

1. (a) A coordinate system attached to car A is a translating system, in which

$$\mathbf{a}_B = \mathbf{a}_A + \mathbf{a}_{B/A}$$

Observe that

$$(a_B)_t = 3 \text{ m/s}^2$$

$$(a_B)_n = \frac{v_B^2}{\rho} = \frac{144}{100} = 1.44 \text{ m/s}^2$$

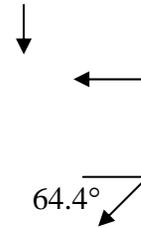
Thus

$$a_B = 3.33 \text{ m/s}^2$$

Either from a graphical or analytical solution,

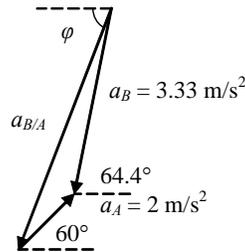
$$a_{B/A} = 5.32 \text{ m/s}^2$$

$$\varphi = 62.72^\circ$$



(b) A coordinate system attached to B is a rotating system. If \mathbf{a}_{rel} is the acceleration of car A as observed from car B , $\mathbf{a}_{\text{rel}} \neq -\mathbf{a}_{B/A}$. It can be shown from rigid-body kinematics that \mathbf{a}_{rel} satisfies

$$\mathbf{a}_A = \mathbf{a}_B + \dot{\boldsymbol{\omega}} \times \mathbf{r}_{A/B} + \boldsymbol{\omega} \times (\boldsymbol{\omega} \times \mathbf{r}_{A/B}) + 2\boldsymbol{\omega} \times \mathbf{v}_{\text{rel}} + \mathbf{a}_{\text{rel}}$$



2. Let T_1 be the tension in the upper string and T_2 tension in the lower string. Force balance on each mass gives

$$4mg - T_1 = 4m\ddot{q}_1 \quad (1)$$

$$3mg - T_2 = 3m\ddot{q}_3 \quad (2)$$

$$mg - T_2 = m\ddot{q}_4 \quad (3)$$

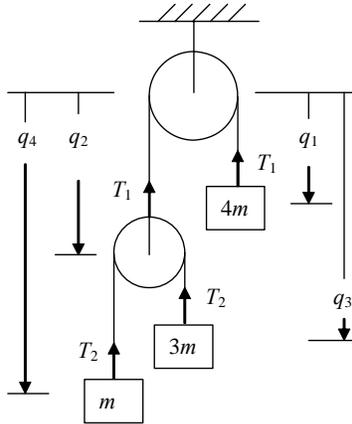
There are five unknowns \ddot{q}_1 , \ddot{q}_3 , \ddot{q}_4 , T_1 , and T_2 in three equations. However,

$$\ddot{q}_3 - \ddot{q}_2 + (\ddot{q}_4 - \ddot{q}_2) = 0 \quad \Rightarrow \quad \ddot{q}_3 + \ddot{q}_4 = 2\ddot{q}_2 = -2\ddot{q}_1$$

$$T_1 = 2T_2$$

Upon solution,

$$\ddot{q}_1 = \frac{1}{7}g = 1.40 \text{ m/s}^2 \quad \downarrow$$



3. Let position 1 of the block be its initial position at 150 mm above the springs. Suppose position 2 corresponds to deflection x in the two springs. Between positions 1 and 2,

$$U = \Delta T + \Delta V_g + \Delta V_e$$

where the work done by forces other than gravitational and spring forces is

$$U = 0$$

$$\Delta T = T_2 - T_1 = 0$$

Define the reference level for measuring potential energy as the level associated with the precompressed springs before impact. Then

$$\Delta V_g = mgh_2 - mgh_1 = mg(-x) - mg(0.15) = -mg(x + 0.15)$$

$$\begin{aligned} \Delta V_e &= 2\left(\frac{1}{2}kx_2^2\right) - 2\left(\frac{1}{2}kx_1^2\right) \\ &= 2\left(\frac{1}{2}k(0.075 + x)^2\right) - 2\left(\frac{1}{2}k(0.075)^2\right) = k[(0.075 + x)^2 - 0.075^2] \end{aligned}$$

Thus

$$U = \Delta T + \Delta V_g + \Delta V_e$$

$$\Rightarrow -mg(x + 0.15) + k[(0.075 + x)^2 - 0.075^2] = 0$$

$$\Rightarrow 5000x^2 + 651.9x - 14.715 = 0$$

$$\Rightarrow x = 0.0196 \text{ or } -0.150$$

The additional deflection is $x = 19.6 \text{ mm}$.

