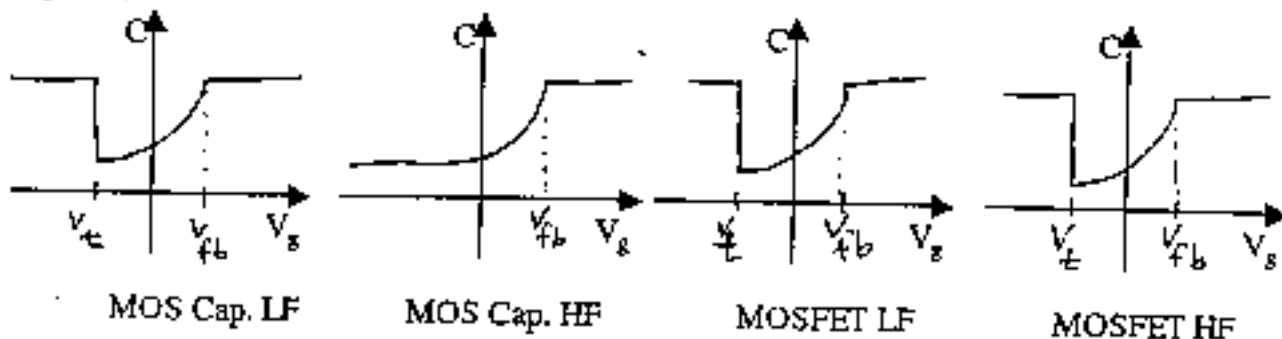


# EE 130, Spring/2000 Midterm II Solutions Professor C. Hu

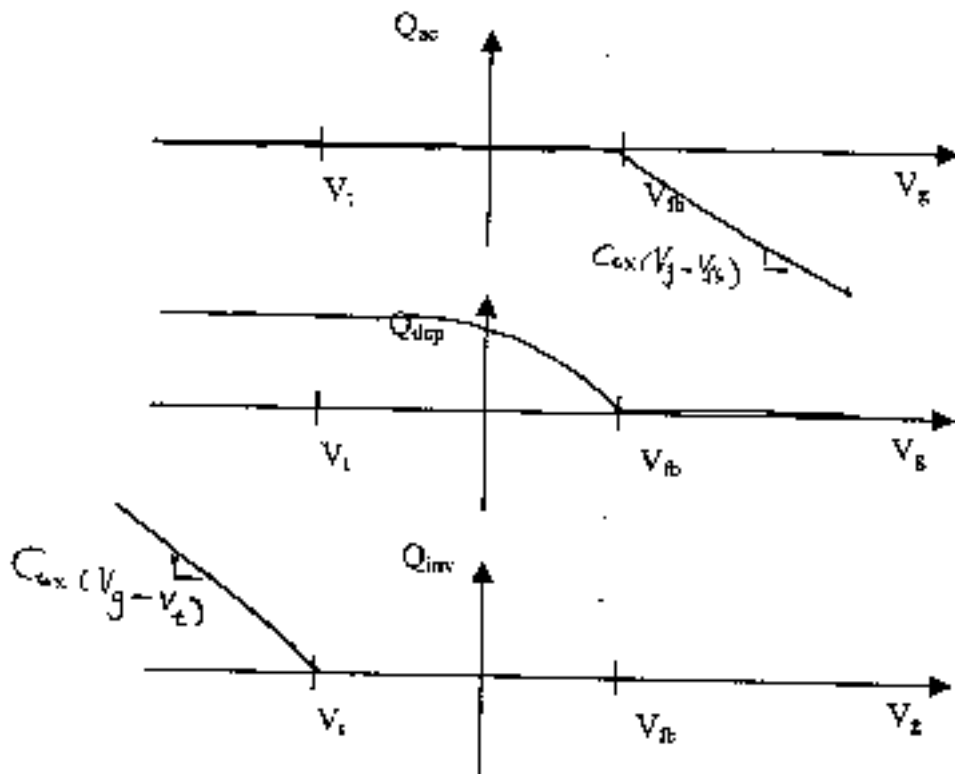
## Problem #1

1. Consider a PMOSFET with a P+ poly-silicon gate and a N-type body. The body doping concentration is  $2.0 \times 10^{17} \text{ cm}^{-3}$ , and gate oxide thickness is 10nm. (35 Points)

