

EECS 140

NAME

SOLUTIONS

FALL 1996

MIDTERM #2

$$k_n' = k_p' = 10^{-4} \text{ A/V}^2$$

$$\gamma_n = \gamma_p = 0$$

$$\lambda_n = \lambda_p = .01$$

$$V_{Tn} = V_{Tp} = 1 \text{ V.}$$

$$C_{gd} = 1 \text{ ff}$$

$$C_{db} = 10 \text{ ff}$$

$$C_{gs} = 100 \text{ ff}$$

$$C_{gb} = 5 \text{ ff}$$

$$C_{sb} = 10 \text{ ff}$$

SHOW YOUR WORK!

- 1
- a 2.1V.
  - b 220 M $\Omega$
  - c .45 m $\Omega$
  - d 203  $\mu$ RAD/SEC.

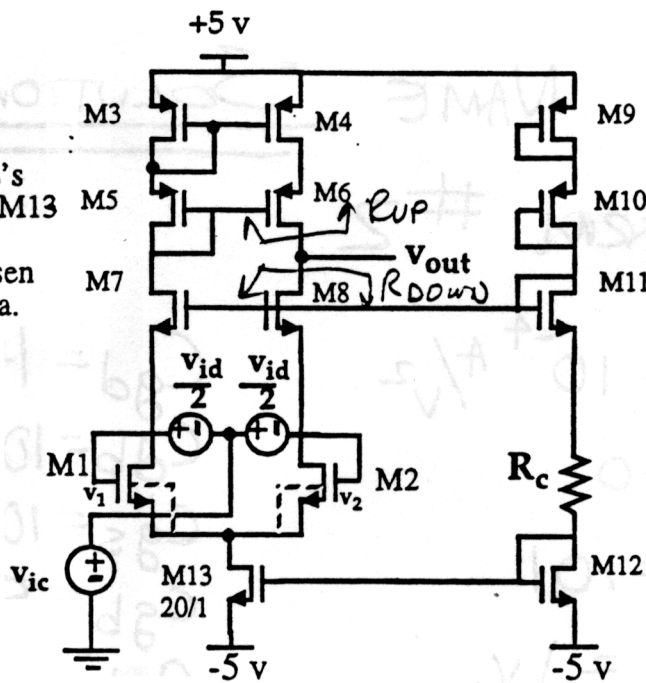
X

- a 3700
  - b 400 RAD/SEC
  - c 9.4 MRAD/SEC
- 4
- a SHUNT-SERIES
  - b .01
  - c X
  - d 25
  - e 2.5 M $\Omega$

Problem 1)

All transistor W/L's are 10, except for M13

Assume  $R_c$  is chosen so that  $I_{ref} = 100 \mu A$ .



$$V_{DSAT} = \left( \frac{2 I_{DS}}{\mu_2' W/L} \right)^{1/2}$$

$$= \left( \frac{2 \cdot 10^{-4}}{10^{-4} \cdot 10} \right)^{1/2}$$

$$= 0.45 V$$

a) What is the DC voltage at vout?

2.1 V

$$2V_T + 2V_{DSAT} = 2.9$$

$$5 - 2.9 = 2.1 V$$

$$r_o = \frac{1}{\lambda I_{DS}} = 1 M\Omega$$

$$g_m = 0.45 mS$$

b) What is Rout (seen at vout)?

$2.25 \times 10^8 \Omega$

$$R_{JP} = r_o (1 + g_m r_o) = 10^6 \cdot (1 + 0.45 \times 10^{-3} \cdot 10^6) = 4.5 \times 10^8 \Omega$$

$$R_{DOWN} = R_{JP}$$

$$R_{OUT} = R_{JP} \parallel R_{DOWN}$$

c) What is  $G_m = i_{out}/v_{id}$  ( $i_{out}$  is the current out if  $v_{out}$  is grounded)?

0.45 mS

$$G_m = g_m = 0.45 mS$$

c) What is the -3db freq of the gain,  $v_{out}/v_{id}$ ?

