

1. Evaluate the integral $\int_{-1}^1 \int_0^{\sqrt{1-x^2}} \sqrt{1-y^2} dy dx.$

[6]

(You can do it without reversing the order of integration, but it's not recommended.)

2. The integral below computes the area of a region. Sketch the area, and compute it by converting to polar coordinates.

[6]

$$\int_{-2}^{-1} \int_{-x}^{\sqrt{8-x^2}} dy dx + \int_{-1}^1 \int_{\sqrt{2-x^2}}^{\sqrt{8-x^2}} dy dx + \int_1^2 \int_x^{\sqrt{8-x^2}} dy dx$$

3. Evaluate the integral $\int_0^2 \int_0^{\sqrt{2x-x^2}} \sqrt{x^2+y^2} dy dx$ by converting to polar coordinates. [6]

4. Find the centroid (geometric center) of the triangle with vertices $(0,0)$, $(-4,-2)$, and $(4,2)$. [8]

5. Set up, but do not evaluate, the integral $\iiint_E x^2 \cos(yz) dV$, where E is the tetrahedron with vertices $(2, 0, 0)$, $(0, 4, 0)$, and $(0, 0, 1)$. $(0, 0, 0)$ [6]

6. Let $E \subseteq \mathbb{R}^3$ be the region bounded below by the cone $z = \sqrt{x^2 + y^2}$ and above by the sphere $x^2 + y^2 + z^2 = 2z$. Express the volume of E as a triple integral in **both** cylindrical and spherical coordinates. You do not have to compute the volume. [6]