

EE42/100 Midterm 2

NO CALCULATORS, CELL PHONES, or other electronics allowed. Show your work, and put final answers in the boxes provided. Use proper units in all answers.

1:51

1. [5] Express the following power ratios in dB

P/Pref	P/Pref [dB]
20	13
50	17
$2 \times 10^{-10}$	-97
1/4	-6
$2.5 \times 10^8$	74

1 pt, no partial credit  
no units necessary (dB on top)  
no credit for answers that include log of anything.

2. [5] Express the following voltage ratios in dB

V/Vref	V/Vref [dB]
Sqrt(2)	3
1/2	-6
0.04	-28
1	0
$2 \times 10^{-3}$	-24

$2^2 \cdot 10^{-2} \Rightarrow 2.6 \approx 2.20$

3. [8] You measure an AC voltage across a  $1k\Omega$  resistor. The digital voltmeter that you use measures in RMS (like all voltmeters), and reports that the voltage is 1V. *use units*

a. What is the zero-to-peak voltage?

$V = \sqrt{2} \cdot 1V = 1.4$   
~~0.707~~

$\sqrt{2}$  OK

$V_{0-p} = 1.4V$

b. What is the peak-to-peak voltage

$V_{p-p} = 2.8V$

c. What is the max power dissipated in the resistor?

$\frac{(1.4)^2}{1k} = \frac{2V^2}{1k}$

$P_{max} = 2mW$

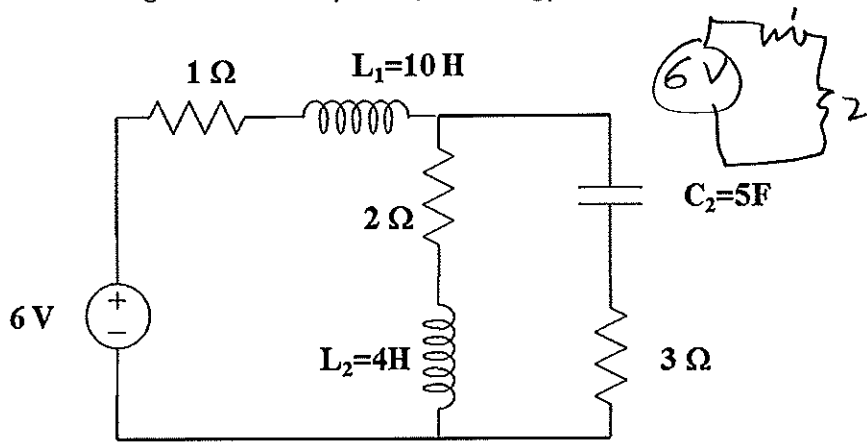
d. What is the average power dissipated in the resistor?

$P_{avg} = 1mW$

-1 1 missing unit  
-2 all missing units

-1 right formula, wrong calc

4. [10] For the circuit below, calculate the steady state values for the current in the two inductors, the voltage across the capacitor, the energy stored in  $L_1$ , and the energy stored in  $C_2$ .



$I_{L1}$	2 A
$I_{L2}$	2 A
$V_{C2}$	4 V
$W_{L1}$	20 J
$W_{C2}$	40 J

OK if consistent w/ wrong answer above

$$\frac{1}{2} L_1 i_1^2 = \frac{1}{2} (10 \text{ H}) (2 \text{ A})^2 = 20$$

$$\frac{1}{2} C V^2 = \frac{1}{2} (5) (4^2) = 40$$

5. [10] Two capacitors, each  $2\mu\text{F}$ , are charged in parallel from a single AA battery with a voltage of 1.5V, and then discharged in series into a  $1\text{k}\Omega$  load. The battery has a source resistance of  $1\Omega$ .

a. What is the equivalent capacitance seen by the battery during charging?

$$C_{\text{charge}} = 4 \mu\text{F}$$

b. What is the time constant during charging?

$$\tau_{\text{charge}} = 4 \mu\text{s}$$

c. What is the equivalent capacitance of the series combination driving the load?

$$C_{\text{series}} = 1 \mu\text{F}$$

d. What is the time constant during discharging?

