

1. (60 points)

The gas turbine system shown schematically above functions like a steady-flow standard Brayton cycle except that a damaged flow conduit between the compressor and heater results in a throttling restriction (with no heat or work interaction) that causes the pressure to drop from 2 to 3 by 100 kPa. Information about the states during actual system operation is shown in the diagram above. The air-flow rate is 8.5 kg/s. The compressor efficiency is 0.82. In analyzing this system, assume the compressor and turbine are adiabatic, and treat the working fluid, air, as a ideal gas with constant specific heats:  $c_p = 1.005 \text{ kJ/kgK}$ ,  $c_v = 0.718 \text{ kJ/kgK}$ .

- Plot the state points and processes on a  $T$ - $s$  diagram, showing appropriate constant pressure lines.
- Determine the power input to the compressor and the actual exit temperature from the compressor,  $T_2$ .
- Determine  $T_3$ .
- Determine the rate of heat input to the heater.
- Determine the net power output of the system and the cycle efficiency.

(b)  $1 \rightarrow 2s$  isentropic  $\Rightarrow T_{2s} = T_1 \left( \frac{P_2}{P_1} \right)^{(k-1)/k}$        $k = c_p/c_v = 1.005/0.718 = 1.400$   
 $(k-1)/k = .400/1.400 = 0.286$   
 $T_{2s} = (27+273) \left( \frac{900}{100} \right)^{.286} = 562 \text{ K}$   
 $\dot{W}_{c,s} = +\dot{m}c_p(T_{2s} - T_1) = +(8.5)(1.005)(562 - 300) = +2238 \text{ kW}$   
 $\dot{W}_c = \dot{W}_{c,s}/\eta_c = -2238/0.82 = +2729 \text{ kW}$   
 $\dot{W}_c = -\dot{m}c_p(T_2 - T_1) \rightarrow T_2 = \frac{-\dot{W}_c}{\dot{m}c_p} + T_1 = \frac{2729}{8.5(1.005)} + 27 = 347 \text{ °C}$   
 $T_2 = 347 + 273 = 620 \text{ K}$

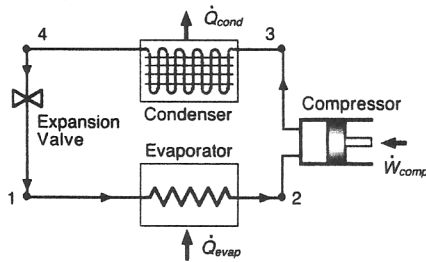
(c) CV around throttling restriction  $\Rightarrow \dot{Q} + \dot{m}h_2 = \dot{m}h_3 \Rightarrow h_3 = h_2$   
 Since ideal gas  $\Rightarrow h = u(T) \Rightarrow T_3 = T_2 = 347 \text{ °C} = 620 \text{ K}$

(d) CV around heater  $\Rightarrow \dot{Q}_{in} + \dot{m}h_3 = \dot{m}h_4 \Rightarrow \dot{Q}_{in} = \dot{m}(h_4 - h_3)$   
 $\Rightarrow \dot{Q}_{in} = \dot{m}c_p(T_4 - T_3) = (8.5)(1.005)(727 - 347) = 3246 \text{ kW}$

(e)  $\dot{W}_t = \dot{m}c_p(T_4 - T_5) = 8.5(1.005)(727 - 330) = 3391 \text{ kW}$

$\dot{W}_{net} = \dot{W}_t + \dot{W}_c = 3391 - 2729 = 662 \text{ kW}$

cycle efficiency  $= \eta_{cycle} = \frac{\dot{W}_{net}}{\dot{Q}_{in}} = \frac{662}{3246} = 0.204 = 20.4 \%$



2. (40 points)

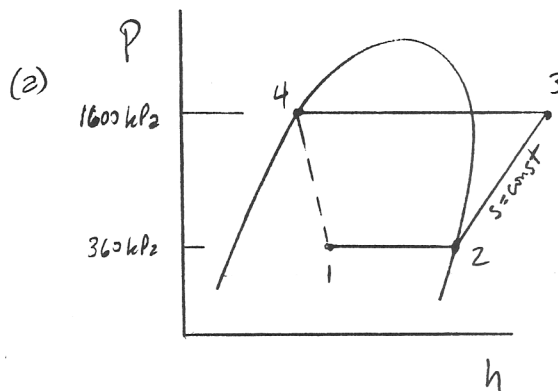
The vapor compression refrigeration system shown schematically above uses R-134a as its working fluid. The mass flow rate of R-134a in the system is 0.031 kg/s. The pressure at states 3 and 4 is 1600 kPa. State 4 is saturated liquid. The pressure at states 1 and 2 is 360 kPa. State 2 is saturated vapor. The following R-134a data is available for your analysis:

The specific entropy of saturated vapor at 360 kPa is 0.92836 kJ/kgK.

For superheated vapor at  $P = 1600$  kPa and  $s = 0.92836$  kJ/kgK, the specific enthalpy is 284.76 kJ/kg.

In this cycle, because the piping is not insulated, the process from 4 to 1 is *not* adiabatic. From 4 to 1, heat is input at a rate of 0.8 kW. In your analysis, assume the compressor is reversible and adiabatic.

- Show the cycle on a  $P$ - $h$  diagram.
- At both 360 kPa and 1600 kPa determine the saturated liquid and vapor specific enthalpies ( $h_f$  and  $h_g$ )
- Determine the rate of heat absorption in the evaporator.
- Determine the cycle COP.



(b)

from saturation table

@ 360 kPa

$$h_f = 59.72 \text{ kJ/kg}$$

$$h_g = h_2 = 253.81 \text{ kJ/kg}$$

@ 1600 kPa

$$h_f = h_4 = 135.93 \text{ kJ/kg}$$

$$h_g = 277.86 \text{ kJ/kg}$$

(c) CV around expansion valve  $\rightarrow \dot{Q} + \dot{m} h_4 = \dot{m} h_1$

$$\Rightarrow h_1 = h_4 + \frac{\dot{Q}}{\dot{m}} = 135.93 + \frac{0.8}{0.031} = 161.73 \text{ kJ/kg}$$

CV around evaporator  $\rightarrow \dot{Q}_{\text{evap}} + \dot{m} h_1 = \dot{m} h_2$

$$\Rightarrow \dot{Q}_{\text{evap}} = \dot{m} (h_2 - h_1) = 0.031 (253.81 - 161.73) = \underline{2.85 \text{ kW}}$$

(d) CV around compressor  $\rightarrow$  rev & adiab  $\Rightarrow s_3 = s_2$

$$-\dot{W}_c = \dot{m} (h_3 - h_2) \Rightarrow \dot{W}_c = -0.031 (284.76 - 253.81)$$

$$\dot{W}_c = -0.959 \text{ kW}$$

$$\text{COP} = \dot{Q}_{\text{evap}} / |\dot{W}_c| = 2.85 / 0.959 = \underline{2.97}$$