

**EECS 40, Fall 2006**  
**Prof. Chang-Hasnain**  
**Midterm #2**

October 25, 2006  
 Total Time Allotted: 50 minutes  
**Total Points: 100 / Bonus: 10 pts**

1. This is a closed book exam. However, you are allowed to bring one page (8.5" x 11"), single-sided notes PLUS your 1-page notes from midterm 1.
2. No electronic devices, i.e. calculators, cell phones, computers, etc.
3. Slide rules are allowed.
4. SHOW all the steps on the exam. **Answers without steps will be given only a small percentage of credits.** Partial credits will be given if you have proper steps but no final answers.
5. **Remember to put down units.** Points will be taken off for answers without units.

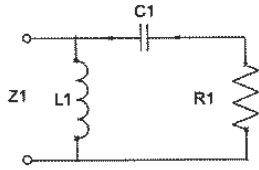
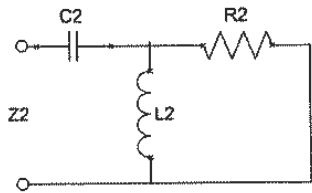
Last (Family) Name: \_\_\_\_\_

First Name: \_\_\_\_\_

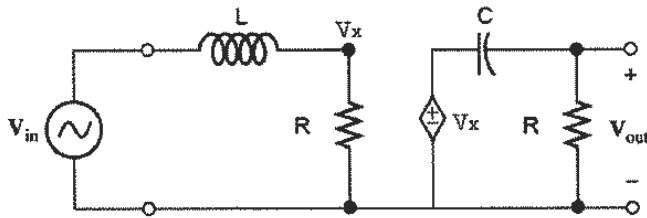
Student ID: \_\_\_\_\_ Discussion Session: \_\_\_\_\_

Signature: \_\_\_\_\_

<b>Score:</b>	
Problem 1 (16 pts) Complex Impedances	
Problem 2 (54 pts): Bode Plots	
Bonus (10 pts):	
Problem 3 (30 pts): Second-order Circuits	
Total	

**1. [16 points] Parallel and Series Complex Impedance**a) [8 pts] What is the complex impedance  $Z_1$ ?b) [8 pts] What is the complex impedance  $Z_2$ ?

## 2. [54 points] Bode Plots:



- (a) [10 points] For the above circuit, show  $H(f) = \frac{1}{1 + j\frac{f}{f_2}} \times \frac{1}{1 - j\frac{f_1}{f}}$
- Express  $f_1$  and  $f_2$  in terms of  $R$ ,  $L$ ,  $C$ . (Hint: Remember  $\omega = 2\pi f$ )

- (b) [6 points] Now Let  $R = 1\text{k}\Omega$ ,  $L = 0.16\text{ mH}$ ,  $C = 0.16\text{ }\mu\text{F}$ , what are  $f_1$  and  $f_2$ ? Remember to put down units.

(c) [22 pt] Bode Magnitude Plot. *You must put down all the steps leading to your results.*

*Hint: You may consider  $f_1 \ll f_2$*

[4 points] Write down the expression for  $y = 10 \log |H(f)|^2$

[4 points] As frequency goes to a very small value, what is the slope of  $y$  as a function of  $\log f$  ?

[4 points] As frequency goes to a very large value, what is the slope of  $y$  as a function of  $\log f$  ?

[4 points] What is  $y$ ,  $f_1 \ll f \ll f_2$  ?

[2 points] What is  $y$  at  $f_1$  ?

[2 points] What is  $y$  at  $f_2$ ?

[2 points] What filter is this?

**Bonus [5 points]** If the input  $|V_{in}| = 1$  V and the frequency is 1 MHz, what is the output  $|V_{out}|$ ?

**Bonus [5 points]** If the input  $|V_{in}| = 1$  V and the frequency is 10 MHz, what is the output  $|V_{out}|$ ?

**(d) [16 pt total] Bode Phase Plot.** *You must put down all the steps leading to your results. Hint: You may consider  $f_1 \ll f_2$*

[4 points] Write down the expression for  $\angle H(f)$

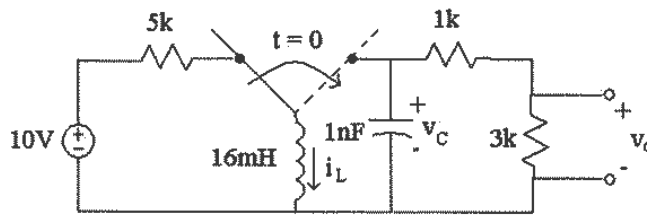
[4 points] What does the value of  $\angle H(f)$  approaches to as  $f \rightarrow 0$ ?

[4 points] What does the value of  $\angle H(f)$  approach as  $f \rightarrow \infty$ ?

[2 points] What is  $\angle H(f)$  at  $f = f_1$ ?

[2 points] What is  $\angle H(f)$  at  $f = f_2$ ?

3. [30 points] Second-order Circuits:



Assume the switch has been to the left for a long time before switching to the right at  $t = 0$ .

(a) Find the following values: [18 points] (Hint: What is  $v_o(t)$  in terms of  $v_C(t)$ ?)

$i_L(0+) =$	
$v_C(0+) =$	$v_C(\infty) =$
$v_o(0+) =$	$v_o(\infty) =$
$\frac{d}{dt} i_L(0+) =$	
$\frac{d}{dt} v_C(0+) =$	
$\frac{d}{dt} v_o(0+) =$	

(b) [6 points] Write the differential equation in terms of  $v_c$ .

(c) [6 points] What are the values of the natural frequency ( $\omega_0$ ) and the damping ratio ( $\zeta$ )?