

MIDTERM 1 SOLUTIONS

Date: February 27, 2007

1. [15 points]

1.a. [3 points] A project is a **temporary** endeavor undertaken to create a **unique** product or service.

Two characteristics make projects differ from operations:

[1 points] Temporary vs. ongoing

[1 points] Unique vs. repetitive

1.b. [4 points] Third-party beneficiary relationship: when **each of two** or more separate entities has a **valid contract** with a **common third entity**, they may be third-party beneficiaries of the contract between the “common” entity and the other noncommon entities.

1.c. [6 points] Give at least three of the following assumptions [2 points per assumption]:

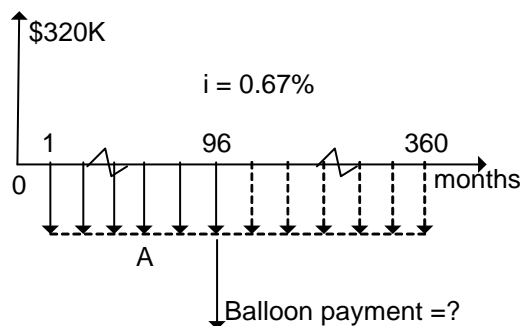
1. Cash flows are known
2. Cash flows are in constant-value currency (dollars); that is, we ignore the effect of inflation and we assume technological stability
3. Interest rate is known. The rate of return i required by an organization is a function of its cost of capital, attitude toward risk, and investment policy.
4. Comparisons are made with before-tax cash flows
5. Comparisons do not include intangible considerations
6. Comparisons do not include consideration of the availability of funds to implement alternatives.

2. [20 points] (Note: Students can use the effective interest rate per year $= (1 + \frac{0.08}{12})^{12} - 1 = 0.083 = 8.3\%$)

[3 points] The amount of the mortgage: $P = \$400K \times 0.8 = \$320K$

[3 points] Effective interest rate per month: $i = \frac{8}{12} = 0.67\% = 0.0067$

Number of monthly payments: 30 years \times 12 months/year = 360 months



Cash flow diagram [3 points]

[5 points] Equal monthly payments: $A = \$320K \times (A/P, i\%, n) = \$320K \times \frac{i(1+i)^n}{(1+i)^n - 1}$

$$A = \$320K \times \frac{0.0067(1 + 0.0067)^{360}}{(1 + 0.0067)^{360} - 1} = \$320K \times 0.0737 = \$2,357$$

Solution 1: [6 points] The balloon payment at year 8 = Present value of the monthly payments for the remaining years (22 years x 12 months/year = 264 months)

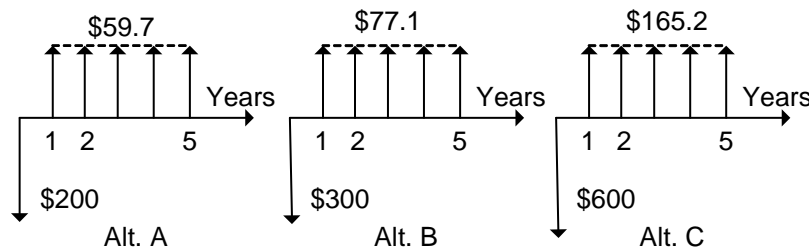
$$= \$2.357K \times (P/A, i\%, n) = \$2.357K \times \frac{(1 + 0.0067)^{264} - 1}{0.0067(1 + 0.0067)^{264}} = \mathbf{\$291.44K}$$

Solution 2: [6 points] The balloon payment at year 8 = Future value (at year 8) of the mortgage – Future value (at year 8) of the monthly payments for last 8 years (8 years x 12 months/year = 96 months)

$$= \$320K \times (F/P, i\%, n) - \$2.357K \times (F/A, i\%, n) = \$320K \times (1 + i)^n - \$2.357K \times \frac{(1 + i)^n - 1}{i}$$

$$= \$320K \times 1.0067^{96} - \$2.357K \times \frac{1.0067^{96} - 1}{0.0067} = \$607.51K - \$316.08K = \mathbf{\$291.43K}$$

3. [25 points]



Step 1: Find IRR for each alternative

[1 point] $NPV_A = -\$200 + \$59.7 \times (P/A, i\%, 5) = 0 \rightarrow (P/A, i\%, 5) = 3.3501$.

[2 points] Observe interest factor tables, $IRR_A \approx 15\%$

[1 point] $NPV_B = -\$300 + \$77.1 \times (P/A, i\%, 5) = 0 \rightarrow (P/A, i\%, 5) = 3.8911$.

