

Problem 1

a) **(smaller)**

According to the bull whip effect, small changes in demand are exaggerated going up the supply chain. The order information is passed from the retailer to the factory along the supply chain, so the demand variation at the factory is greater than that at the retailer.

b) **(EOQ)(EMQ)...(total costs)**

EOQ /EMQ models are used to minimize the overall costs, including ordering/setup costs and inventory holding costs.

c) **(sometimes)...(>=)**

We increase the batch size of the i^{th} product in order that the external setup of the $\{i+1\}^{\text{th}}$ product can be finished when processing one batch of i^{th} product. But this does not necessarily give the minimal batch size which can meet the demand, as seen from the homework.

Problem 3

$$Y(n) = Kn^{-a}$$

$$K = Y(1) = 10$$

$$2^{-a} = Y(2n)/Y(n) = Y(2)/Y(1) = Y(4)/Y(2) = 0.8 \Rightarrow a = -\log_2 0.8 = 0.3219$$

$$Y(6) = K(6)^{-a} = 10(6)^{-0.3219} = 5.62 \text{ hrs}$$

Problem 4

n	D_n	S_{n-1}
1	2500	$=(2500+2600+2800+2400)/4=2575$
2	2600	$=(0.1)(2500)+(0.9)(2575)=2567.5$
3	2800	$=(0.1)(2600)+(0.9)(2567.5)=2570.75$
4	2400	$=(0.1)(2800)+(0.9)(2570.75)=2593.68$
5		$=(0.1)(2400)+(0.9)(2593.68)=2574.31$

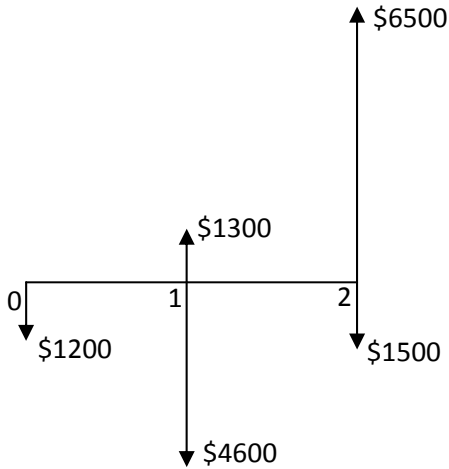
So the demand forecast for 2009 is 2574.

Problem 5

$$P = -\$1200 + (-\$4600 + \$1300)(P/F, 18\%, 1) + (-\$1500 + \$6500)(P/F, 18\%, 2)$$

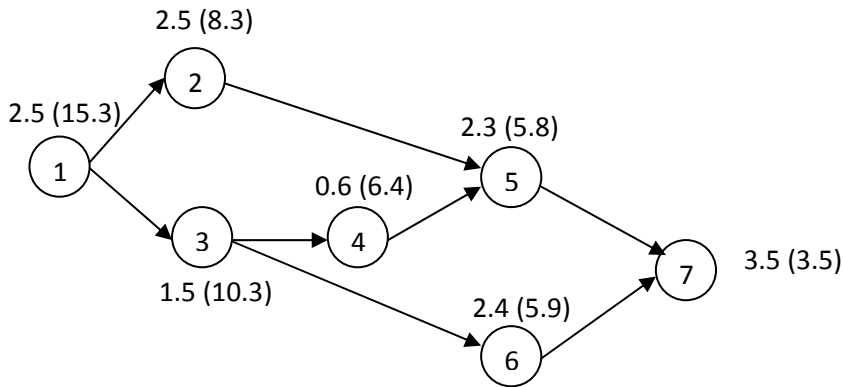
$$= -\$1200 + (-\$3300)(0.8475) + (\$5000)(0.7182)$$

$$= -\$405.75$$



Problem 6

- a) $\tau = \frac{1}{D} = \frac{50 \text{ wk/yr} \cdot 40 \text{ hr/wk}}{24000 \text{ unit/yr}} = \frac{1}{12} \text{ hr/unit} = 5 \text{ min/unit}$
- b) Total work time = $(2.5+2.5+1.5+0.6+2.3+2.4+3.5) \text{ min} = 15.3 \text{ min}$, so the lower bound of the station number is given by $\lceil 15.3/5 \rceil = \lceil 3.06 \rceil = 4$
- c)



Rank: 1 -> 3 -> 2 -> 4 -> 6 -> 5 -> 7

Stations	Total Task Time (min)
1, 3, 4	4.6
2, 6	4.9
5	2.3
7	3.5

Problem 7

$$M = \$1.50/\text{unit}$$

$$C = \$8.00/\text{unit}$$

$$v = C - M = \$6.5/\text{unit}$$

$$s = 60 \text{ min} = 1/10/250 \text{ yr} = 1/2500 \text{ yr}$$

$$A = \$50.00$$

$$p = 5 \text{ min} = 5/60/10/250 \text{ yr} = 1/30000 \text{ yr}$$

$$w = 1/40\% = 2.5$$

$$i = 0.75/\text{yr}$$

$$D = 8000 \text{ unit/yr}$$

$$\text{a) } h_{\text{wip}} = i(M+v/2) = (.75/\text{yr})(\$1.50+\$6.5/2)/\text{unit} = \$3.56/\text{unit/yr}$$

b) Using the EMQ formula

$$Q^* = \sqrt{\frac{2AD}{i \left[(M + v) + 2p w D \left(M + \frac{v}{2} \right) \right]}} = 272.80 \text{ unit/batch}$$

Compare the total cost for $Q = 272$ unit/batch and $Q = 273$ unit/batch:

When $Q = 272$ unit/batch, total cost is \$14961.088;

When $Q = 273$ unit/batch, total cost is \$14961.076.

So $Q^* = 273$ unit/batch.

Problem 8

Using little's law,

$$\text{Throughput Time} = \frac{\text{Average Inventory}}{\text{Sales Rate}} = \frac{4 \text{ batch}}{(3 \text{ batch}) / (8 \text{ hr})} = \frac{32}{3} \text{ hr} = 10 \text{ hr } 40 \text{ min}$$