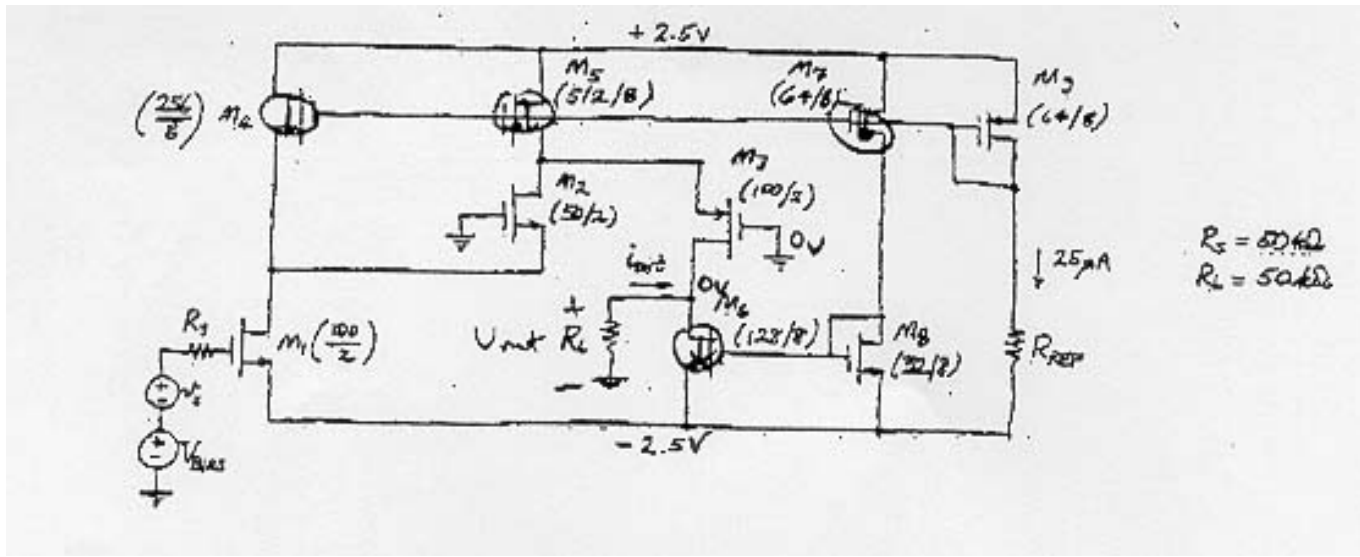


EECS 105 Spring 1998 Final

1. CMOS Transconductance Amplifier [35 pt]



(a) [3 pts] Find the numerical value of R_{REF} .

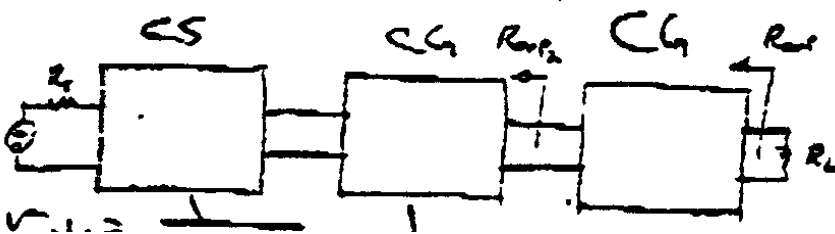
(b) [3 pts] Redraw the circuit with all currents supplies replaced by symbols.

(c) [3 pts] Find the numerical values of the DC currents and voltages listed in the table below.

Note that V_{BIAS} is selected such that $V_{OUT} = 0V$.

M1	ID1	V
M2	ID2	
M3	ID3	

(d) [4 pts] This three-stage amplifier can be modeled as the cascade below. Find the numerical value of $R_{OUT, 2}$. Answers within $\pm 5\%$ of the correct answer will receive full credit.



(e) [4 pts] Find the numerical value of the output resistance R_{OUT} . Answers within $\pm 5\%$ of the correct answer will receive full credit.

(f) [5 pts] Find the numerical value of the overall transconductance of the amplifier, i_{OUT}/v_S , including the effects of R_S and R_L – the values of which are both $50\text{ k}\Omega$. R_{OUT} , 2.