[2 points] Observe interest factor tables, $IRR_B \approx 9\%$

[1 point] $NPV_C = -\$600 + \$165.2 \times (P/A, i\%, 5) = 0 \rightarrow (P/A, i\%, 5) = 3.6320$.

Observe interest factor tables, IRR_C is somewhere between 11% and 12%.

$NPV_C(11\%) = -\$600 + \$165.2 \times 3.6959 = \$10.56$

$NPV_C(12\%) = -\$600 + \$165.2 \times 3.6048 = -\$4.49$

[2 points] $\rightarrow IRR_C = 11\% + \frac{0 - \$10.56}{-\$4.49 - \$10.56} \times (12\% - 11\%) \approx 11.7\%$

[1 point] **Necessary condition:** $IRR_C \geq MARR \rightarrow MARR \leq 11.7\%$

Step 2: Find IRR's for investment increments (Note: since we just want to know when C is preferred, we do not have to find IRR_{B-A} . Of course, it is OK if you do that)

[1 point] $NPV_{C-B} = -\$300 + \$88.1 \times (P/A, i\%, 5) = 0 \rightarrow (P/A, i\%, 5) = 3.4052$.

Observe interest factor tables, IRR_{C-B} is somewhere between 12% and 15%.

[1 point] $NPV_{C-B}(12\%) = -\$300 + \$88.1 \times 3.6048 = \$17.58$

[1 point] $NPV_{C-B}(15\%) = -\$300 + \$88.1 \times 3.3522 = -\$4.67$

[1 point] $\rightarrow IRR_{C-B} = 12\% + \frac{0 - \$17.58}{-\$4.67 - \$17.58} \times (15\% - 12\%) \approx 14.37\%$

[1 point] $NPV_{C-A} = -\$400 + \$105.5 \times (P/A, i\%, 5) = 0 \rightarrow (P/A, i\%, 5) = 3.7915$.

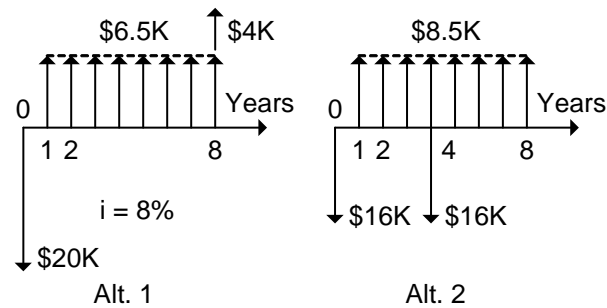
[3 points] Observe interest factor tables, $IRR_{C-A} \approx 10\%$.

[2 points] **Sufficient condition:** $IRR_{C-B} \geq MARR$ and $IRR_{C-A} \geq MARR \rightarrow MARR \leq 10\%$

[2 points] \rightarrow **Necessary and sufficient conditions:** $MARR \leq 11.7\%$ and $MARR \leq 10\%$
 \rightarrow **MARR $\leq 10\%$.**

4. [20 points]

The solutions are based on an eight-year analysis period and a replacement alternative 2 that is identical to the present alternative 2.



Cash flow diagram [4 points]

[4 points] $NPV_1 = -\$20K + \$6.5K \times (P/A, 8\%, 8) + \$4K \times (P/F, 8\%, 8)$
 $= -\$20K + \$6.5K \times 5.7466 + \$4K \times 0.5403 = \$19.51K$

[4 points] $NPV_2 = -\$16K + \$8.5K \times (P/A, 8\%, 8) - \$16K \times (P/F, 8\%, 4)$
 $= -\$16K + \$8.5K \times 5.7466 - \$16K \times 0.7350 = \$21.09K$

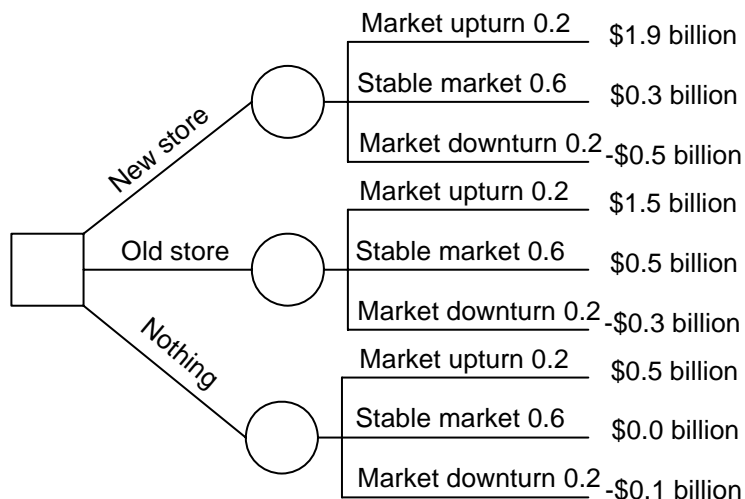
[2 points] $NPV_2 > NPV_1 > 0 \rightarrow$ Choose Alternative 2.

