

University of California at Berkeley
College of Engineering
Dept. of Electrical Engineering and Computer Sciences

EE 105 Midterm II

Spring 2002

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Your Name (Last, First)

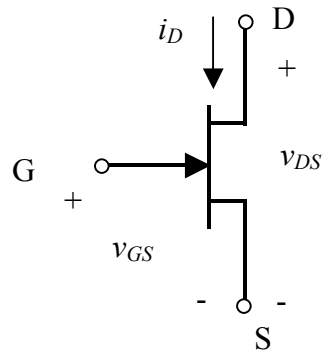
Guidelines

Closed book and notes; one 8.5" x 11" page (both sides) of *your own notes* is allowed.
You may use a calculator.
Do not unstaple the exam.
Show all your work and reasoning on the exam in order to receive full or partial credit.

Score

Problem	Points Possible	Score
1	16	
2	18	
3	16	
<i>Total</i>	50	

1. Junction Field-Effect Transistor (JFET) Model. [16 points].



Device parameters:

$$I_{DSS} = 125 \mu\text{A}$$

$$V_P = -1.5 \text{ V}$$

$$\lambda_n = 0.05 \text{ V}^{-1}$$

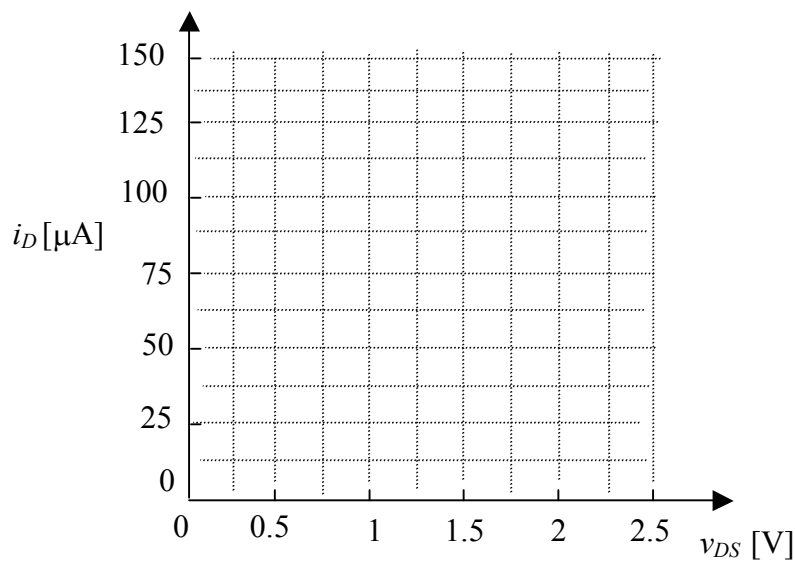
A simplified large-signal model for an n-channel JFET is:

$$i_D = \frac{2I_{DSS}}{V_P^2} (v_{GS} - V_P - \frac{v_{DS}}{2}) v_{DS} (1 + \lambda_n v_{DS}) \text{ for } v_{DS} \leq v_{GS} - V_P \text{ and } V_P \leq v_{GS} \leq 0 \text{ V (triode)}$$

$$i_{D.SAT} = \frac{I_{DSS}}{V_P^2} (v_{GS} - V_P)^2 (1 + \lambda_n v_{DS}) \text{ for } v_{DS} \geq v_{GS} - V_P \text{ and } V_P \leq v_{GS} \leq 0 \text{ V (saturation)}$$

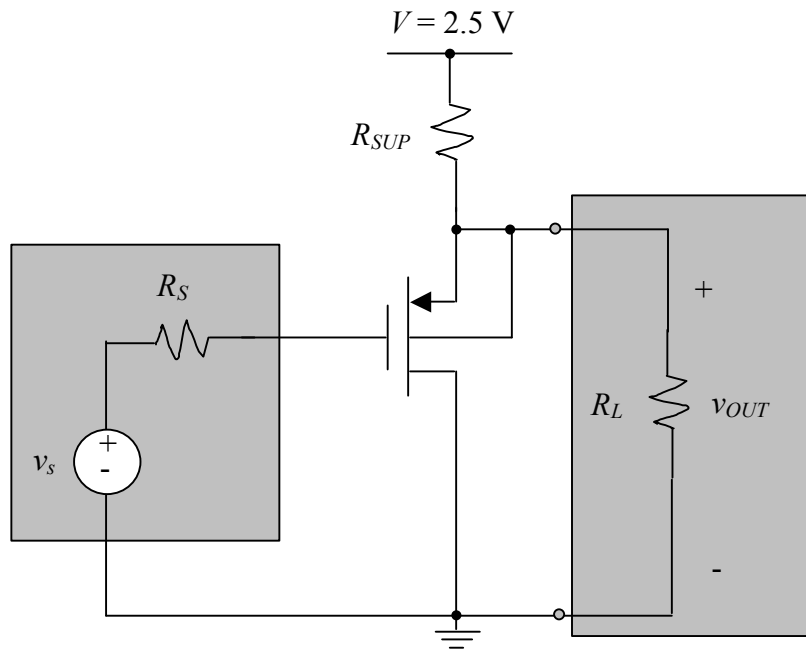
where V_P is the pinch-off voltage and λ_n is the “fudge factor.”

- (a) [4 pts.] Sketch the drain characteristics for this JFET on the graph below for $v_{GS} = 0 \text{ V}, -0.5 \text{ V}, -1 \text{ V},$ and -1.5 V . You can set $\lambda_n = 0$ for this part. Your current values in saturation should be accurate; the triode curves can be sketched.



