

Fall Semester 2003

Name: SOLUTIONS

UNIVERSITY OF CALIFORNIA AT BERKELEY
College of Engineering
Department of Materials Science and Engineering, Prof. E. E. Haller

Engineering 45

Exam #1 (40 pts.), Sept. 26

- 1.) (2 pts.) Gallium, one of the most important components of optoelectronic semiconductors, has an atomic weight of 69.75. It consists of the two isotopes ^{69}Ga and ^{71}Ga . What are the relative abundances of these two isotopes?

$$69.75 = x \cdot 69 + (1-x) \cdot 71$$

$$= -2x + 71$$

$$x = 0.625$$

$$62.5\% \text{ } ^{69}\text{Ga}$$

$$37.5\% \text{ } ^{71}\text{Ga}$$

- 2.) (5 pts.) The hydrogen atom consists of one proton binding one electron with an energy of $E_1 = -13.6\text{eV}$ in the ground state. There are higher lying bound states with energies

$$E_n = \frac{1}{n^2} E_1 \quad (n=2, 3, \dots)$$

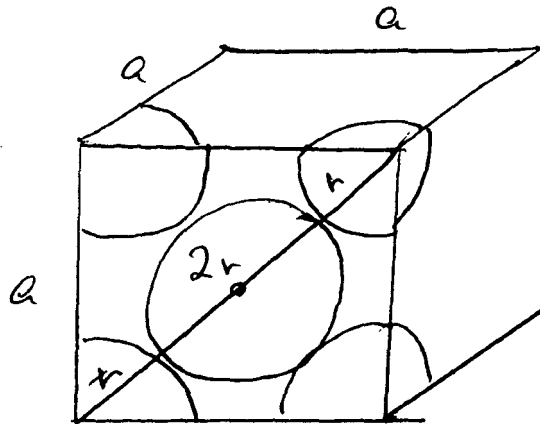
Assume the hydrogen atom has been excited into the $n=2$ state. Will shining visible light onto this excited hydrogen atom lead to full ionization? (visible range: $2\text{eV} < E_{\text{photon}} < 3\text{eV}$) $E_{\text{photon}} = hv = hc/\lambda$, with $h = 4.1375 \times 10^{-15} \text{eV}\cdot\text{s}$
Show your work!

$$E_2 = \frac{1}{2^2} (-13.6 \text{ eV})$$

$$= -3.4 \text{ eV}$$

Visible light ($2\text{eV} < E < 3\text{eV}$) cannot
ionize H in its $n=2$ state

- 3.) (4 pts.) Calculate the atomic packing factor (APF) for a FCC metal. (Hint: make a sketch of the FCC unit cell and figure out how many atoms occupy the cell.)



$$a\sqrt{2} = 4r \quad r = \frac{1}{4} a\sqrt{2}$$

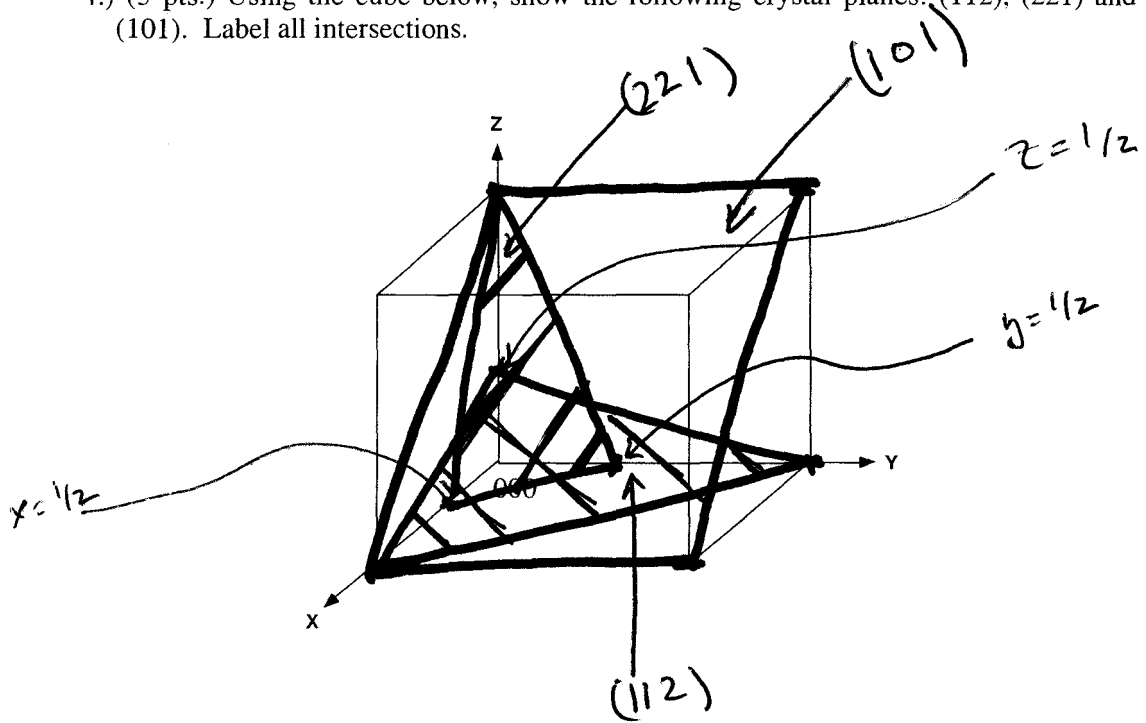
there are 4 atom volumes in the FCC unit cell

