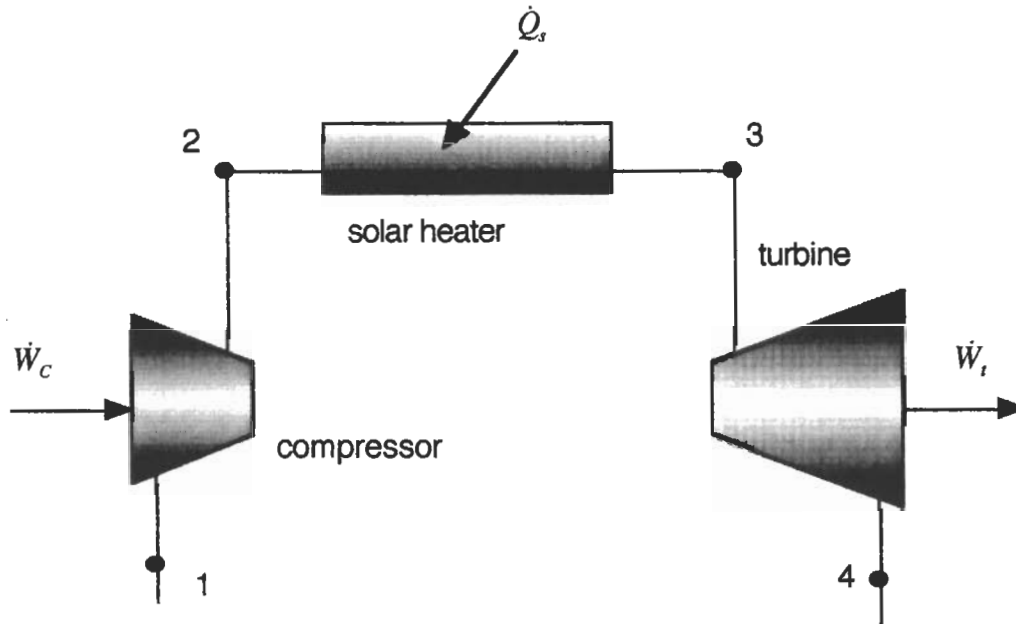


Midterm I

Name W/sala

Instructions: Do both problems. Show all work and make sure that your final answers are clearly distinguishable *with proper units*.

1. (50 points)



Steam enters the compressor shown in the schematic above at state 1 with $P_1 = 100$ kPa and $T_1 = 250$ °C. The steam flow rate is 1.2 kg/s. The compressor operates reversibly and adiabatically. The exit pressure for the compressor is $P_2 = 500$ kPa. The steam then enters a solar heater that transfers heat into the steam flow at a rate of 1389 kW. The pressure drops to 400 kPa at the exit (3) of the heater. The pressure at the turbine exit (P_4) is 100 kPa.

- Determine the power input into the compressor.
- Determine the specific enthalpy at state 3.
- Assuming the turbine operates reversibly and adiabatically, find the power output of the turbine.
- Determine the turbine work output and estimate the exit temperature if the turbine is adiabatic with an efficiency of 0.8.

$$\begin{aligned}
 (a) \quad & h_1 = 2974.5 \text{ kJ/kg} & s_2 = s_1 = 8.0346 & \rightarrow \begin{cases} T_2 = 500^\circ\text{C} \\ h_2 = 3484.5 \end{cases} \\
 & s_1 = 8.0346 \text{ kJ/kgK} & P_2 = 500 \text{ kPa} &
 \end{aligned}$$

$$\dot{W}_c = \dot{m} (h_2 - h_1) = 1.2 (3484.5 - 2974.5) = \underline{612 \text{ kW}}$$

$$(b) \quad h_3 = h_2 + \frac{\dot{Q}_5}{\dot{m}} = 3484.5 + \frac{1389}{1.2} = \underline{4642} \text{ kJ/kg} \quad \left. \begin{array}{l} T_3 = 1000^\circ\text{C} \\ s_3 = 9.3396 \end{array} \right\}$$
$$P_3 = 400 \text{ kPa}$$

$$(c) \quad \dot{W}_{t,5} = \dot{m} (h_3 - h_{4s})$$

$$\left. \begin{array}{l} s_{4s} = s_3 = 9.3396 \\ P_{4s} = 100 \text{ kPa} \end{array} \right\} h_{4s} = 3929.4$$