$2.03 \times 10^5 \text{ RAD/SEC}$

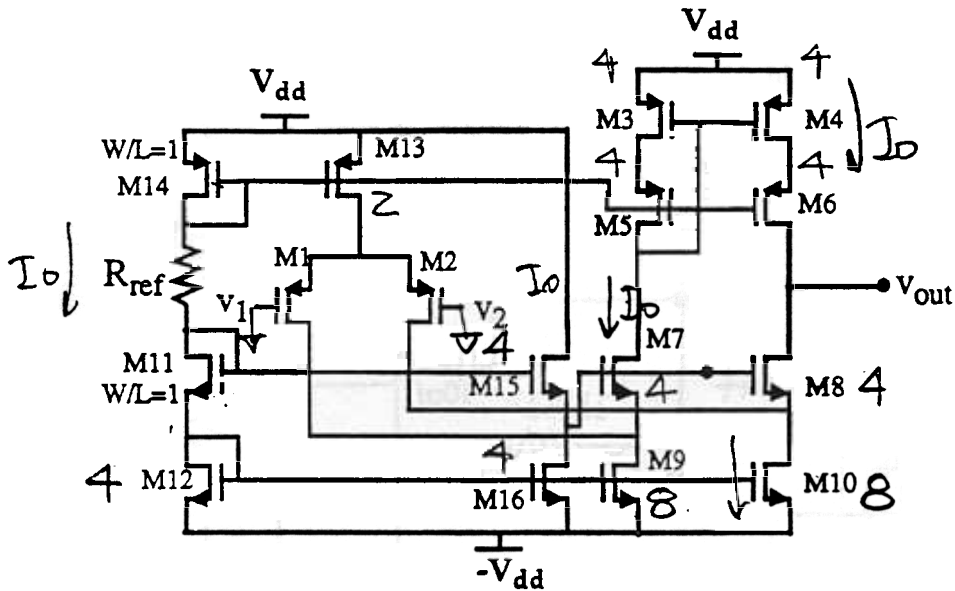
AT THE  $v_{OUT}$  NODE

$$C_{OUT} = C_{db6} + C_{gd6} + C_{db8} + C_{gd8} = 22 fF$$

$$\omega_{3dB} = \frac{1}{22 \times 10^{-15} \times 2.2 \times 10^8}$$

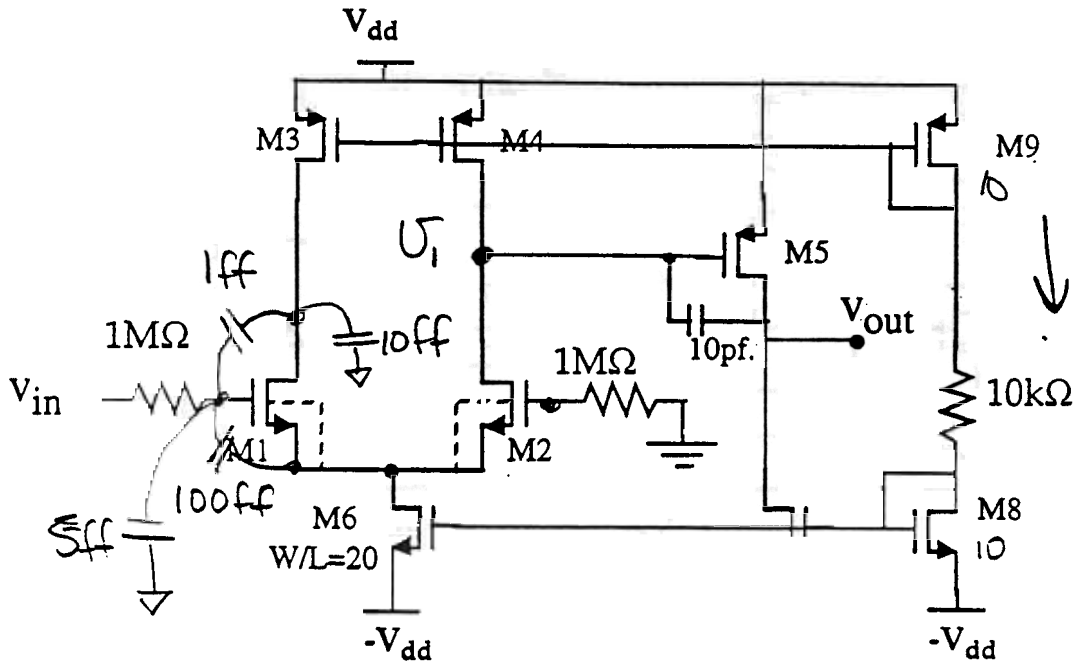
$$= 2.03 \times 10^5 \text{ RAD/SEC}$$

Problem 2)



Choose the values of the W/L's for all the transistors (except for M11 and M14 which are 1), so that the currents in all transistors have the same value,  $I_o$ , except for M9, M10 and M13 which are twice that value or  $2I_o$ . Also, choose those sizes so that M3, M4, M9 and M10 are biased at the edge of saturation.  $\lambda=0$  for this problem.

- M1 ANY VALUE
- M2 SAME AS M1
- M3 4
- M4 4
- M5 4
- M6 4
- M7 4
- M8 4
- M9 8
