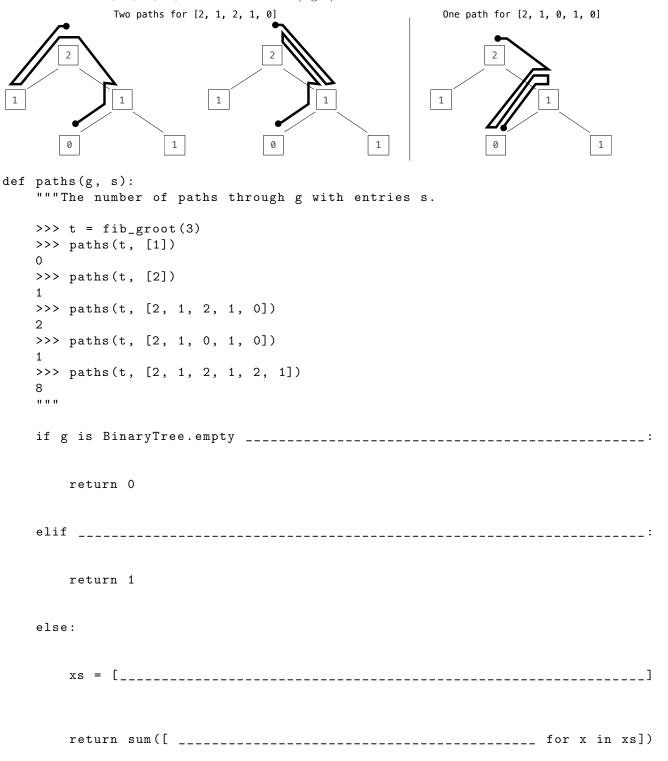
Fill in the blanks below so that the **parent** attribute is set correctly. You may not need to use all of the lines. Indentation is allowed. You *should not* include any **assert** statements. Using your solution, the doctests for **fib_groot** should pass. The **BinaryTree** class appears on your study guide.

Hint: A picture of fib_groot(3) appears on the next page.

```
class GrootTree(BinaryTree):
  """A binary tree with a parent."""
  def __init__(self, entry, left=BinaryTree.empty, right=BinaryTree.empty):
    BinaryTree.__init__(self, entry, left, right)
     _____
       _____
     _____
      _____
        _____
      _____
def fib_groot(n):
  """Return a Fibonacci GrootTree.
  >>> t = fib_groot(3)
  >>> t.entry
  2
  >>> t.parent.is_empty
  True
  >>> t.left.parent.entry
  2
  >>> t.right.left.parent.right.parent.entry
  1
  .....
  if n == 0 or n == 1:
    return GrootTree(n)
  else:
    left, right = fib_groot(n-2), fib_groot(n-1)
    return GrootTree(left.entry + right.entry, left, right)
```

(b) (4 pt) Fill in the blanks of the implementation of paths, a function that takes two arguments: a GrootTree instance g and a list s. It returns the number of paths through g whose entries are the elements of s. A path through a GrootTree can extend either to a branch or its parent.

You may assume that the GrootTree class is implemented correctly and that the list s is non-empty. The two paths that have entries [2, 1, 2, 1, 0] in fib_groot(3) are shown below (left). The one path that has entries [2, 1, 0, 1, 0] is shown below (right).



5. (8 points) Abstraction and Growth

def length(slinky):

(a) (6 pt) Your project partner has invented an abstract representation of a sequence called a slinky, which uses a transition function to compute each element from the previous element. A slinky explicitly stores only those elements that cannot be computed by calling transition, using a starts dictionary. Each entry in starts is a pair of an index key and an element value. See the doctests for examples. Help your partner fix this implementation by crossing out as many lines as possible, but leaving a program