$$\text{Total atom volume: } 4 \times \frac{4\pi r^3}{3} = \frac{16}{3} \pi \left(\frac{1}{4} a\sqrt{2}\right)^3$$

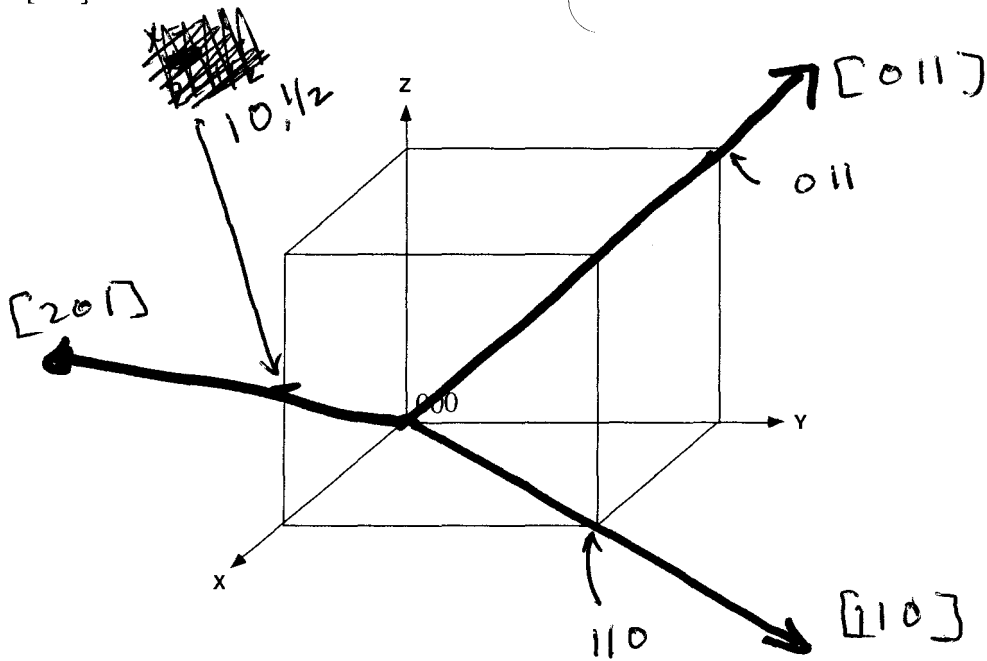
$$\text{Total unit cell volume: } a^3$$

$$\text{APF} = \frac{16}{3} \pi \left(\frac{\sqrt{2}}{4}\right)^3 = 0.74$$

4.) (3 pts.) Using the cube below, show the following crystal planes: (112), (221) and (101). Label all intersections.



5) (3 pts.) Using the cube below, show the following crystal directions: [110], [011], and [201]. Label all intersections.



- 6.) (4 pts.) Consider the family of directions $\langle 111 \rangle$. Which ones of these directions lie in the $(10\bar{1})$ plane?

use the dot product!

$$[10\bar{1}] \cdot [111] = 0$$

$$^a \quad [1\bar{1}1] = 0$$

$$^b \quad [11\bar{1}] = 0$$

$$^c \quad [1\bar{1}\bar{1}] = 0$$

- 7.) (5 pts.) The vacancy concentration in silicon is rising exponentially with temperature.

$$n_v = N_{Si} \exp\left(-\frac{E_v}{k_B T}\right)$$

with $N_{Si} = 5 \times 10^{22} \text{ cm}^{-3}$, $k_B = 8.62 \times 10^{-5} \text{ eV/K}$ and $E_v = 2 \text{ eV}$.

