

Chemistry 1B, Exam III
April 12, 2007
Professor R.J. Saykally

Name Key
TA _____

1. (15) _____
2. (20) _____
3. (20) _____
4. (15) _____
5. (15) _____
6. (15) _____

TOTAL EXAM SCORE (100) _____

Rules:

- Work all problems to 2 significant figures
- No lecture notes or books permitted
- No word processing calculators
- Time: 90 minutes
- Show all work to get partial credit
- Periodic Table, Tables of Physical Constants, and Conversion Factors included

A vertical ruler scale from 0 to 6 inches. The scale is marked with major tick marks at every inch from 0 to 6. There are also smaller, unlabeled tick marks between each major mark, representing fractions of an inch.

Periodic Table of the Elements

Note: Atomic masses shown here are the 1983 IUPAC values (maximum of six significant figures).

Physical Constants

Standard acceleration of terrestrial gravity	$g = 9.80665 \text{ m s}^{-2}$ (exactly)
Avogadro's number	$N_0 = 6.022137 \times 10^{23}$
Bohr radius	$a_0 = 0.52917725 \text{ \AA} = 5.2917725 \times 10^{-11} \text{ m}$
Boltzmann's constant	$k_B = 1.38066 \times 10^{-23} \text{ J K}^{-1}$
Electron charge	$e = 1.6021773 \times 10^{-19} \text{ C}$
Faraday constant	$\mathcal{F} = 96,485.31 \text{ C mol}^{-1}$
Masses of fundamental particles:	
Electron	$m_e = 9.109390 \times 10^{-31} \text{ kg}$
Proton	$m_p = 1.672623 \times 10^{-27} \text{ kg}$
Neutron	$m_n = 1.674929 \times 10^{-27} \text{ kg}$
Ratio of proton mass to electron mass	$m_p/m_e = 1836.15270$
Permittivity of vacuum	$\epsilon_0 = 8.8541878 \times 10^{-12} \text{ C}^2 \text{ J}^{-1} \text{ m}^{-1}$
Planck's constant	$h = 6.626076 \times 10^{-34} \text{ J s}$
Speed of light in a vacuum	$c = 2.99792458 \times 10^8 \text{ m s}^{-1}$ (exactly)
Universal gas constant	$R = 8.31451 \text{ J mol}^{-1} \text{ K}^{-1}$ $= 0.0820578 \text{ L atm mol}^{-1} \text{ K}^{-1}$

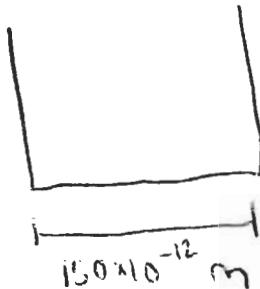
Values are taken from "Quantities, Units and Symbols in Physical Chemistry," International Union of Pure and Applied Chemistry, Blackwell Scientific Publications, 1988.

Conversion Factors

Standard atmosphere	$1 \text{ atm} = 1.01325 \times 10^5 \text{ Pa} = 1.01325 \times 10^5 \text{ kg m}^{-1} \text{ s}^{-2}$ (exactly)
Atomic mass unit	$1 \text{ u} = 1.660540 \times 10^{-27} \text{ kg}$
	$1 \text{ u} = 1.492419 \times 10^{-10} \text{ J} = 931.4943 \text{ MeV}$ (energy equivalent from $E = mc^2$)
Calorie	$1 \text{ cal} = 4.184 \text{ J}$ (exactly)
Electron volt	$1 \text{ eV} = 1.6021773 \times 10^{-19} \text{ J} = 96.48531 \text{ kJ mol}^{-1}$
Foot	$1 \text{ ft} = 12 \text{ in} = 0.3048 \text{ m}$ (exactly)
Gallon (U.S.)	$1 \text{ gallon} = 4 \text{ quarts} = 3.78541 \text{ L}$ (exactly)
Liter-atmosphere	$1 \text{ L atm} = 101.325 \text{ J}$ (exactly)
Metric ton	$1 \text{ metric ton} = 1000 \text{ kg}$ (exactly)
Pound	$1 \text{ lb} = 16 \text{ oz} = 0.45359237 \text{ kg}$ (exactly)