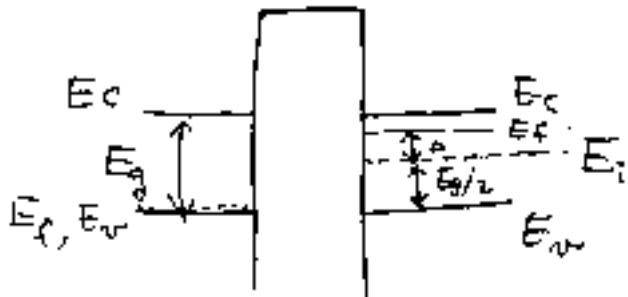
(a) Qualitatively sketch the C-V curve of MOS capacitor and MOSFET for high frequency and low frequency. (No need to calculate  $V_{fb}$  and  $V_t$  here) (7 pts)



(b) Draw charge vs gate voltage of PMOSFET qualitatively. (7 pts)



(c) Calculate the flat band voltage. (7 pts)



$$V_{fb} = E_g/2 + \Delta = E_g/2 + K \cdot T/q \cdot \ln(N_{sub}/N_i) = 0.55 + 0.026 \cdot \ln(2.0 \cdot 10^{17} / (1.0 \cdot 10^{10})) = 0.55 + 0.44 = 0.99V$$

(d) Calculate the threshold voltage. (7 pts)

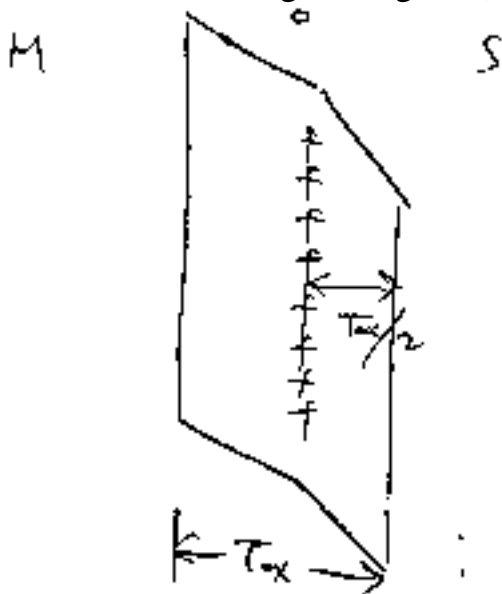
$$V_t = V_{fb} - 2 \cdot \Phi_{ib} - (2 \cdot \epsilon_{Si} \cdot q \cdot N_{sub} \cdot 2 \cdot \Phi_{ib})^{0.5} / C_{ox}$$

$$\Phi_{ib} = K \cdot T/q \cdot \ln(N_{sub}/N_i) = 0.44 \text{ (} = \Delta \text{ in (d) )}$$

$$C_{ox} = \epsilon_{SiO_2} / T_{ox} = 3.9 \cdot 8.85 \cdot 10^{-14} / 10^{-6} = 3.45 \cdot 10^{-7} \text{ (F/cm}^2\text{)}$$

$$V_t = 0.99 - 2 \cdot 0.44 - 2.41 \cdot 10^{-7} / (3.45 \cdot 10^{-7}) = -0.59V$$

(e) A sheet of electrons ( $6.9 \cdot 10^{-8} C/cm^2$ ) is trapped at the center of the gate oxide. How much is the threshold voltage changed? (7 pts)

