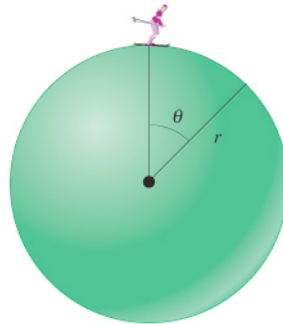
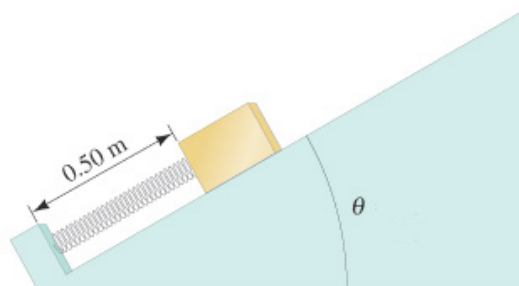


1. (20 points) A skier of mass m starts from rest at the top of a solid sphere of radius r and slides down its frictionless surface.
 - a) At what angle, θ , will the skier leave the sphere?
 - b) Now, instead of a skier, consider a ring of radius R and mass m . Assuming the ring rolls without slipping, at what angle, θ , will the ring leave the sphere?



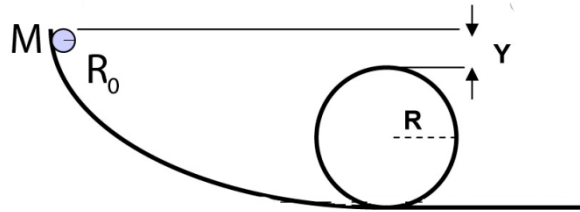
2. (20 points) A spring with spring constant $k = 80$ N/m has an equilibrium length of 1.00 m. The spring is compressed to a length of 0.5 m and a mass of $m = 1.8$ kg is placed at its free end on a frictionless slope which makes an angle of $\theta = 37^\circ$ with respect to the horizontal. The spring is then released. [Note: you may use the approximations $\sin 37^\circ = 0.6$ and $\cos 37^\circ = 0.8$ for simplicity]
 - a) If the mass is *not* attached to the spring, how far up the slope will the mass move before coming to rest?
 - b) If the mass *is* attached to the spring, how far up the slope will the mass move before coming to rest?
 - c) Now the incline has a coefficient of kinetic friction μ_k . If the block, attached to the spring, is observed to stop just as it reaches the spring's equilibrium position, what is the coefficient of friction?



3.

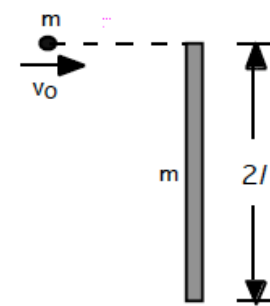
- a) (10 points) Calculate the moment of inertia of a uniform solid sphere of radius R_0 and mass M for an axis through its center.
- b) (15 points) What should be the minimum height, Y , above the loop shown below, that the disk must be released so that it can roll without slipping and still make it around the loop of radius R ? If you were unable to solve part (a), $I_{\text{sphere}} = \frac{2}{5} MR_0^2$

(Hint: The sphere is not a point object - do not neglect its radius!)



4. (15 points) A rocket traveling at a speed 1850 m/s away from the Earth at an altitude of 6400 km fires its rockets, which eject gas at a speed of 1300 m/s relative to the rocket. If the mass of the rocket at this moment is 25000 kg and an acceleration of 1.5 m/s^2 is desired, at what rate must the gases be ejected?

5. (20 points) A plank of length $2l$ and mass m lies on a frictionless plane. A ball, also of mass m , strikes the end of the plank with speed v_0 , as shown. After the collision, the ball continues along the original line of motion with decreased speed. Mechanical energy is conserved in the collision.



- a) Find the final velocity of the ball, v_f .
- b) The experiment is repeated, but this time the plank is pivoted (pegged to the ground) at its lower end. What is the new final velocity of the ball?