

ME 106 FLUID MECHANICS

EXAM 1 – open class notes and bspace notes, no external communication

1. **(20+5=25%)** The Pitot-static tube of an A380 jumbo jet flying at 13 km altitude, its stated service ceiling, in standard atmosphere is reading a pressure differential of 1.0×10^4 Pa. You may consult the table in your class notes for atmospheric data.

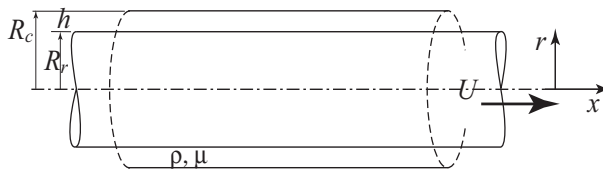
- (a) Determine the speed of the aircraft.
- (b) Determine the Mach number of the aircraft.

2.(20+5=25%) Construct and sketch the streamline equation for the flow field given in cylindrical coordinates

$$\mathbf{u} = (u_r, u_\theta) = \left(\cos \theta, \frac{1}{r} - \sin \theta \right)$$

Hint: remember the chain rule; $d(fg) = g df + f dg$

3. (25%) Determine the force per unit length required to pull at velocity U a rod of radius R_r out of a cylinder of inner radius R_c filled with an oil of viscosity μ . The rod and the cylinder are concentric. The gap between them $h = (R_c - R_r)$ is much smaller than their diameters, $h/R_c < h/R_r \ll 1$ so that you may wish to use planar flow approximation. Of course, you are always welcome to use the exact solution developed in class, but at your own peril!



4. (10+10+5=25%)

Consider the flow fluid of viscosity μ between two parallel infinite plates which are h apart. The top plate is moving to the right at constant velocity of U in its plane and the bottom plate is fixed. There is a constant negative pressure gradient of $dp/dx < 0$ acting on the fluid in the gap. Determine the value of $P = dp/dx$ for which the shear stress on the top plate vanishes.

Hint: Write the force balance for an infinitesimal fluid strip and apply the boundary conditions as you go along when integrating.