- (b) [4 pts.] What is the numerical value of the small-signal transconductance g_m at the operating point Q_1 ($V_{GS} = -0.5$ V, $V_{DS} = 1.5$ V)? Notes: (i) λ_n is not zero for this part, (ii) you don't need the plots in part (a) in order to answer this question.
- (c) [4 pts.] What is the numerical value of the small-signal drain resistance r_o at the operating point Q_1 ($V_{GS} = -0.5$ V, $V_{DS} = 1.5$ V). Notes: (i) λ_n is not zero for this part, (ii) you don't need the plots in part (a) in order to answer this question.
- (d) [4 pts.] What is the numerical value of the small-signal transconductance g_m at the operating point Q_2 ($V_{GS} = -0.5$ V, $V_{DS} = 0.5$ V). Again, you don't need the plot in part (a) in order to answer this question.

2. MOSFET single stage amplifier [18 pts.]



Given:
 $L = 1 \mu\text{m}$
 $\mu_p C_{ox} = 62.5 \mu\text{A}/\text{V}^2$
 $V_{Tp} = -1 \text{ V}$
 $\lambda_p = 0.025 \text{ V}^{-1}$
 $g_{mb} = g_m/10$

$R_S = 10 \text{ k}\Omega$
 $R_{SUP} = 5 \text{ k}\Omega$
 $R_L = 1 \text{ k}\Omega$

(a) [3 pts.] Find the numerical value of channel width W in μm in order that the DC output voltage $V_{OUT} = 1.25 \text{ V}$. Note: the gray boxes indicate small-signal elements that can be neglected for the DC bias analysis.

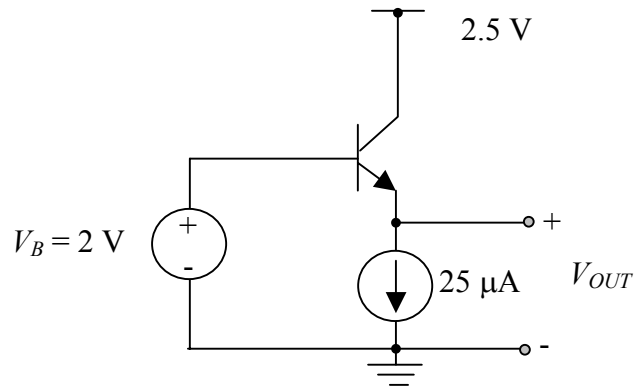
(b) [3 pts.] What is DC power dissipated in the MOSFET in μW ?

- (c) [3 pts.] Find the numerical value of the output resistance R_{out} of this amplifier in $k\Omega$. If you couldn't solve part (a), you can assume for this part that the channel width $W = 100 \mu\text{m}$ (not the correct answer to (a), of course.)
- (d) [3 pts.] Find the numerical value of the two-port parameter A_v , the open-circuit voltage gain, for this amplifier. Again, if you couldn't solve part (a), you can assume for this part that the channel width $W = 100 \mu\text{m}$ (not the correct answer to (a), of course.)
- (e) [3 pts.] Find the overall voltage gain v_{out} / v_s with R_S and R_L present (values of which are given next to the schematic on the previous page). If you couldn't solve (c) or (d), you can assume for this part that $R_{out} = 2.5 k\Omega$, and $A_v = 0.85$. Needless to say, these are not correct answers to either (c) or (d).

- (f) [3 pts.] We now remove the small-signal source and its resistance and replace it with a large-signal source v_{IN} ; we also remove the load resistor. Assuming the MOSFET remains in the saturation (constant-current) region and neglecting channel-length modulation ($\lambda_n = 0$), find an equation for v_{IN} in terms of v_{OUT} . If you couldn't solve part (a), you can assume that $W = 100 \mu\text{m}$ for this part.

What is the numerical value of v_{IN} for the case when $v_{OUT} = 2 \text{ V}$?

3. npn bipolar transistors [16 pts.]



Given:

Base width = $W_B = 100\text{ nm} = 0.1\text{ }\mu\text{m}$

Emitter-base junction area = $A_E = 5\text{ }\mu\text{m}^2$

Emitter width = $W_E = 75\text{ nm} = 0.075\text{ }\mu\text{m}$

Base-collector junction area = $A_C = 15\text{ }\mu\text{m}^2$

Electron diffusion constant in base: $D_n = 20\text{ cm}^2/\text{s}$

Hole diffusion constant in emitter: $D_p = 5\text{ cm}^2/\text{s}$

Electron charge: $-q = -1.6 \times 10^{-19}\text{ C}$

Intrinsic concentration: $n_i = 10^{10}\text{ cm}^{-3}$

$V_{th} = 26\text{ mV}$

- (a) [4 pts.] Find the numerical value of the electron diffusion current density J_{nB} in the base [units $\mu\text{A}/\mu\text{m}^2$]. Neglect the base current I_B for this part.

- (b) [4 pts.] What is the numerical value of $n_{pB}(x = 0)$, the minority electron concentration in the base at the edge of the emitter-base depletion region? Again, you can neglect the base current I_B for this part.

(c) [3 pts.] Find the numerical value of V_{OUT} to 3 significant figures. The base doping is $N_{aB} = 1 \times 10^{17} \text{ cm}^{-3}$. You can neglect the base current for this part, too.

(d) [4 pts.] We now increase V_B above 2 V to the point where the minority carrier concentrations in the bipolar transistor are given by the plot below. The value of $n_{pB}(0)$ is unchanged from parts (b) and (c). What is the value of V_B to 3 significant figures? *Note:* if you can't find the exact value, the answer to 2 significant figures is worth 2 pts.