- M10 8
- M11 1
- M12 4
- M13 2
- M14 1
- M15 4
- M16 4



a) What is the DC gain  $3.7 \times 10^3$

$$\frac{V_{out}}{V_{in}} = \underbrace{\left(\frac{g_m}{2} \left(\frac{r_o}{2}\right)\right)}_{1^{st} \text{ STAGE}} \underbrace{\left(g_m \frac{r_o}{2}\right)}_{2^{nd} \text{ STAGE}} = \frac{(g_m r_o)^2}{8}$$

$$I_{ref} = \frac{10 - 2V_T - 2V_{SAT}}{10k\Omega} = 0.8 \text{ mA} - 0.14 \text{ mA} (I_{cm})$$

$$I_{ref} = 0.68 \text{ mA}$$

$$g_m = 1.17 \times 10^{-3}$$

$$r_o = 147k\Omega$$

For parts b) & c) use  $g_m = 10^{-3}$  &  $r_o = 1M\Omega$  FOR

b) What is the lowest frequency pole  $400 \text{ RAD/SEC}$  ALL TRANSISTORS:  $M5: C_{gs} = 10 \text{ pF}$

$$\omega_1 = \frac{1}{r_o/2 \cdot 10^{-11} \cdot \frac{g_m r_o}{2}} = 400 \text{ RAD/SEC}$$