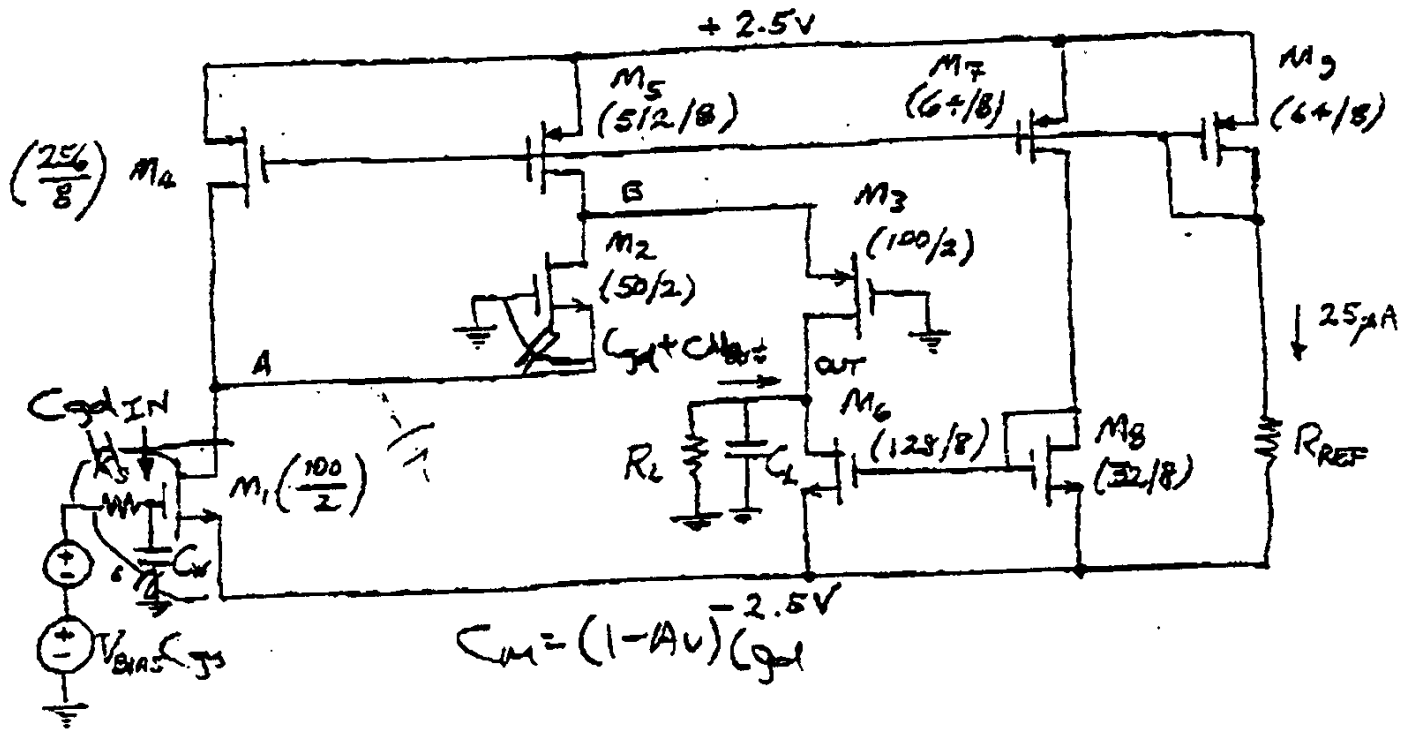
Answers within $\pm 5\%$ of the correct answer will receive full credit.

(g) [5 pts] Find the maximum value of the output current $i_{OUT, max}$ for which all transistors remain in their constant-current regions. (Note that "maximum" means "most positive" in this case.)

(h) [4 pts] Find the minimum value of the output current $i_{OUT, min}$ for which all transistors remain in their constant-current regions. (Note that "minimum" means "most negative" in this case.)

- i. [4 pts] On the graph below, sketch i_{OUT} versus v_S . Your plot should include the limits to i_{OUT} that you found in parts (g) and (h). If you couldn't solve these parts, you can assume that $i_{OUT, max} = 70 \mu A$ and $i_{OUT, min} = -100 \mu A$

2. Frequency Response of CMOS Transconductance Amplifier



Note that a wiring capacitance $C_W = 50 \text{ fF}$ and a load capacitance $C_L = 500 \text{ fF}$ have been added to the schematic.