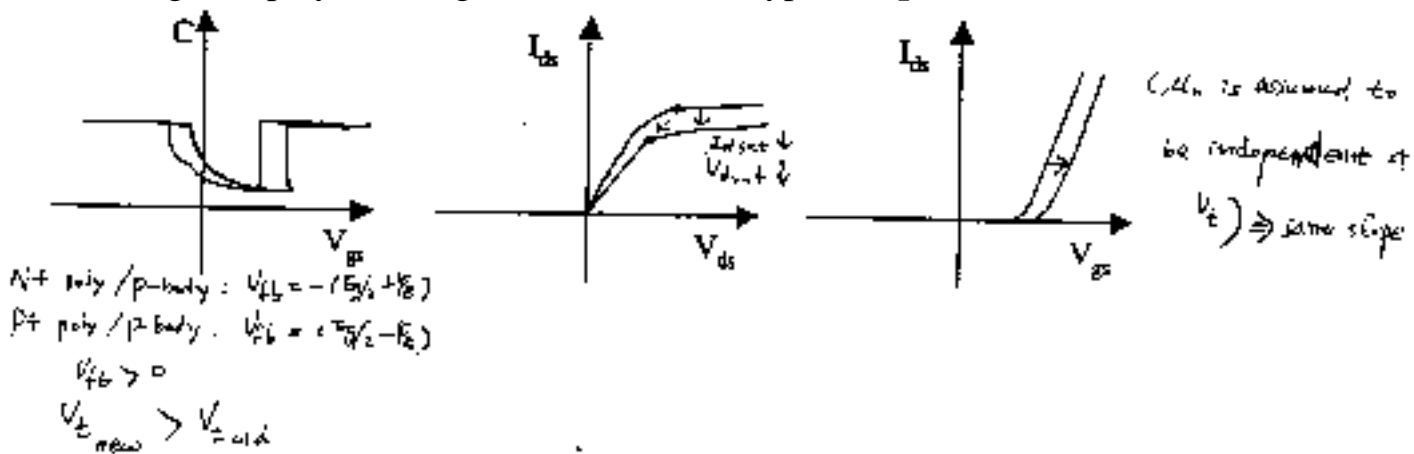


$$\Delta V_t = -Q / C_{ox} = -Q / (\epsilon_{SiO_2} / (T_{ox}/2)) = -Q / (2 \cdot C_{ox}) = -(-6.9 \cdot 10^{-8}) / (2 \cdot 3.45 \cdot 10^{-7}) = 0.1V$$

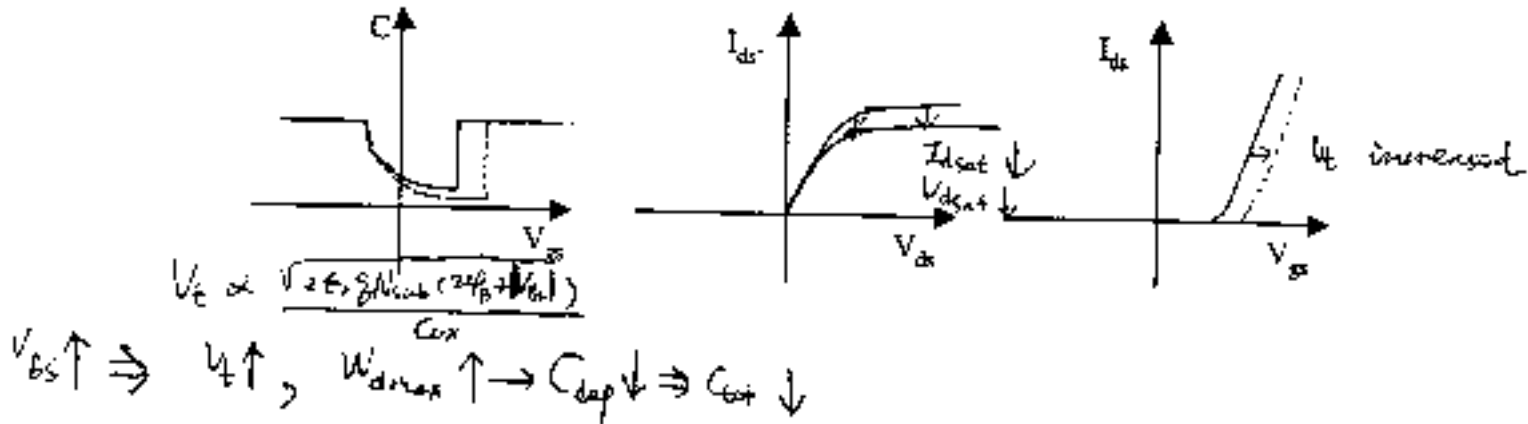
## Problem #2

Qualitatively sketch the C-V, Id-Vg, and Id-Vd curves for an NMOSFET to indicate how the curves would differ in response to the changes given below. Assume the mobility is fixed for (a) and (b). (30 pts)