[2 points] This decision would be reversed if $NPV_1 \geq NPV_2$

[4 points] $\rightarrow -\$20K + \$6.5K \times 5.7466 + SV \times 0.5403 \geq \$21.09K$

$\rightarrow SV \geq \frac{\$21.09K + \$20K - \$6.5K \times 5.7466}{0.5403} = \$6.92K \rightarrow$ **Salvage value $\geq \$6,920$**

5. [20 points] 5.a.



Decision tree [5 points]

5.b. [5 points]

[1.5 points] EV (Build new store) = $1.9 \times 0.2 + 0.3 \times 0.6 - 0.5 \times 0.2 = \0.46 billion

[1.5 points] EV (Expand old store) = $1.5 \times 0.2 + 0.5 \times 0.6 - 0.3 \times 0.2 = \0.54 billion

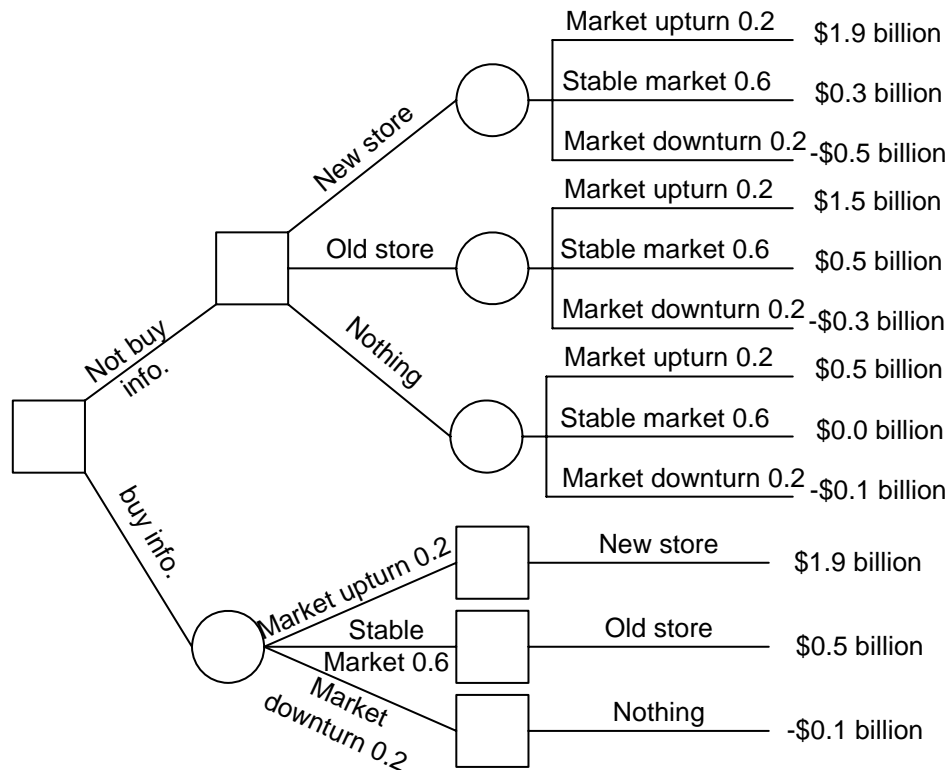
[1.5 points] EV (Do nothing) = $0.5 \times 0.2 + 0.0 \times 0.6 - 0.1 \times 0.2 = \0.08 billion

[0.5 point] → Expected net present value of “expand old store” is greatest → **Expand old store.**

5.c. [5 points]

Expected net present value (returns) of this optimal decision = $\$0.54$ billion = **\\$540 million**

5.d. [5 points] Perfect information



New decision tree [1 point]

[2 points] EV (with perfect information) = $1.9 \times 0.2 + 0.5 \times 0.6 - 0.1 \times 0.2 = \0.66 billion = **\\$660 million**

[2 points] EV (with perfect information) – EV (with no perfect information) = $\$660$ million - $\$540$ million = $\$120$ million > $\$10$ million → The building supply store should accept the ForSure’s offer.

TOTAL: 100