- a. [5 pts] Find the open-circuit time constant for the capacitance between node "IN" and ground. Use the Miller theorem to transform any capacitance connected from "IN" to another node into an equivalent capacitance to ground. Answers within $\pm 5\%$ of the correct answer will receive full credit.

(b) [5 pts] Find the open-circuit time constant for the capacitance between node "A" and ground. Use the Miller theorem to transform any capacitance connected from "A" to another node into an equivalent capacitance to ground. Answers within $\pm 5\%$ of the correct answer will receive full credit.

(c) [5 pts] Find the open-circuit time constant for the capacitance between node "B" and ground. Use the Miller theorem to transform any capacitance connected from "B" to another node into an equivalent capacitance to ground. Answers within $\pm 5\%$ of the correct answer will receive full credit.

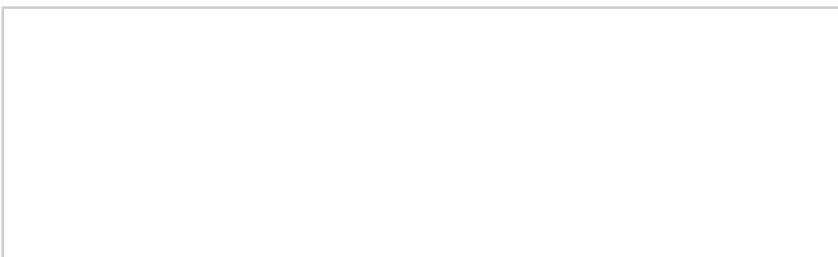
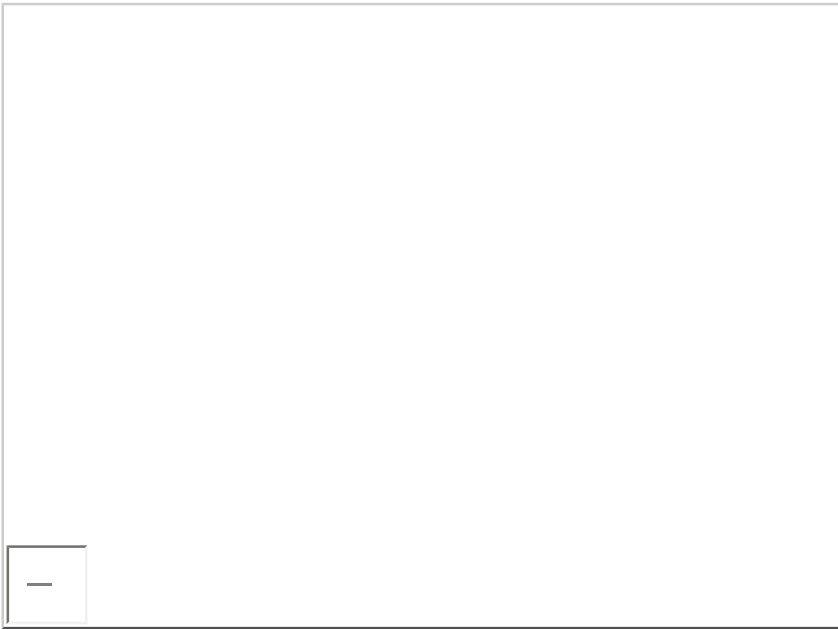
- d. [5 pts.] Find the open-circuit time constant for the capacitance between node "OUT" and ground. Use the Miller theorem to transform any capacitance connected from "OUT" to another node into an equivalent capacitance to ground. Answers within $\pm 5\%$ of the correct answer will receive full credit.

(e) [4 pts] What is the -3 dB frequency f_1 of this amplifier in MHz, according to the open-circuit

time constant approximation? Answers within $\pm 5\%$ of the correct answer will receive full credit. Note that you need not have done (a), (b), (c), and (d) in order to answer this part