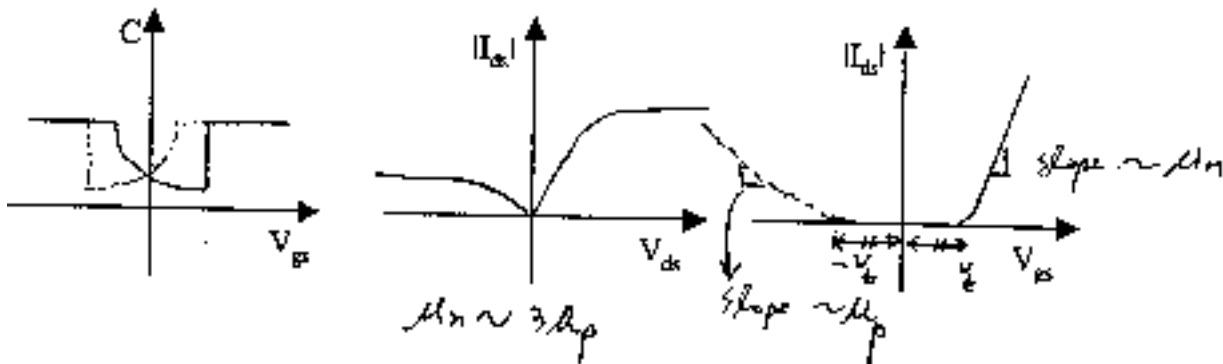
(a) Change the poly-silicon gate from N+ to P+ type: (10 pts)



(b) Reverse back bias is applied to the body. (10 pts)

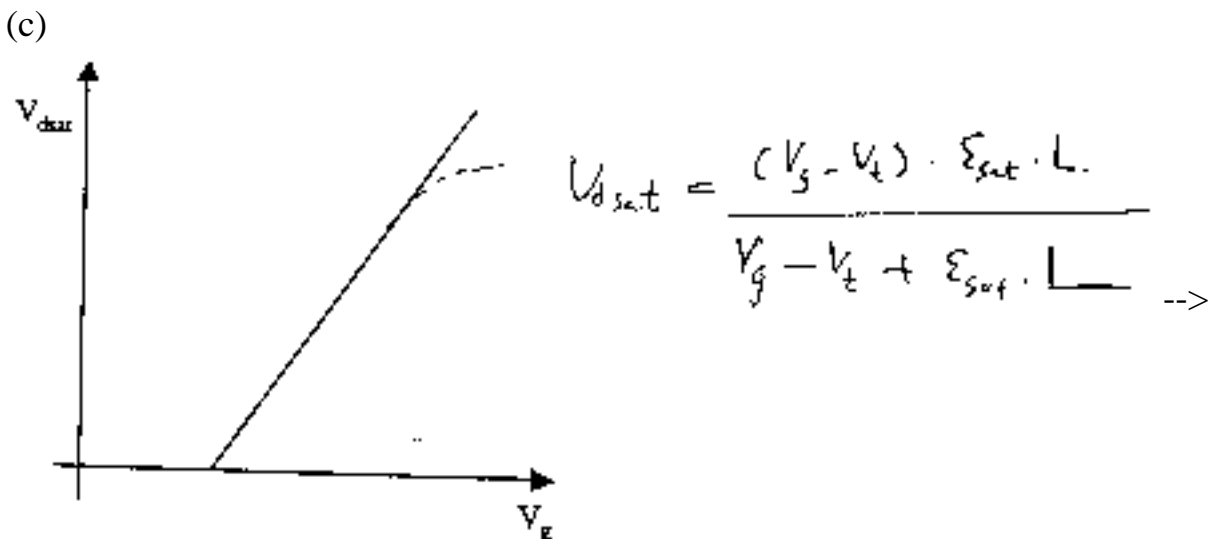
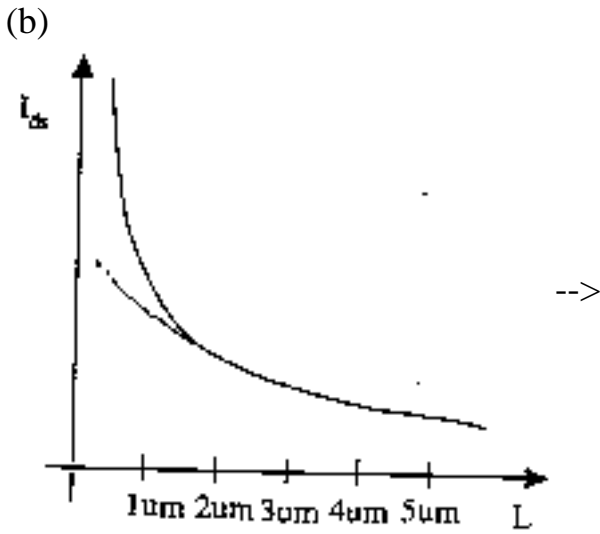
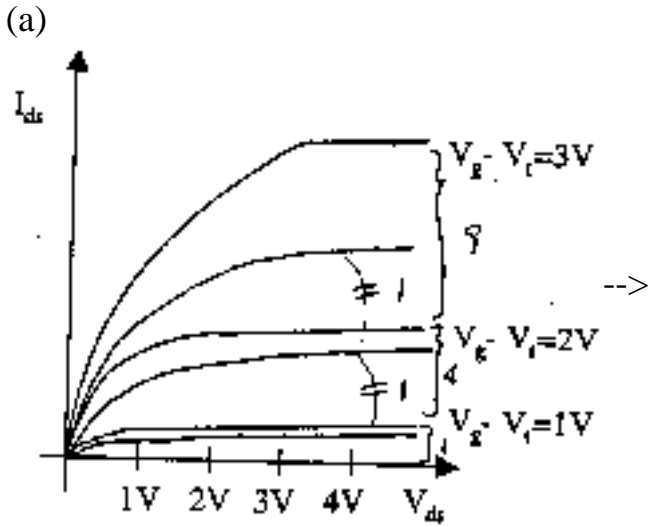