that passes the doctests. Do not change the doctests. The program continues onto the following page.

```
return slinky[0]
def starts(slinky):
    return slinky[1]
def transition(slinky):
    return slinky[2]
def slinky(elements, transition):
    """Return a slinky containing elements.
    >>> t = slinky([2, 4, 10, 20, 40], lambda x: 2*x)
    >>> starts(t)
    \{0: 2, 2: 10\}
    >>> get(t, 3)
    20
    >>> r = slinky(range(3, 10), lambda x: x+1)
    >>> length(r)
    7
    >>> starts(r)
    \{0: 3\}
    >>> get(r, 2)
    5
    >>> slinky([], abs)
    [0, {}, <built-in function abs>]
    >>> slinky([5, 4, 3], abs)
    [3, {0: 5, 1: 4, 2: 3}, <built-in function abs>]
    .....
    starts = {}
    last = None
    for e in elements[1:]:
    for index in range(len(elements)):
        if not e:
        if index == 0:
            return [0, {}, transition]
        if last is None or e != transition(last):
        if e == 0 or e != transition(last):
        if index == 0 or elements[index] != transition(elements[index-1]):
            starts[index] = elements[index]
            starts[index] = elements.pop(index)
            starts[e] = transition(last)
            starts[e] = last
        last = e
    return [len(starts), starts, transition]
    return [len(elements), starts, transition]
    return [len(starts), elements, transition]
    return [len(elements), elements, transition]
```

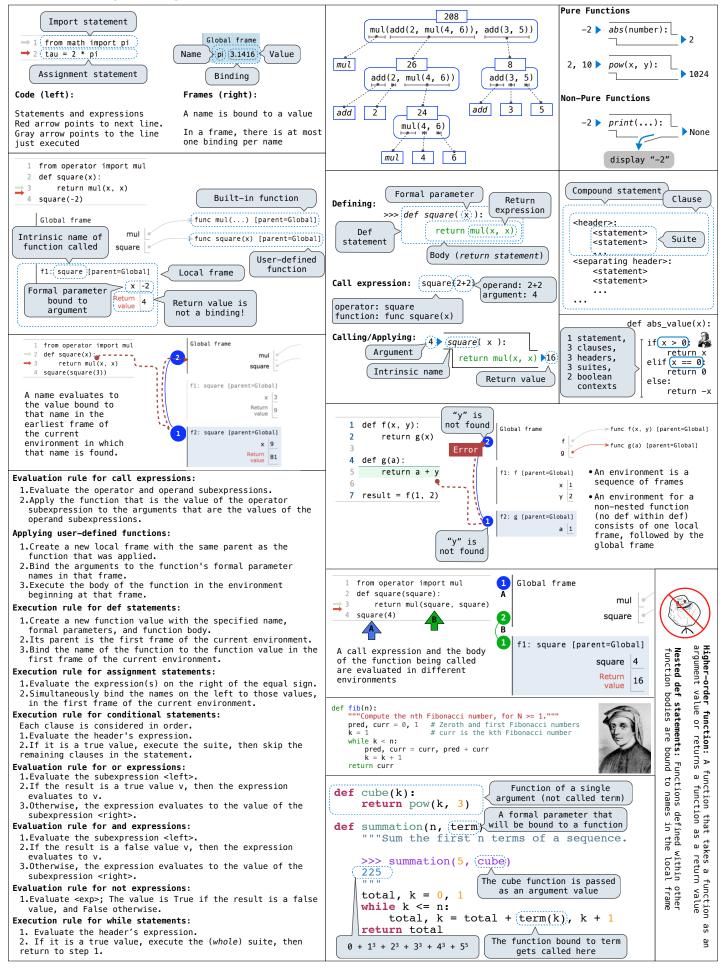
```
def get(slinky, index):
    """Return the element at index of slinky."""
    if index in starts(slinky):
        return starts(slinky)[index]
    start = index
    start = 0
   f = transition(slinky)
    while start not in starts(slinky):
    while not f(get(start)) == index:
        start = start + 1
        start = start - 1
   value = starts(slinky)[start]
   value = starts(slinky)[0]
    value = starts(slinky)[index]
    while start < index:
    while value < index:
        value = f(value)
        value = value + 1
        start = start + 1
        start = start + index
   return value
   return f(value)
```

- (b) (2 pt) Circle the Θ expression below that describes the number of operations required to compute slinky(elements, transition), assuming that
 - *n* is the initial length of elements,
 - *d* is the final length of the **starts** dictionary created,
 - the transition function requires constant time,
 - the pop method of a list requires constant time,
 - the len function applied to a list requires linear time,
 - the len function applied to a range requires constant time,
 - adding or updating an entry in a dictionary requires constant time,
 - getting an element from a list by its index requires constant time,
 - creating a list requires time that is proportional to the length of the list.