$$\tau_{\text{discharge}} = 1 \text{ ms}$$

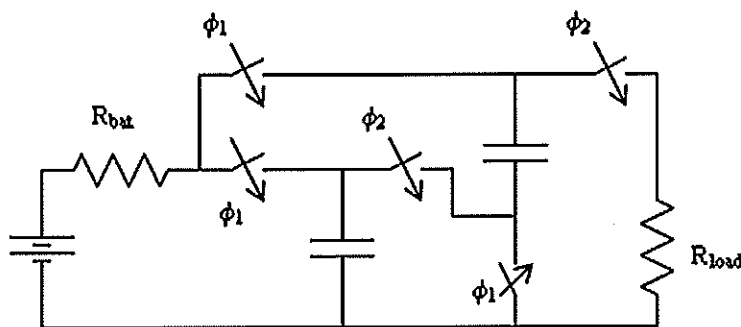
e. How long does it take for the output voltage to droop 5% after the  $\phi_2$  switches are closed?

$$(5\%) (1 \text{ ms}) =$$

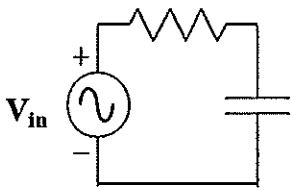
$$t_{5\%} = 50 \mu\text{s}$$

also accepts  $70.0011 \ln(0.95)$

-1 right formula wrong calc

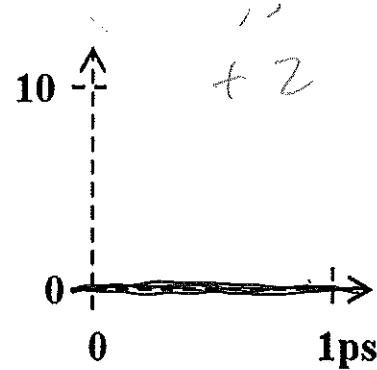
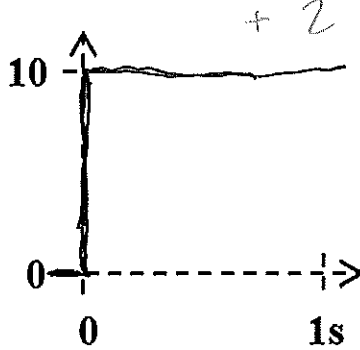
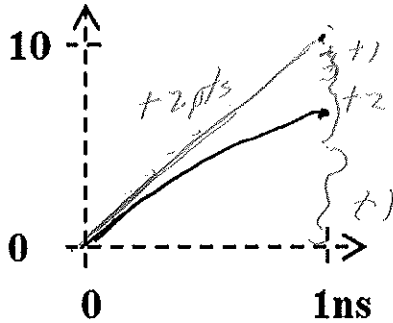


1:58 6. [10] In the RC circuit below assume  $V_{in}$  is a voltage step from 0 to 10V at  $t=0$ . If  $R=1$  and  $C=1nF$ , sketch the response of the circuit on the three different time scales provided.



$\tau = RC = 10^{-9} s$

$H(s) = \frac{1}{1 + j\omega/\omega_p}$   $\omega_p = 10^9 \text{ rad/sec.}$



+4 total

7. [8] The RC circuit above is driven by an input signal  $v_{in}(t) = \sin(100t) + \cos(10^9t)$ . What is  $V_{out}(t)$  in steady state?