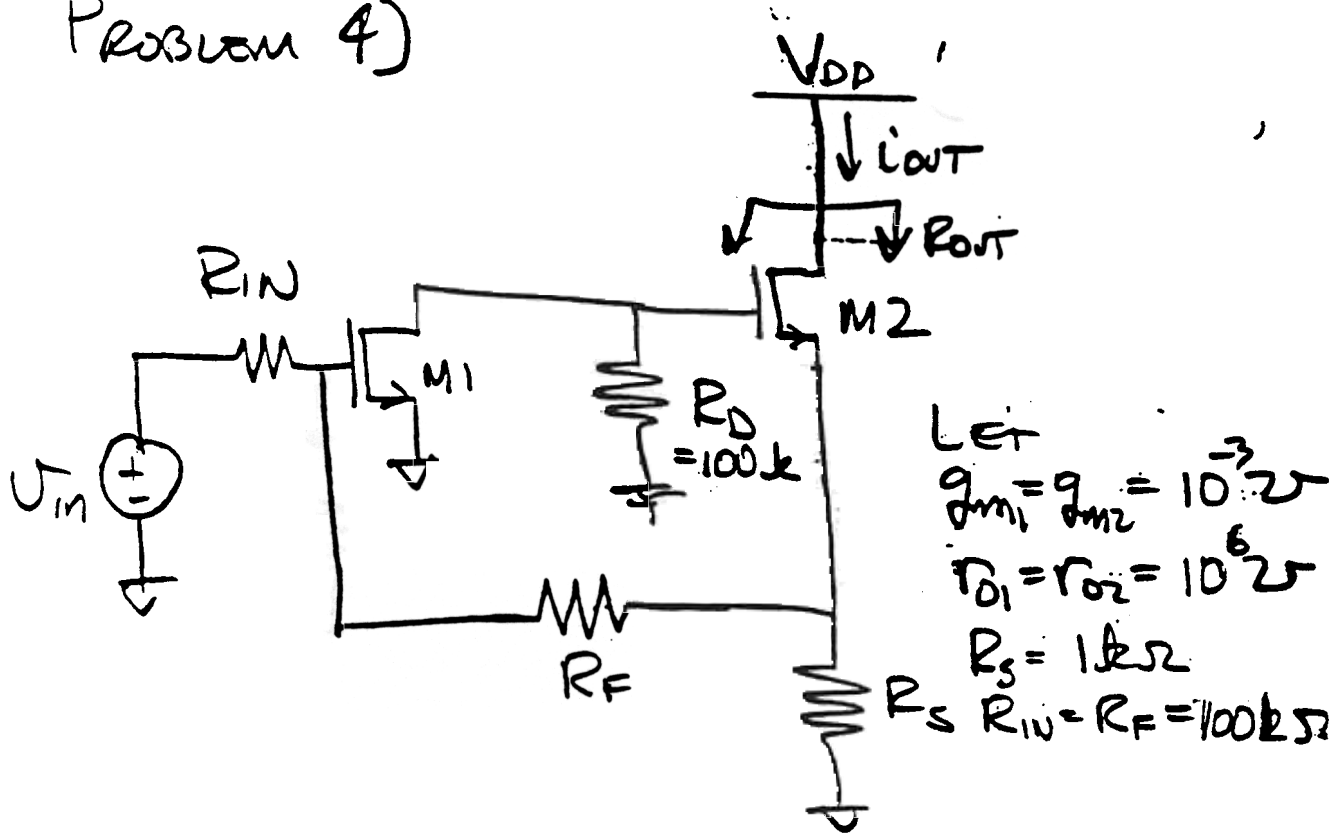
CHECK MILLER ON M2  $\left(\frac{g_m r_o}{4}\right) 1 \text{ fF} = 172 \text{ fF}$  SMALL WITH SAME  $r_o$

c) What is next lowest frequency pole  $9.4 \times 10^6 \text{ RAD/SEC}$

SINCE M5 AND THE 10pF CAP LOOK LIKE  $V_{gs}$  AT  $\omega \gg \omega_1$  THE GAIN AT  $V_1$  IS SMALL THUS NO MILLER MULT. THE EFFECTIVE CAPACITANCE AT THE GATE OF M2 IS

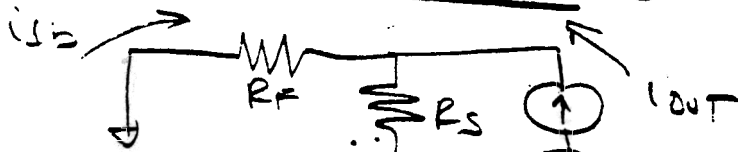
$$C_{eff} = C_{gs2} + C_{gd2} + C_{gb2} \approx 106 \text{ fF} \quad \omega_2 = \frac{1}{10^6 \cdot 106 \times 10^{-15}} = 9.4 \times 10^6 \text{ RAD/SEC}$$