By what factor does n_v drop when the Si crystal cools down from 1600K to 1000K?

$10 \rightarrow 9$

$$\frac{n_v^{1600} - n_v^{1000}}{n_v^{1000}}$$

$$\frac{n_v(1600\text{K})}{n_v(1000\text{K})} = \frac{N_{Si}}{N_{Si}} \cdot \frac{\exp[-E_v/k_B T_1]}{\exp[-E_v/k_B T_2]}$$

$$= \exp\left(-E_v/k_B \left(\frac{1}{1600} - \frac{1}{1000}\right)\right)$$

$$\ln\left(\frac{n_v(1600)}{n_v(1000)}\right) = -\frac{E_v}{k_B} \left(\frac{1}{1600} - \frac{1}{1000}\right)$$

$$\frac{6.25 \times 10^4 - 10^{-3}}{-3.75 \times 10^{-3}}$$

$$= 8.700$$

-4-

$$\frac{n_v(1600)}{n_v(1000)} = \underline{\underline{6003}}$$

equation
with
ratio

8.) (5 pts.) Today I measured the resistances of the filaments of a 150W and a 40W incandescent light bulb. My Ohm Meter showed 7Ω and 30Ω , respectively. Calculate the resistances of these two light bulbs based on their specifications running at 110V.

The power P dissipated in Watts (W) is:

$$P = IV$$

The resistance R is: $R = \frac{V}{I}$

Compare your calculated result with the measurements. In case there are differences, explain these with physical arguments.

$$P = IV = \frac{V^2}{R}$$

150 watt bulb : $R = \frac{(110)^2}{150} = 80.7 \Omega$ + 2

compared to the 7Ω !
reading.

40 watt bulb : $R = \frac{(110)^2}{40} = 302.5 \Omega$ + 2
as compared to 30Ω !

The big difference in resistivity is related to the fact that the resistivity increases with temperature. + 1

An operating light bulb is very hot $\rightarrow R$ large;

The Ohm Meter does not heat the light bulb filament

$\rightarrow R$ small.

9.) (6 pts.) (a) The possibility to find an electron at energy E is given by the Fermi function F(E):

$$F(E) = \frac{1}{1 + \exp \frac{E - E_F}{k_B T}}$$

Determine F(E) at room temperature 300K for the following energies:

$$E - E_F = k_B T, 2k_B T, -k_B T, -2k_B T$$

$$F(E) = \begin{matrix} \downarrow \\ 0.269 \\ \downarrow \\ = 0.1194 \\ \downarrow \\ \approx 0.731 \leftarrow \\ \downarrow \\ = 0.881 \leftarrow \end{matrix}$$

(b) Assume the Fermi level E_F lies in the middle of the bandgap of Si ($E_G = 1.1\text{eV}$). Calculate the probability to find at room temperature ($T = 300\text{K}$) an electron at the conduction band edge.

$$F(E) = \frac{1}{1 + \exp \left[\frac{0.55\text{eV}}{8.62 \cdot 10^{-5}\text{eV/K} \cdot 300\text{K}} \right]}$$

$$= \underline{\underline{5.8 \times 10^{-10}}}$$

21.268

(c) as (b) but calculate the probability to find a hole at the valence band edge.

$$1 - F(E) = \text{prob. to find a hole}$$

$$= 1 - \frac{1}{1 + \exp \left[\frac{-0.55\text{eV}}{k_B \cdot 300\text{K}} \right]}$$

$$= \underline{\underline{5.8 \times 10^{-10}}}$$

10.) (3 pts.) True or False

- | | T | F |
|---|-------------------------------------|--|
| - Phosphorus forms a donor in silicon. | <input checked="" type="checkbox"/> | <input type="checkbox"/> |
| - Silicon forms a donor on an As site in GaAs. | <input type="checkbox"/> | <input checked="" type="checkbox"/> |
| - Germanium forms a donor on a Ga site in GaP. | <input checked="" type="checkbox"/> | <input type="checkbox"/> |
| - For a given temperature, intrinsic silicon contains more free carriers than intrinsic germanium. | <input type="checkbox"/> | <input checked="" type="checkbox"/> |
| - A semiconductor containing the same amount of donors as acceptors exhibits a free carrier concentration large than the intrinsic carrier concentration. | <input type="checkbox"/> | <input checked="" type="checkbox"/> |
| - A given doped semiconductor is dominated by the dopants over a finite temperature range. | <input checked="" type="checkbox"/> | <input type="checkbox"/> |
- deleted