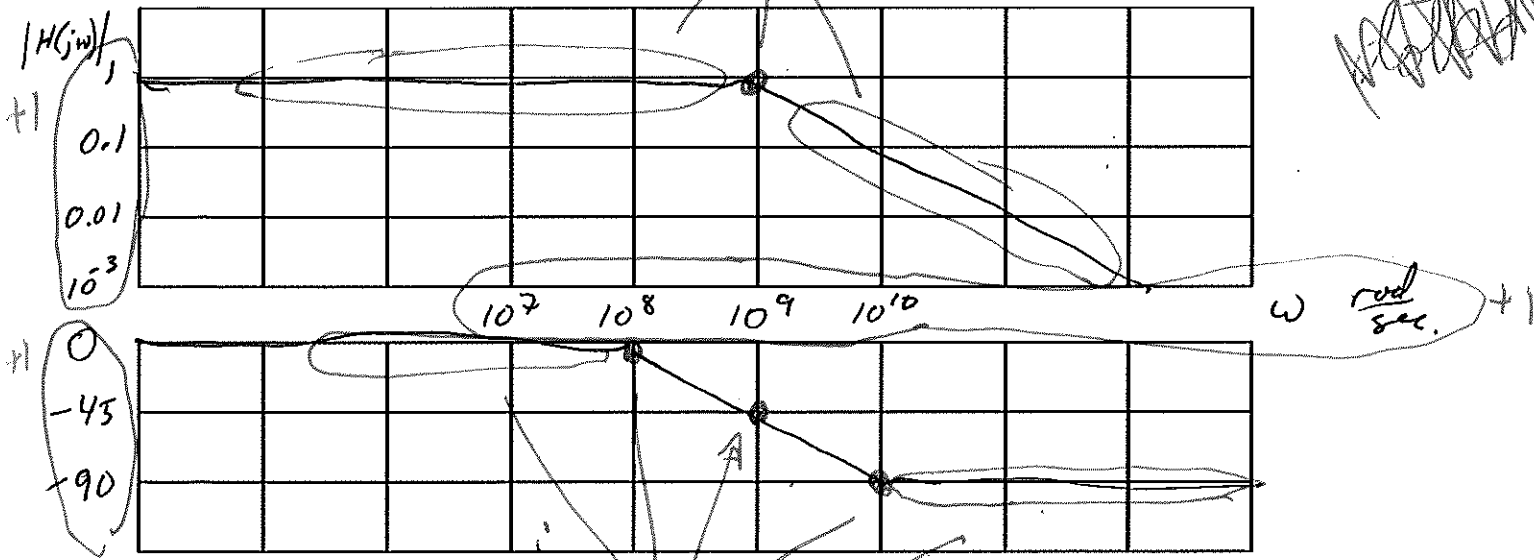
$V_{out}(t) = \sin(100t) + \frac{1}{\sqrt{2}} \cos(10^9t - 45^\circ)$

Annotations:  $\sin(100t)$  has '2 pts each' and '0V' below it.  $\cos(10^9t - 45^\circ)$  has '1 each' below it.

dB OK

8. [8] Sketch a Bode plot of the transfer function of the RC circuit above. Label each axis!

- 2 pts total max



- 1 wrong pole freq

1 pt off for missing any of these (-3 max)

$L = 10^{-4}$      $10^7 = \frac{1}{\sqrt{10^{-4}C}}$      $10^{14} = \frac{1}{10^{-4}C}$      $C = 10^{-10}$

9. [18 total] You want to build an AM radio with an LC tank at a resonant frequency of  $10^7$  rad/sec. Your inductor is 100uH and has a series resistance of  $20\Omega$ .

a. [2] How big should your capacitor be?

$C = 100\text{pF}$

b. [6] Sketch the magnitude of the inductor impedance (including series resistor) and capacitor impedance on the axes below. Label each axis!

c. [2] Assuming an ideal capacitor, what will the Q of your LC tank be?

$\frac{\omega_p L}{R} = \frac{10^7 \cdot 10^{-4}}{20} = \frac{1000}{20} = 50$

$Q = 50$

d. [2] What is the magnitude of the tank impedance at 1 rad/sec?

$Z(j1) = 20$

e. [2] What is the magnitude of the tank impedance at  $10^6$  rad/sec?