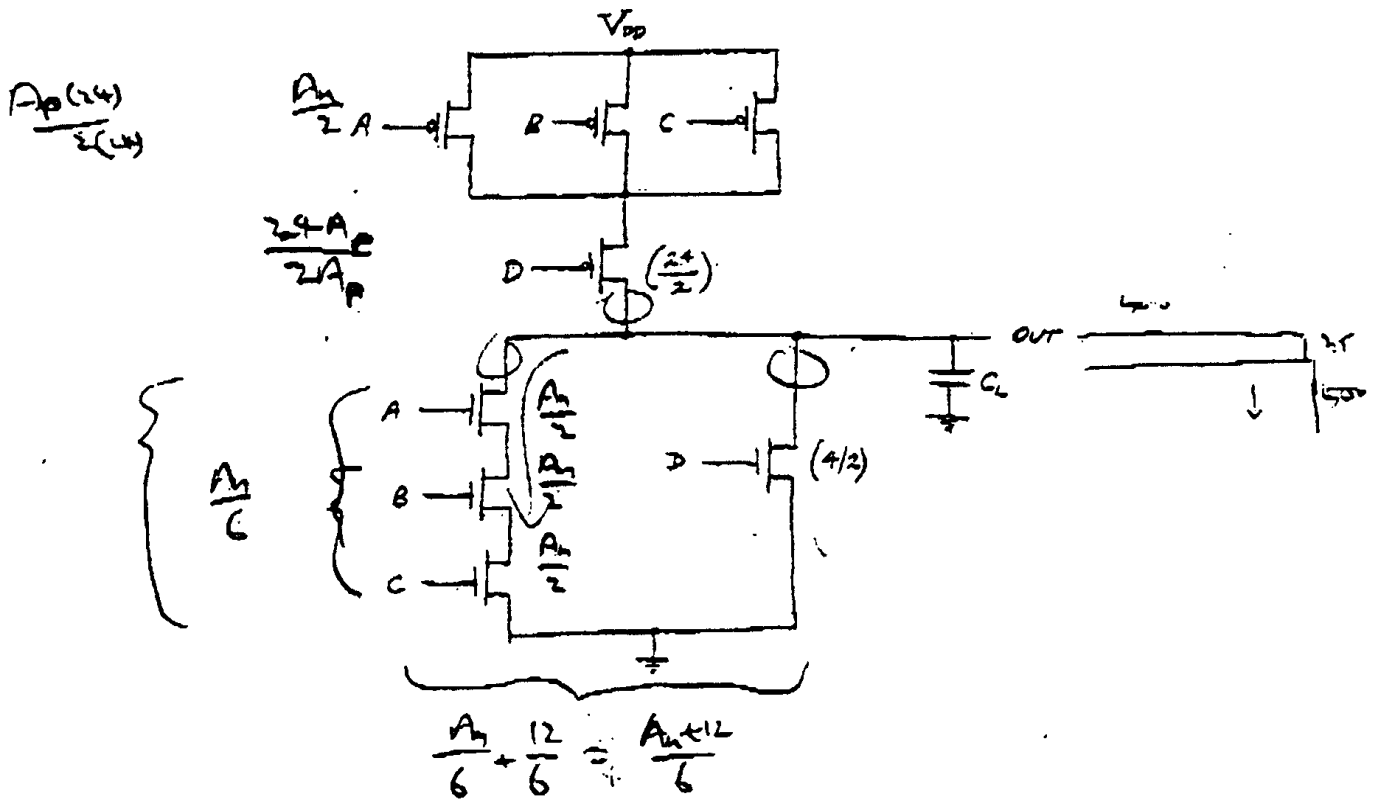
with adequate precision.

- e. [6 pts] SPICE simulation shows that the next pole is located at $f_2 = 50$ MHz. Plot the transfer function I_{OUT}/V_S on the graphs below. Note that the units of the gain will be "20 log Siemens". If you couldn't solve part (d), you can assume that $f_1 = 2$ MHz for this part. Also, if you couldn't solve (f), you can assume that $I_{OUT}/V_S = 0.5$ mS for this part.





3. CMOS Digital Gate [20 pts]



- a. (c) [2 pts] What is the logic function implemented by this gate?
 [2 pts] What is the logic function implemented by this gate?

(b) [3 pts] Find the widths of NMOS transistors A, B, and C such that the high-to-low propagation delay t_{PHL} is the same as the slowest t_{PHL} . Given: $W_{An} = W_{Bn} = W_{Cn}$ and all transistors have the same gate length $L = 2\mu\text{m}$

