

# ME109 – Heat Transfer

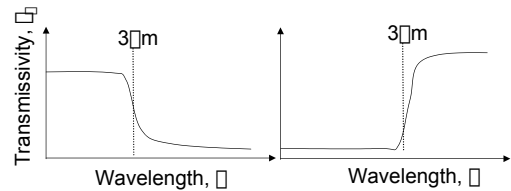
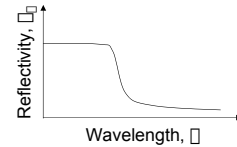
## Final Exam; Instructor: Prof. A. Majumdar

December 18, 2004; Time: 12:30-3:30 pm; Maximum Points = 100

NOTE: This is an open book, open notes exam.

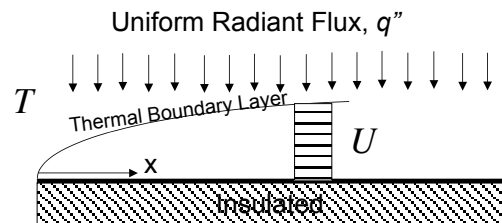
1. Give brief answers with explanation and reasoning.

- (i) Show that the Biot number,  $Bi = hL/k$ , is the ratio of two thermal resistances; internal conduction resistance and external thermal resistances. (4)
- (ii) The spectral reflectivity of a diffuse opaque surface has the following spectral distribution. If the temperature increases, will the total-hemispherical emissivity increase or decrease with temperature. (4)
- (iii) The resistance network analysis used for conduction can be combined with the radiation network analysis used radiation, when both conduction and radiation are relevant. True or False. Explain. (4)
- (iv) It is widely believed that greenhouse gases in the atmosphere lead to global warming. Which of the following spectral transmissivity does the atmosphere have to produce greenhouse effect. (4)
- (v) At a surface, the velocity of a fluid is zero, such that only conduction leads to heat transfer between a solid and a fluid. What, then, is the role of convection, i.e. when you increase the velocity, why does the heat transfer increase? (4)



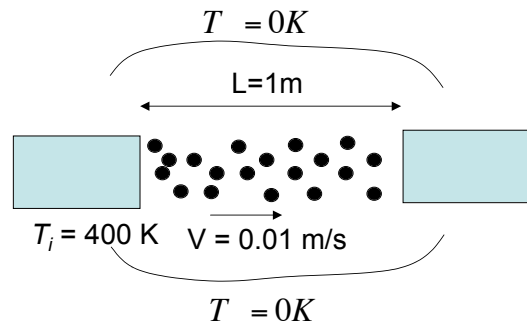
2. A silicon chip of thickness,  $d = 0.5$  mm, has a surface area,  $A = 2$  cm x 2 cm. It is packaged in a way that the heat transfer coefficient between the chip and ambient air is  $h = 500$  [ $\text{W}/\text{m}^2\text{-K}$ ] on both the 2 cm x 2 cm surfaces of the chip. At  $t = 0$ , the power input to the chip is turned on to  $P_o = 100$  W. Properties of silicon are: thermal conductivity,  $k = 150$   $\text{W}/\text{m-K}$ ; density,  $\rho = 2300$   $\text{kg}/\text{m}^3$ ; and heat capacity,  $C_p = 700$   $\text{J}/\text{kg-K}$ .
  - (i) Based on 1<sup>st</sup> law of thermodynamics, develop an equation for the temperature of the silicon chip as a function of time. (5)
  - (ii) Develop an expression and calculate the thermal time constant,  $\tau$  for the chip. (5)
  - (iii) Calculate the steady state temperature rise,  $\Delta T_{ss} = T_{ss} - T_\infty$ . (10)

3. A flat opaque plate exchanges radiative heat transfer with its surroundings such that a net uniform  $q''$  (see figure) is absorbed. The bottom surface the plate is insulated, whereas on the top surface a transparent fluid at temperature  $T$  and velocity  $U$  flows over the plate. The convection is such that the thermal boundary layer is much thicker than the velocity boundary layer. In fact, the velocity can be assumed to be  $U$  across the thermal boundary layer. Using the integral method, determine the temperature of the plate surface along the flow direction, i.e.  $x$  direction, in terms of  $U$ ,  $T$ ,  $q''$ , and thermal diffusivity,  $\alpha$ . (Note: the heat flux is uniform, but not the surface



