# CS 61A Structure and Interpretation of Computer Programs Fall 2012 MIDTERM 1

## INSTRUCTIONS

- You have 2 hours to complete the exam.
- The exam is closed book, closed notes, closed computer, closed calculator, except one hand-written  $8.5" \times 11"$  crib sheet of your own creation and the official 61A midterm 1 study guide attached to the back of this exam.
- Mark your answers ON THE EXAM ITSELF. If you are not sure of your answer you may wish to provide a *brief* explanation.

Last name	
First name	
SID	
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TA & section time	
Name of the person to	
your left	
Name of the person to	
your right	
All the work on this exam	
is my own. (please sign)	
1	

For staff use only						
Q. 1	Q. 2	Q. 3	Q. 4	Total		
/12	/12	/14	/12	/50		

1. (12 points) The Call Express is Delayed

For each of the following call expressions, write the value to which it evaluates *and* what would be output by the interactive Python interpreter. The first two rows have been provided as examples.

- In the **Evaluates to** column, write the value to which the expression evaluates. If evaluation causes an error, write ERROR.
- In the column labeled **Interactive Output**, write all output that would be displayed during an interactive session, after entering each call expression. This output may have multiple lines. Whenever the interpreter would report an error, write ERROR. You *should* include any lines displayed before an error.

Assume that you have started Python 3 and executed the following statements:

```
from operator import add, mul
def square(x):
    return mul(x, x)

def delay(arg):
    print('delayed')
    def g():
        return arg
    return g
```

Expression	Evaluates to	Interactive Output
square(5)	25	25
1/0	Error	Error
<pre>print(square(4))</pre>		
<pre>square(square(print(2)))</pre>		
<pre>print(add(3, 4), print(5))</pre>		
delay(square)(3)		
<pre>add(delay(square)()(2), 1)</pre>		
delay(delay)()(6)()		

## 2. (12 points) Protect the Environment

- (a) (6 pt) Fill in the environment diagram that results from executing the code below until the entire program is finished, an error occurs, or all frames are filled. You may not need to use all of the spaces or frames. A complete answer will:
  - Add all missing names, labels, and parent annotations to all local frames.
  - Add all missing values created during execution.
  - Show the return value for each local frame.



- (b) (6 pt) Fill in the environment diagram that results from executing the code below until the entire program is finished, an error occurs, or all frames are filled. You may not need to use all of the spaces or frames. A complete answer will:
  - Add all missing names, labels, and parent annotations to all local frames.
  - Add all missing values created during execution.
  - Show the return value for each local frame.



#### 3. (14 points) Sequences

(a) (2 pt) Fill in the blanks so that the final call expression below evaluates to a tuple value.

```
def pair(x):
    if x == 30:
        return lambda: (1, 2, 3)
    else:
        return lambda: 4
```

(lambda\_\_\_\_\_)(pair, "sequence")

(b) (2 pt) Draw a box and pointer diagram for the following rlist:

a = rlist(1, rlist(rlist(2, (3, empty\_rlist)), rlist((4, 5, 6), empty\_rlist)))

(c) (2 pt) What is the element at index 1 of this rlist, returned by getitem\_rlist(a, 1)?

```
def getitem_rlist(s, i):
    """Return the element at index i of recursive list s."""
    while i > 0:
        s, i = rest(s), i - 1
    return first(s)
```

(d) (2 pt) What is the length of this rlist, returned by len\_rlist(a)?

```
def len_rlist(s):
    """Return the length of recursive list s."""
    length = 0
    while s != empty_rlist:
        s, length = rest(s), length + 1
    return length
```

(e) (6 pt) When the int constructor is called on a float value, it "truncates toward zero," meaning that it returns the largest integer less than any positive argument, or the least integer greater than any negative argument. For example:

```
>>> int(2)
2
>>> int(2.7)
2
>>> int(-1.5)
-1
```

Assume that you have started Python 3 and executed the following statements:

```
def alt(f, g, z):
    while g(z) > 0 and z != 5:
        f, g = g, f
        z = g(z)
    return z
def grow(x):
    return int((x * 3) / 2)
def shrink(x):
    return x - 2
def flip(x):
    return int(10 / (x-2))
```

For each of the following call expressions, write the value to which it evaluates. If evaluation causes an error, write ERROR. If evaluation would run forever, write FOREVER.

```
• alt(grow, shrink, 3)
```

• alt(grow, shrink, 4)

• alt(flip, shrink, 3)

### 4. (12 points) In Verse

The inverse of some function $F$	There once was a rhyming device
is a function of argument $X$	That was built to make any sound, twice,
that returns you the Y,	But used orthography
such that when you apply	And not phonology
F to $Y$ you recover the $X$ .	To decide if a rhyme would suffice.

An invertible function is a function that takes and returns a single numeric value, is differentiable, and never returns the same value for two different arguments. Some examples:

```
def double(y):
    """Return twice the value of y."""
    return 2 * y

def cube(y):
    """Return y raised to the third power."""
    return pow(y, 3)

def pow2(y):
    """Return 2 raised to the power of y."""
    return pow(2, y)
```

(a) (4 pt) Implement a function invert that takes an invertible function argument and returns its inverse. You may call find\_root, newton\_update, approx\_deriv, and/or iter\_improve. You cannot use any assignment, conditional, while, or for statements.

```
def invert(f):
    """Return the inverse of invertible function f.
    >>> halve = invert(double)
    >>> halve(12)
    6.0
    >>> cube_root = invert(cube)
    >>> cube_root(27)
    3.0
    >>> log2 = invert(pow2)
    >>> log2(32)
    5.0
    """
```

A sight rhyme is a pair of words that do not rhyme, but have the same endings, such as *device* and *office*. Two numbers that end in the same digit can be sight rhymes. For example:

- (13, 53) are pronounced *thirteen* and *fifty-three*, despite both ending with the same one's digit 3.
- (0, 30) are pronounced zero and thirty, despite both ending with the same one's digit 0.
- (b) (4 pt) A numpair is a pair of integers that have the same one's digit. Fill in the two missing expressions in the constructor below, which takes two non-negative integers less than 100, asserts that they have the same one's digit, and returns a numpair represented as a pair of tens digits and the shared one's digit.

```
from operator import floordiv, mod \# Use these functions or // and \%
```

```
def numpair(first, second):
    """Return a numpair as a pair of ten's digits and a shared one's digit.
    >>> numpair(23, 53)
    ((2, 5), 3)
    >>> numpair(67, 7)
    ((6, 0), 7)
    """
    assert _____, "different one's"
    return
```

(c) (4 pt) Fill in four missing expressions below so that sight\_rhyme returns whether the numbers in a numpair p do not end with the same sound when *pronounced*. Your implementation cannot depend on the *representation* of a numpair; use selector functions. You cannot use the boolean operators and or or.

```
def ones(p):
  return p[1]
def first_tens(p):
  return p[0][0]
def second_tens(p):
  return p[0][1]
def sight_rhyme(p):
   """Return whether the two numbers in a numpair do not rhyme.
  >>> sight_rhyme(numpair(13, 53))
  True
  >>> sight_rhyme(numpair(0, 30))
  True
  >>> sight_rhyme(numpair(53, 23))
  False
  ......
  if
    :-----:
     return _____
  elif ones(p) == 0:
     if first_tens(p) == 0:
        return _____
     else:
        return _____
  else:
     return False
```