1. (3 points each)

- a) Using the quantum well model for the hydrogen atom, i.e. treating the atom as an electron in a one-dimensional box of length 150. pm, predict the wavelength of radiation emitted when the electron falls from the level with $n = 3$ to that with $n = 2$.



$$E_n = \frac{h^2 n^2}{8m\ell^2}$$

$$\begin{aligned}\Delta E_{3 \rightarrow 2} &= \frac{9h^2}{8m\ell^2} - \frac{4h^2}{8m\ell^2} = \frac{-5h^2}{8m\ell^2} \\ &= \frac{-5h^2}{3(9.1 \times 10^{-31} \text{ kg})(150 \times 10^{-12} \text{ m})^2} \\ &= 1.34 \times 10^{-17} \text{ J}\end{aligned}$$

$$\lambda = \frac{h \cdot c}{E} = \boxed{15 \text{ nm}}$$

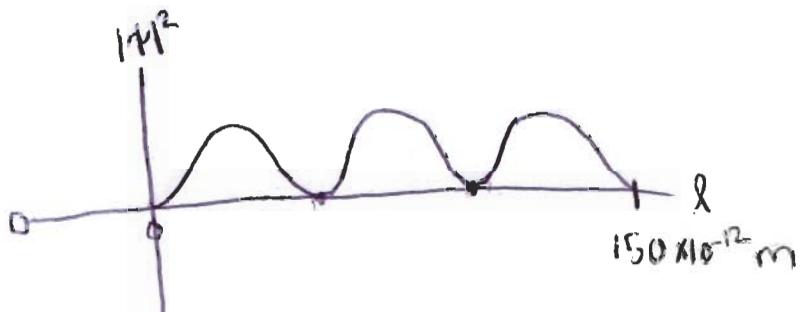
- b) What part of the spectrum is this in? UV

- c) Calculate the zero-point energy of the atom. $\rightarrow n = 1$

$$E_n = \frac{h^2 (1)^2}{8m_e \ell^2} = \boxed{2.68 \times 10^{-18} \text{ J}}$$

- d) Sketch the probability for finding the electron in the box state $n = 3$.

$n=3$; 2 nodes



- e) In principle, both $\sin \theta$ and $\cos \theta$, with $\theta = \frac{n\pi x}{L}$ are solutions to the Schrodger equation. Why is the $\cos \theta$ solution not used?

The boundary conditions require that $\psi(0)=0$; there is no probability of finding the particle at the edge of the box. Since $\cos(0)=1$, this part of the solution must be thrown out.

2. (5 points each) The sun emits radiant energy of $3.9 \times 10^{26} \text{ J}\cdot\text{s}^{-1}$; about 10% of this comes from the CNO fusion chain.

- a) Calculate the mass loss from the CNO chain.

$$\Delta E = \Delta m \cdot c^2$$

In one second:

$$\Delta E_{\text{sun}} = -3.9 \times 10^{26} \text{ J}$$

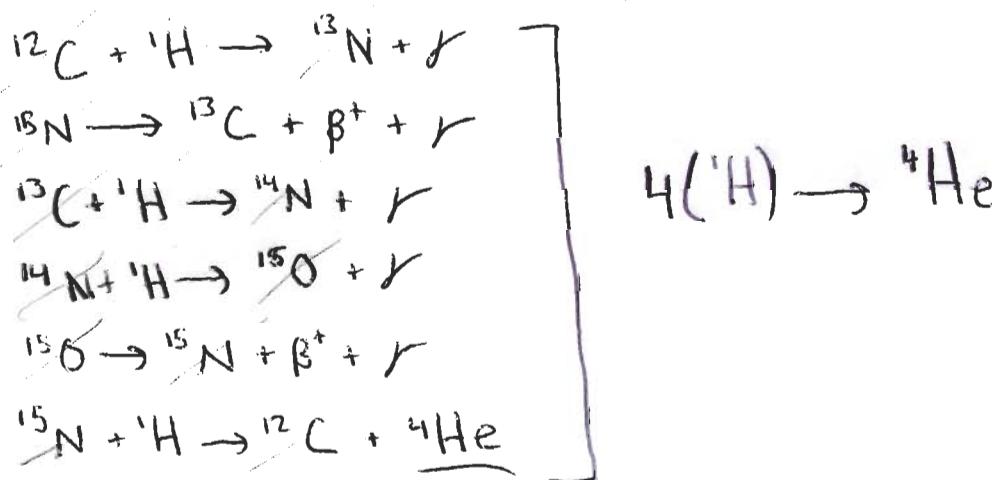
$$\Delta E_{\text{sun(CNO)}} = (0.1)(\Delta E_{\text{sun}})$$