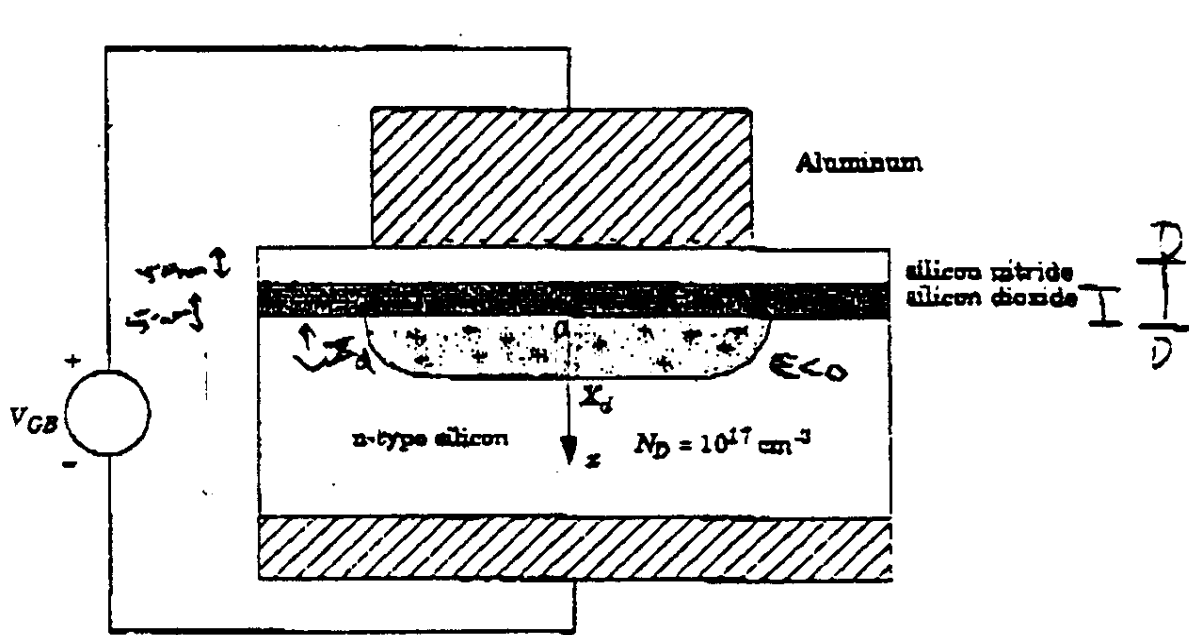
- c. [3 pts.] Find the widths of PMOS transistors A, B, and C such that the worst-case low-to-high propagation delay is equal to the high-to-low propagation delay: $t_{PLH, wc} = t_{PHL}$. Given: $W_{An} = W_{Bn} = W_{Cn}$ and all transistors have the same gate length $L = 2\mu\text{ m}$.

d. [3 pts] Find the numerical value of CDB for this gate in fF.

e. [3 pts.] The aluminum line from the output to the next gate is $500 \mu\text{m}$ in the length and $2.5 \mu\text{m}$ wide. Given that the field oxide under the aluminum is 500nm in thickness, find the numerical value of the wire capacitance C_W .

- f. [3 pts.] Find the max fanout of this logic gate, assuming that the output is connected to one input of each of the CMOS gates and that the transistors in these "load gates" have dimensions: PMOS: $(W/L) = 20/2$ and NMOS: $(W/L) = 10/2$. The propagation delay must be less than 15 ns. If you couldn't get parts (d) and (e), you can assume that $C_{DB} = 200$ fF and that $C_W = 150$ fF

- g. [3 pt] Estimate the minimum supply voltage V_{DD} for which the noise margins of this logic gate will be greater than 500mV



4. MOSE

Electrostatics [15 pts]

Given: Permittivities ϵ (silicon) = $11.7 \epsilon_0$ (silicon, $X_d = -750 \text{ \AA} = 75 \text{ nm}$) ϵ (oxide) = $3.9 \epsilon_0$ (silicon dioxide) thickness; $t = 500 \text{ \AA} = 50 \text{ nm}$ ϵ (silicon nitride) = $7.5 \epsilon_0$ (silicon nitride) thickness; $t = 50 \text{ nm}$

- a. [4pts] Find the numerical value of the electric field $E(x=0^+)$, which is just inside the silicon.

b. [3 pts] Find the numerical value of the electric field $E(x=0^-)$, which is just inside the silicon dioxide. If you couldn't solve (a), assume $E(x=0^+) = 50 \text{ kV/cm}$.

c. [4 pts] Find the numerical value of the potential drop across the oxide/nitride sandwich. You can make the

same assumption as in (b) as a default.

(d) [4 pts] Find the numerical value of the capacitance C_{gb} for the MOS capacitor biased as shown in the figure.

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If you have any questions about these online exams
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