# Problem 4)



a) WHAT KIND OF FEEDBACK? SHUNT-SERIES

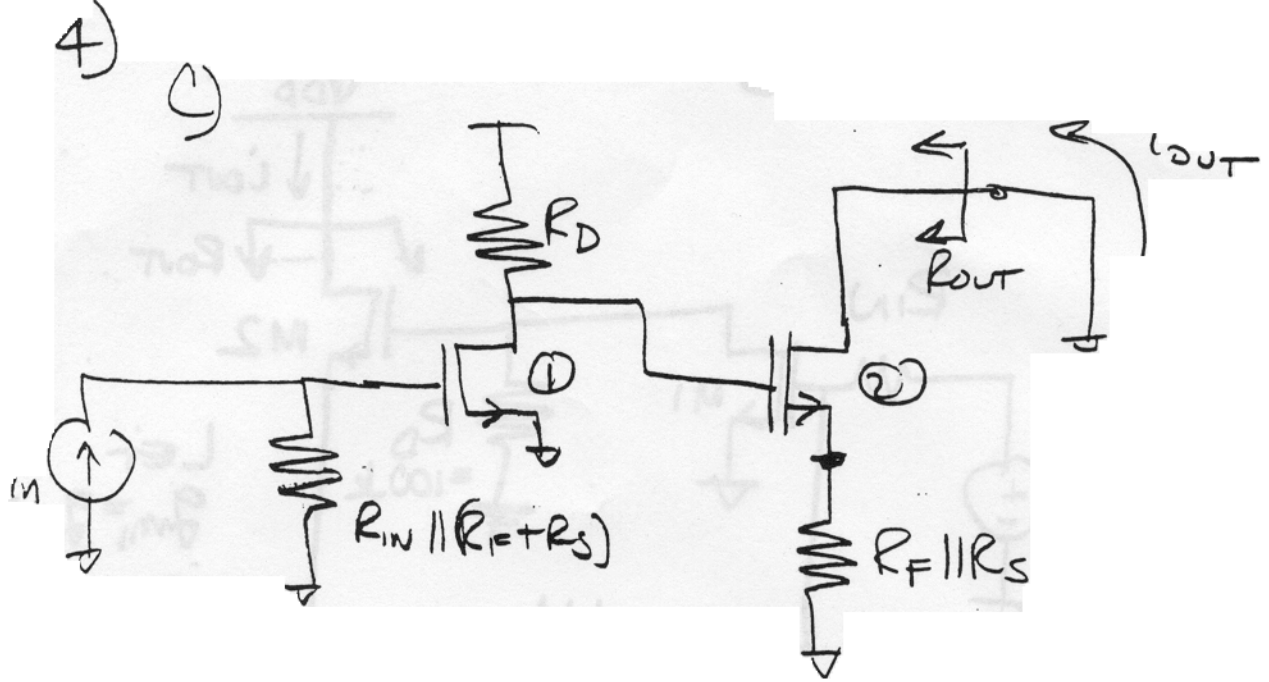
WHAT IS  $f$ ?  $-\frac{R_S}{R_F + R_S}$



DRAW THE BASIC AMPLIFIER, WITH LOADING OF THE FEEDBACK NETWORK, ON THE NEXT PAGE.

d) CALCULATE THE GAIN OF THE BASIC AMPLIFIER (WITH LOADING).

WHAT IS  $R_{out}$ ?



d)

$$a_v = g_{m1} [R_{in} \parallel (R_F + R_S)] (R_D \parallel r_o) \left[ \frac{g_{m2}}{1 + g_{m2}(R_F \parallel R_S)} \right]$$

$$= 10^{-3} (50 \mu\text{A}) 91 \Omega \frac{0^3}{+ 10^{-3} / 1 \Omega} = 2300$$

e)

$$r_{out}' = (R_F \parallel R_S) + r_{o2} (1 + g_{m2}(R_F \parallel R_S))$$

$$= 2 \Omega + 10^6 (1 + 1) = 2 \times 10^6 \Omega$$

$$R_{out} = (1 + T') r_{out}' = (1 + 23) (2 \times 10^6) \Omega = 48 \times 10^6 \Omega$$

$$T \text{ at } f = 23$$