$$-3.9 \times 10^{25} \text{ J} = (3.0 \times 10^8 \frac{\text{m}}{\text{s}})^2 \Delta m$$

$$\Delta m = -4.3 \times 10^8 \text{ kg}$$

$-4.3 \times 10^8 \frac{\text{kg}}{\text{s}}$

- b) Write out the CNO chain mechanism, showing that it gives the correct overall stoichiometry for the fusion reaction.



- c) Explain why the even-Z elements are more abundant than odd-Z elements for the representative elements.

This is due to the primary method of forming the elements being α -particle fusion reactions, leading to even-Z elements.

Second, the even-Z elements are more stable. Those elements with odd numbers of nucleons result in an unpaired proton.

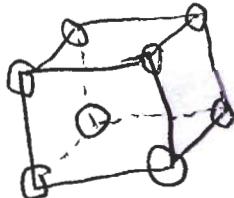
- d) How were the transition metals formed?

The transition metals following iron have endothermic nucleon binding energy and were only formed when stars become Supernovas, not during the big bang.

Before Fe, the transition metals could be formed by simple fusion in first and subsequent stars.

3. (5 points each) One form of silicon has density of $2.33 \text{ g}\cdot\text{cm}^{-3}$ and crystallizes in a simple cubic lattice with a unit cell edge of 543 pm and a band gap of 1.21 eV.

- a) What is the mass of each unit cell?



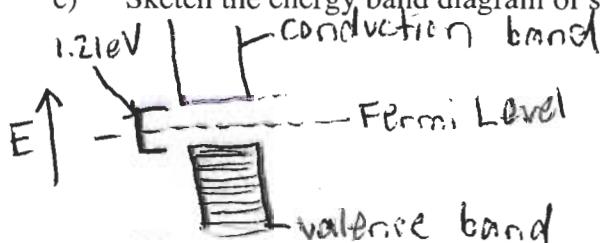
$$V = (543 \times 10^{-10} \text{ cm})^3 = 1.601 \times 10^{-22} \text{ cm}^3$$

$$V \cdot d = m \quad \frac{2.33 \text{ g}}{\text{cm}^3} \cdot 1.601 \times 10^{-22} \text{ cm}^3 = \boxed{3.73 \times 10^{-22} \text{ g}}$$

- b) How many silicon atoms does one unit cell contain?

1

- c) Sketch the energy band diagram of silicon, labeling the Fermi level.



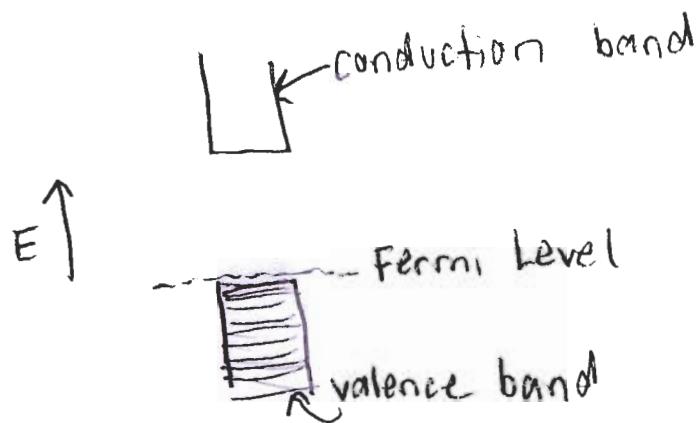
- d) What is the longest wavelength that can excite an electron in a crystal of pure cubic silicon?