(c) Reverse the doping types of the source/drain, body, and gate, i.e. change from NMOSFET to PMOSFET. Select the proper quadrant. Source and body are tied to ground (0V). Consider  $\mu_{Un} \neq \mu_{Up}$ . (10 pts)



**Problem #3**

The printed curves in each of the figures are drawn for a MOSFET without consideration for velocity saturation. Draw new curves in each figure to indicate the effect of velocity saturation. (15 pts: 5 pts each)



$$V_{dsat} = (V_g - V_t) \cdot E_{sat} \cdot L / (V_g - V_t + E_{sat} \cdot L)$$

### Problem #4

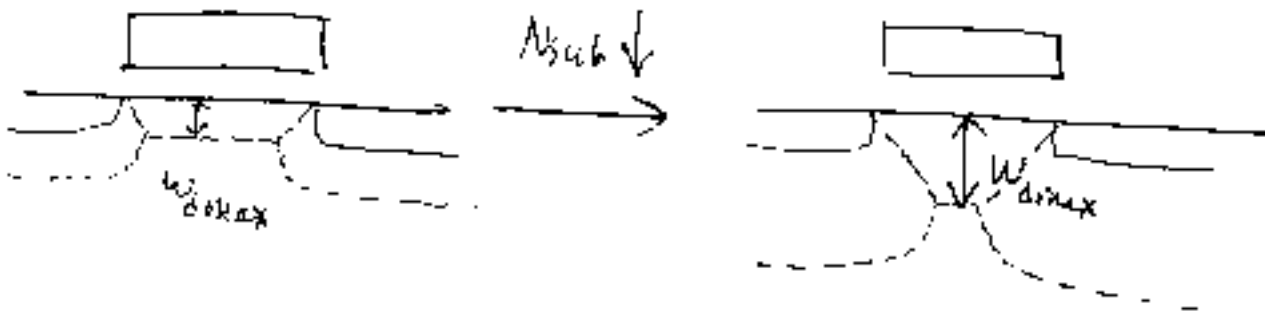
Indicate in the table below the consequences of decreasing the body doping concentration,  $N_{sub}$ , in an NMOSFET by checking two appropriate boxes (Increase/Decrease and Desirable/Undesirable) for each line. (20 pts)

	Increases	Decreases	Desirable	Undesirable	Points
Transconductance, $G_{m,sat}$	X		X		5 pts
Subthreshold swing, $S$		X	X		5 pts
$V_t$ roll-off (Short channel effect)	X			X	5 pts
Body effect coefficient, ALPHA		X	X		5 pts

i)  $G_{m,sat} = dI_{dsat}/dV_{gs} = \mu C_{ox} W/L * (V_g - V_t)$   $N_{sub}$  down implies  $V_t$  down implies  $G_{m,sat}$  up desirable

ii)  $S = 60mV * (1 + C_{dep}/C_{ox})$   $N_{sub}$  down implies  $W_{dmax}$  up implies  $C_{dep}$  down implies  $S$  down desirable

iii)



$V_t$  roll-off increases implies undesirable

iv)  $ALPHA = C_{dep}/C_{ox}$  ;  $N_{sub}$  down ;  $C_{dep}$  down ; ALPHA down

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