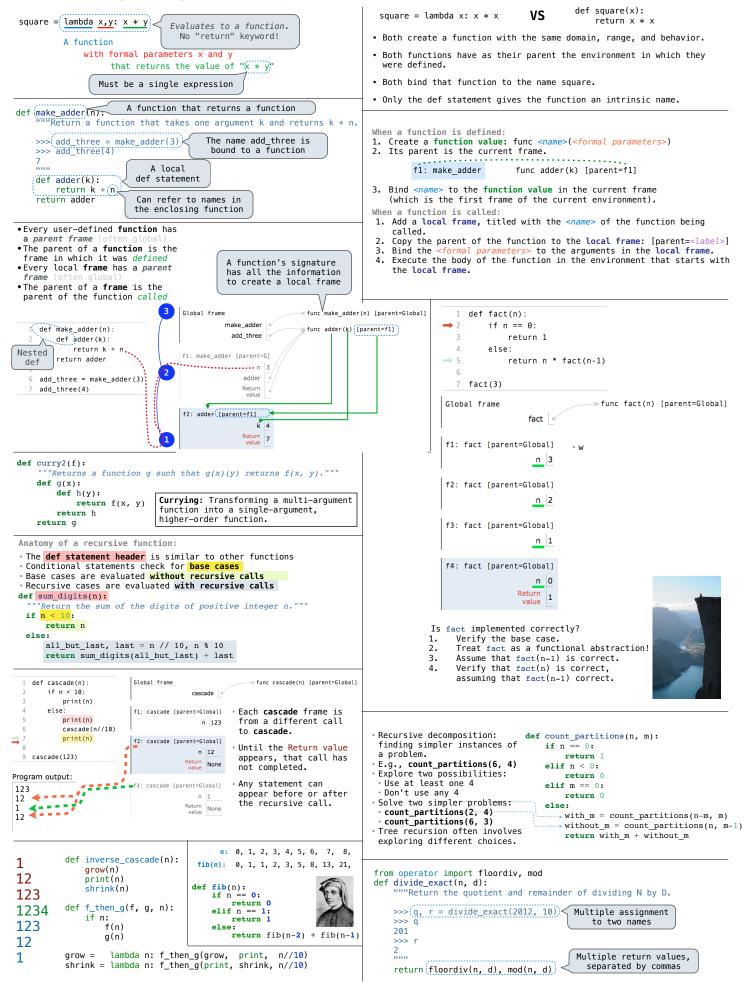
$$\Theta(1)$$
 $\Theta(n)$ $\Theta(d)$ $\Theta(n^2)$ $\Theta(d^2)$ $\Theta(n \cdot d)$