$Z(j10^6) = 100$

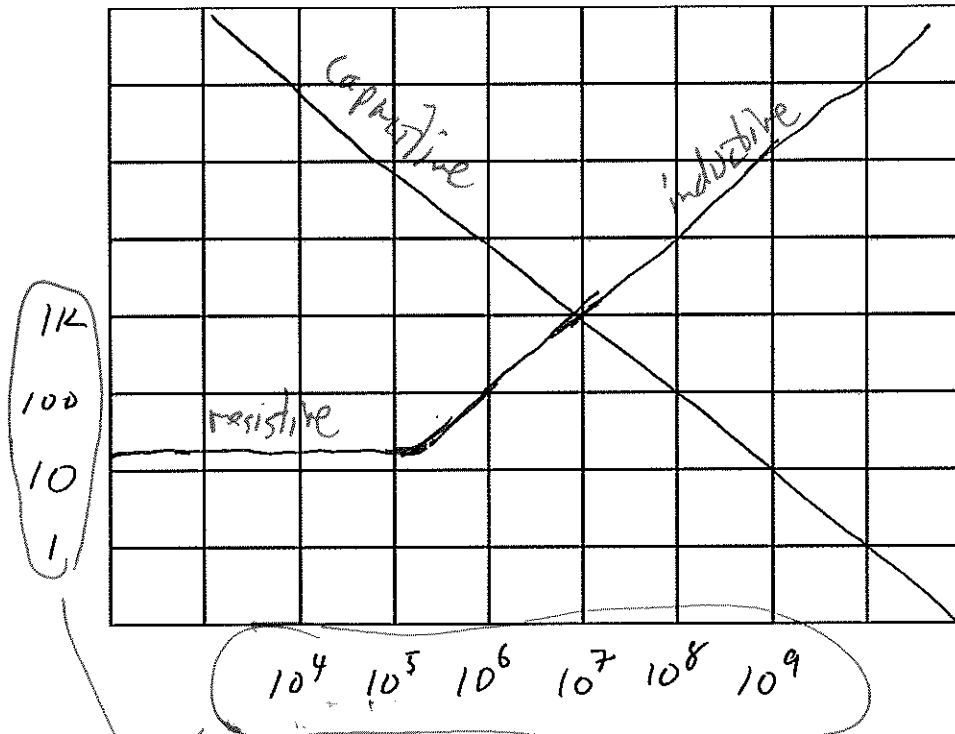
f. [2] What is the magnitude of the tank impedance at the resonant frequency?

$Q \omega_p L$

$Z(j\omega_p) = 50K$

g. [2] What is the magnitude of the tank impedance at  $10^9$  rad/sec?

$Z(j10^9) = 10$



-1 total if either or both are missing  
 2 pts each for Resistive/inductive, capacitive pts { 1 pt shape, 1 pt correct value.

# Rubric:

only punished once on the problem for wrong units.

- (a) wrong units (-1)  
no units: ok.

Wrong L value (-1)

- Off by OOM but wrote formula (-1)  
(wrong, no work (-2)).

(b) missing axis (one or both) (-1)

• 1 pt. each for crossings

• 1 pt. each for shape

• only swiggle 1/2 credit

- (-1) additionally if resistor and inductor not added correctly.

- (c) two formulas for Q (wrong answer)

(-1)

- (-1) no axes labels.

- No simplification (-1)

→

- 120  $\Omega$
- (e) → correct answer

- (f) 20  $\Omega$  instead of 10  $\Omega$  (-2) (didn't use C value → used R instead).

full credit.

find this paper.

- (g) did not multiply by Q (-1)

- 120  $\Omega$  versus 100  $\Omega$
- read off correctly from their graph: no punishment, ok.
- propagated wrong L value. ok. no punishment.

◦ inverted Q (-1)

◦ just expression left but evaluates to correct answer (-1)

◦ symbolic expression (-2)

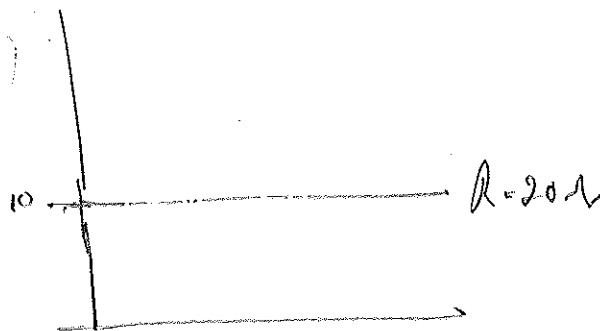
◦ C is right

graph is wrong

(-2)

answer is wrong, but taken from graph

◦ add Q instead of multiply by Q.



(-1)