longest wavelength = lowest Energy excitation = band gap

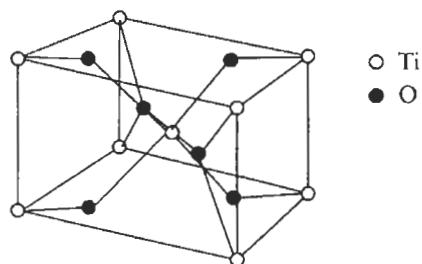
$$\lambda = \frac{h \cdot c}{E} = \frac{(4.136 \times 10^{-15} \text{ eV}\cdot\text{s})(3 \times 10^8 \text{ m/s})}{1.21 \text{ eV}} = \boxed{1.025 \times 10^{-6} \text{ m}} \\ \text{or } 1025 \text{ nm}$$

4. (5 points each)

- a) Sketch the band structure diagram expected for rutile (TiO_2), labeling the Fermi level.



- b) Calculate the number of cations, anions, and formula units per unit cell for rutile, given the unit cell.



$$\# \text{Ti} = 8 \text{corners} \times \frac{1}{8} + 1 \text{center} = 2 \text{Ti}$$

$$\# \text{O} = 4 \text{faces} \times \frac{1}{2} + 2 \text{center} = 4 \text{O}$$

2 cations / cell	$(\text{TiO}_2) \times 2$
4 anions / cell	2 formula units / cell

- c) What are the coordination numbers of the ions in rutile?

Cation = 6

$A_{\text{crown}} = 3$

5. (3 points each) Order the following atoms according to increase in the stated property.

- a) Electron affinity: Cl, I, P, Be

$\text{Be} < \text{P} < \text{I} < \text{Cl}$

- b) First ionization energy: Na, Mg, Al, Ar

$\text{Na} < \text{Al} < \text{Mg} < \text{Ar}$

- c) Atomic radius: K, F⁻, Rb, Co²⁵⁺, Br

$$C_0^{25^\circ} < F^+ < K < Br < R_b$$

d) Explain why gold is so unreactive.

- 1) Due to the Lanthanide Contraction, e^- experience a high effective nuclear charge and are held very tightly
- 2) It contains completely filled 6s and 5d (and 5p) orbitals. So ~~the~~ adding or subtracting e^- is unfavorable relative to the other elements.

f) Explain why gold is so much denser than silver.

$\text{Density} = \frac{\text{mass}}{\text{volume}}$. The mass per atom of gold is much higher. However, the interatomic distance, and thus volume, of gold is nearly identical due to the Lanthanide contraction, thus the density of gold is much higher than that of silver.

6. (5+10 points)

a) Describe the differences between diamagnetism, paramagnetism, ferromagnetism, and antiferromagnetism.

Diamagnetic atoms have no spin-unpaired electrons, and thus exhibit no or little magnetic properties, they are weakly repelled by a magnetic field. Paramagnetic materials contain atoms with spin unpaired electrons. They are magnetically active and move into magnetic fields. Ferromagnetic materials exhibit the property that neighboring atoms' spins* correlate with one another in a parallel manner, thus creating a permanent magnet after a magnetic field is applied. Anti-ferromagnetic materials exhibit atoms where neighboring spins are anti-parallel, cancelling each other out, ~~and thus~~ yielding no strong magnetic property.

- b) A silicon solar cell (band gap = 1.21 eV) with area $A = 10 \text{ cm}^{-2}$ experiences an insolation of $1000 \text{ watt}\cdot\text{hours}\cdot\text{cm}^{-2}$ per day, generating a voltage of 2.50 volts and a current of 3.0 amps. Calculate the efficiency of the solar cell.

$$P_{\text{cell}} = V \cdot I = 2.50 \text{ V} \times 3.0 \text{ A} = 7.5 \text{ W}$$

$$\frac{1000 \text{ W}\cdot\text{hr}}{\text{cm}^2 \cdot \text{day}} \times 10 \text{ cm}^2 \times \frac{3600 \text{ J}}{\text{watt}\cdot\text{hr}} \times \frac{1 \text{ day}}{24 \text{ hours}} \times \frac{1 \text{ hr}}{3600 \text{ s}} = 417 \text{ W}$$

$\approx \text{Power}_{\text{wind}}$
 available

$$\text{Efficiency} = \frac{7.5 \text{ W}}{417 \text{ W}} \times 100\% = \boxed{1.8\%}$$