Scratch Paper

Scratch Paper



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True

Numeric types in Python: List comprehensions: [<map exp> for <name> in <iter exp> if <filter exp>] >>> type(2) Represents <class 'int'>integers Short version: [<map exp> for <name> in <iter exp>] exactlv >>> type(1.5) A combined expression that evaluates to a list using this <class 'float'> < evaluation procedure: Represents real 1. Add a new frame with the current frame as its parent numbers >>> type(1+1j) 2. Create an empty result list that is the value of the approximately <class 'complex'> expression 3. For each element in the iterable value of <iter exp>: Functional pair implementation: A. Bind <name> to that element in the new frame from step 1 B. If <filter exp> evaluates to a true value, then add def pair(x, y): the value of <map exp> to the result list """Return a functional pair.""" def apply_to_all(map_fn, s): def get(index): if index == 0: "Apply map_fn to each element of s. This function return x represents a >>> apply_to_all(lambda x: x*3, range(5)) elif index == 1: pair return y [0, 3, 6, 9, 12] return get return [map_fn(x) for x in s] Constructor is a def select(p, i): higher-order function def keep_if(filter_fn, s): "List elements x of s for which """Return element i of pair p.""" filter_fn(x) is true. return p(i) _ Selector defers to >>> keep_if(lambda x: x>5, range(10)) the object itself >>> p = pair(1, 2) [6, 7, 8, 9] >>> select(p, 0) return [x for x in s if filter_fn(x)] >>> select(p, 1) def reduce(reduce_fn, s, initial): 2 ""Combine elements of s pairwise using reduce_fn, Lists: starting with initial. 16,777,216 >>> digits = [1, 8, 2, 8] r = initial >>> len(digits) list pow 4 for x in s: digits ____ 0 1 2 3 $r = reduce_fn(r, x)$ >>> digits[3] 8 2 8 1 pow return r 8 >>> [2, 7] + digits * 2 reduce(pow, [1, 2, 3, 4], 2) pow [2, 7, 1, 8, 2, 8, 1, 8, 2, 8] >>> pairs = [[10, 20], [30, 40]] pow >>> pairs[1] list list pairs 0 1 [30, 40] 0 Type dispatching: Look up a cross-type implementation of an >>> pairs[1][0] 20 • 10 operation based on the types of its arguments Type coercion: Look up a function for converting one type to 30 list Executing a for statement: another, then apply a type-specific implementation. 1 0 for <name> in <expression>: $\Theta(b^n)$ Exponential growth. Recursive fib takes e are positive $| \ \mathbf{k_2} \ \mathrm{such} \ \mathrm{that} \ \mathbf{k_2} \ \mathrm{such} \ \mathrm{that} \ \mathbf{k_3} \ \mathrm{that} \ \mathbf{k_2} \ \mathrm{than} \ \mathrm{such} \ \mathbf{m}$. Then some \mathbf{m} 30 40 <suite> $\Theta(\phi^n)$ steps, where $\phi=\frac{1+\sqrt{5}}{2}\approx 1.61828$ Incrementing the problem scales R(n) 1. Evaluate the header <expression>, which must yield an iterable value (a sequence) by a factor 2. For each element in that sequence. $\Theta(n^2)$ Quadratic growth. E.g., overlap in order: at there is ki and k $\leq R(n) \leq n$ larger Incrementing n increases R(n) by the A. Bind <name> to that element in (f(n))the current frame problem size n B. Execute the <suite> $\Theta(n)$ Linear growth. E.g., factors or exp $\begin{array}{l} R(n) = \Theta(f) \\ means that \\ constants k \\ constants k \\ k_1 \cdot f(n) \\ \Theta(l) \\ \Theta(l$ Unpacking in a Logarithmic growth. E.g., exp_fast A sequence of for statement: fixed-length sequences Doubling the problem only increments R(n) $\Theta(1)$ Constant. The problem size doesn't matter >>> pairs=[[1, 2], [2, 2], [3, 2], [4, 4]] >>> same_count = 0 →func make withdraw(balance) [parent=Global] Global frame A name for each element in a fixed-length sequence make_withdraw >func withdraw(amount) [parent=f1] withdraw >>> for (x, y) in pairs: ... if x == y: >>> withdraw = make_withdraw(100) >>> withdraw(25) f1: make withdraw [parent=Global] same_count = same_count + 1 75 . . . balance 50 >>> withdraw(25) The parent withdraw 50 >>> same_count frame contains def make_withdraw(balance): 2 Return the balance of value def withdraw(amount): withdraw ..., -3, -2, -1, 0, 1, 2, 3, 4, ... nonlocal balance f2: withdraw [parent=f1] amount 25 Every call Return value 75 decreases the return balance range(-2, 2)same balance return withdraw Length: ending value - starting value f3: withdraw [parent=f1] Status Element selection: starting value + index amount 25 •No nonlocal statement •"x" is not bound locally Return value 50 >>> list(range(-2, 2)) { List constructor [-2, -1, 0, 1] •No nonlocal statement Strings as sequences: •"x" is bound locally >>> list(range(4)) { Range with a 0 >>> city = 'Berkeley' •nonlocal x starting value >>> len(city) [0, 1, 2, 3] •"x" is bound in a 8 non-local frame Membership: Slicing: >>> city[3] >>> digits[0:2] >>> digits = [1, 8, 2, 8] •nonlocal x 'k' >>> 2 in digits [1.8] •"x" is not bound in >>> 'here' in "Where's Waldo?" >>> digits[1:] True a non-local frame True [8, 2, 8] >>> 1828 not in digits •nonlocal x >>> 234 in [1, 2, 3, 4, 5]