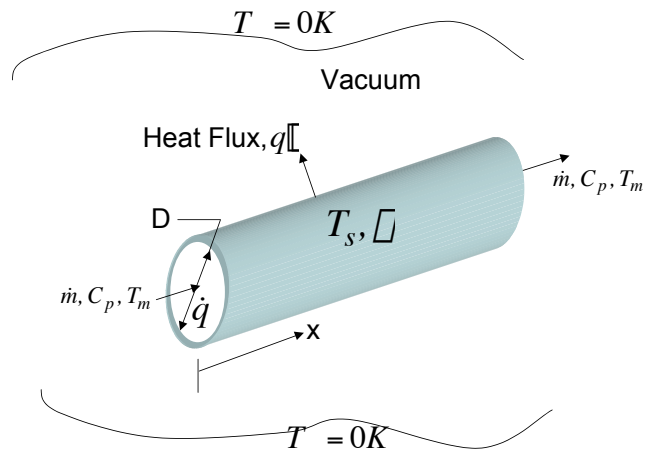
temperature) Integral energy equation: 
$$\frac{d}{dx} \int_0^{\delta} \rho u (T - T_s) dy = \alpha \left. \frac{\partial T}{\partial y} \right|_{y=0} \quad (20)$$

4. A radiative heat exchanger used in space uses small aluminum balls of,  $\rho C = 2 \times 10^6 \text{ J/m}^3\text{-K}$ , diameter  $D = 0.1 \text{ mm}$  to flow through a region that is fully enclosed by space, which is assumed to be a temperature of  $0 \text{ K}$ . The balls enter the heat exchanger at  $400 \text{ K}$  and move at a speed of  $0.01 \text{ m/s}$ . The heat exchanger length is  $1 \text{ m}$ . The emissivity of the outer surface of the ball is  $1$ . Assume that lumped capacitance can be used and that neighboring balls and the tubes at either end do not influence the heat transfer of an individual ball.



- (i) Using first law of thermodynamics, derive an equation for the time variation of the temperature of the ball? (5)
- (ii) Solve the equation to find the temperature of a ball at the exit of the heat exchanger. (5)
- (iii) What is the energy transferred by a single ball during its passage through the heat exchanger? (5)
- (iv) What is the effectiveness of the heat exchanger? (5)

5. Consider an opaque tube of diameter  $D = 0.01 \text{ m}$  through which there is a thermally and hydrodynamically fully developed flow of reacting gases at a mass flow rate of  $\dot{m} = 0.001 \text{ kg/s}$  and heat capacity of  $C_p = 1 \text{ kJ/kg-K}$ . The fluid enters the tube at a mean temperature of  $T_{mi} = 600 \text{ K}$ . As the gases flow through the tube, the reaction produces an energy generation rate of  $\dot{q} = 10^6 \text{ W/m}^3$  per unit volume inside the tube. Because the fluid inside the tube is hotter than the tube surface temperature,  $T_s$ , heat is transferred from the fluid to the tube walls, with a heat transfer coefficient,  $h = 25 \text{ W/m}^2\text{-K}$ , which remains constant along  $x$ . The heat transfer conditions are such that both the mean fluid temperature,  $T_m$ , and the heat flux,  $q''$ , remain unchanged along the  $x$ -direction. Assume the outer and inner surfaces of the tube to be at the same temperature, i.e., the tube poses no thermal resistance. The tube is used in a spacecraft such that the outer surface of the tube is completely surrounded by space ( $T = 0 \text{ K}$ ) and transfers heat by radiation.



- (i) Using first law of thermodynamics, derive an equation for the variation of the mean fluid temperature,  $T_m$ , as a function of  $x$  inside the tube in terms of  $\dot{q}$ ,  $\dot{m}$ ,  $C_p$ ,  $T_{mi}$ ,  $T_s$ . (5)
- (ii) Given the fact that  $T_m$  does not change with  $x$ , derive a relation for the surface temperature,  $T_s$ , in terms the parameters given above. What is the value of  $T_s$ ? (5)
- (iii) What is the heat flux  $q''$ ? (3)
- (iv) What is the total-hemispherical emissivity,  $\epsilon$  of the outer tube surface? (7)