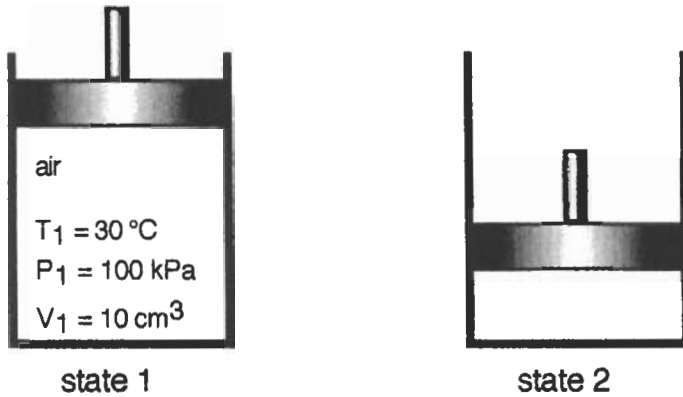
$$\dot{W}_{t,5} = 1.2 (4642 - 3929) = \underline{855.6} \text{ kW}$$

$$(d) \quad \dot{W}_t = 0.8 (855.6) = \underline{684.5} \text{ kW}$$

$$h_4 = h_3 - \frac{\dot{W}_t}{\dot{m}} = 4642 - \frac{684.5}{1.2} = 4072 \text{ kJ/kg}$$

$$P_4 = 100 \text{ kPa}$$

$$\Rightarrow T_4 = 700 + \frac{4072 - 3929}{4163 - 3929} (800 - 700) = \underline{762}^\circ\text{C}$$



2. (50 points) In analyzing this system, treat the air as an ideal gas with constant specific heats.

The piston and cylinder device above contains air. Initially (state 1) the air inside is at a pressure of 100 kPa, the temperature is 30 °C and the system volume is 10 cm³. The gas is then compressed to state 2 reversibly and isothermally. The volume in state 2 is 1.5 cm³.

- Determine the pressure in state 2
 - Determine the work done compressing the gas from state 1 to state 2
 - Determine the change in entropy for the system from state 1 to state 2
 - Determine the heat transfer for the process from state 1 to state 2.
- e. An inventor claims to have designed a device that compresses air adiabatically from state 1 above to a final state f in which $P_f = 500\text{ kPa}$ and $T_f = 200\text{ }^\circ\text{C}$. Is such a device possible? Justify your answer.

$$m = \frac{P_1 V_1}{R T_1} = \frac{100,000 (10^{-5})}{.287(1000)(303)} = 1.15 \times 10^{-5} \text{ kg}$$

air
 $c_p = 1.005 \text{ kJ/kgK}$
 $c_v = 0.718$
 $R = 0.287$
 $k = 1.400$

$$(a) P_2 = \frac{V_1}{V_2} P_1 \quad (\text{for isothermal})$$

$$\Rightarrow P_2 = \left(\frac{10}{1.5}\right) 100 = \underline{666.7 \text{ kPa}}$$

$$(b) W = \int_1^2 P dV = \int_1^2 \frac{mRT}{V} dV = mRT \ln(V_2/V_1)$$

$$= (1.15 \times 10^{-5}) (.287)(1000)(303) \ln(1.5/10) = \underline{1.897 \text{ J}}$$

$$(c) \quad S_2 - S_1 = m(s_2 - s_1) = m c_v \ln(T_2/T_1) + m R \ln(v_2/v_1) \\ = 1.15 \times 10^{-5} (1.287) \ln(1.5/1.0) = -6.26 \times 10^{-6} \text{ kJ/K}$$

$$(d) \quad \Delta U = 0 \text{ since } \Delta T = 0 \text{ so} \\ \Delta U = 0 = Q - W \rightarrow Q = W = \underline{-1.897 \text{ J}}$$

$$(e) \quad 1^{\text{st}} \text{ Law requires } \Delta U = -W \\ \rightarrow W = -\Delta U = -m c_v (T_f - T_i) \\ = -1.15 \times 10^{-5} (1.718) (200 - 30) = -1.40 \times 10^{-3} \text{ kJ}$$

this is OK.

$$2^{\text{nd}} \text{ Law Requires } dS \geq \frac{\delta Q}{T} \rightarrow dS \geq 0 \rightarrow S_2 - S_1 \geq 0$$

$$S_2 - S_1 = m c_p \ln(T_2/T_1) - m R \ln(P_2/P_1) \\ = 1.15 \times 10^{-5} (1.005) \ln(473/303) - 1.15 \times 10^{-5} (1.287) \ln(500/1.0) \\ = -1.64 \times 10^{-7} \text{ kJ/K}$$

this violates the 2nd Law \rightarrow impossible