Slicing creates

a new object

False

False

>>> [2, 3, 4] in [1, 2, 3, 4]

List & dictionary mutation: >>> a = [10] >>> a = [10] >>> b = a >>> b = [10] >>> a == b >>> a == b True True >>> a.append(20) >>> b.append(20) >>> a >>> a == b True [10] >>> a >>> b [10, 20] [10, 20] >>> h >>> a == b [10, 20] False >>> nums = { 'I': 1.0, 'V': 5, 'X': 10} >>> nums['X'] 10 0, 1, 2, 3, 4 >>> nums['I'] = 1 >>> nums['L'] = 50 >>> nums {'X': 10, 'L': 50, 'V': 5, 'I': 1} >>> sum(nums.values()) 0, 3, 6, 9, 12 66 >>> dict([(3, 9), (4, 16), (5, 25)])
{3: 9, 4: 16, 5: 25} 0, 1, 2, 3, 4, 5, 6, 7, 8, 9 >>> nums.get('A', 0) 0 >>> nums.get('V'. 0) λx: x>5 >>> {x: x*x for x in range(3,6)} {3: 9, 4: 16, 5: 25} 6, 7, 8, 9 >>> suits = ['coin', 'string', 'myriad'] >>> original_suits = suits >>> suits.pop() 'mvriad' >>> suits.remove('string') >>> suits.append('cup') >>> suits.extend(['sword', 'club']) 4 >>> suits[2] = 'spade' >>> suits
['coin', 'cup', 'spade', 'club']
>>> suits[0:2] = ['heart', 'diamond'] >>> suits
['heart', 'diamond', 'spade', 'club'] >>> original_suits ['heart', 'diamond', 'spade', 'club'] Identity: <exp0> is <exp1> evaluates to True if both <exp0> and <exp1> evaluate to the same object Equality: <exp0> == <exp1> evaluates to True if both <exp0> and <exp1> evaluate to equal values Identical objects are always equal values You can copy a list by calling the list constructor or slicing the list from the beginning to the end. Constants: Constant terms do not affect the order of growth of a process not affect the order of growth of a process $\Theta(\log_2 n) = \Theta(\log_{10} n)$ $\Theta(\ln n)$ Nesting: When an inner process is repeated for each step in an outer process, multiply the steps in the outer and inner processes to find the total number of steps def overlap(a, b): count = 0 Outer: length of a for item in a: ---if item in b: count += 1 Inner: length of b return count If a and b are both length \mathbf{n} , then overlap takes $\Theta(n^2)$ steps if amount > balance:
 return 'No funds Lower-order terms: The fastest-growing part of the computation dominates the total balance = balance - amount $\Theta(n^2) \quad \Theta(n^2 + n) \quad \Theta(n^2 + 500 \cdot n + \log_2 n + 1000)$ Effect Create a new binding from name "x" to number 2 in the first frame of the current environment Re-bind name "x" to object 2 in the first frame of the current environment Re-bind "x" to 2 in the first non-local frame of the current environment in which "x" is bound SyntaxError: no binding for nonlocal 'x' found

λx: x*3

3

x = 2

•"x" is bound in a

•"x" also bound locally

non-local frame

2

64

4

2

2 1

SyntaxError: name 'x' is parameter and nonlocal

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